



# Statistical Structures of Low Density Pedestrian Dynamics

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with:

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# Introduction & Motivation

- Walking pedestrians: *rich & complex dynamics*
  - Reliable models: relevant in science & technology
- Stochastic, nearly unpredictable motion
  - *Quantitative-(statistical) assessment of fluctuations?*
    - Measurements?
    - Rare behaviors?
    - Modeling?

# Introduction & Motivation

- This presentation:
  - “low density” pedestrian dynamics in a corridor
    - Quantitative-(statistical) models?
- Content:

# Introduction & Motivation

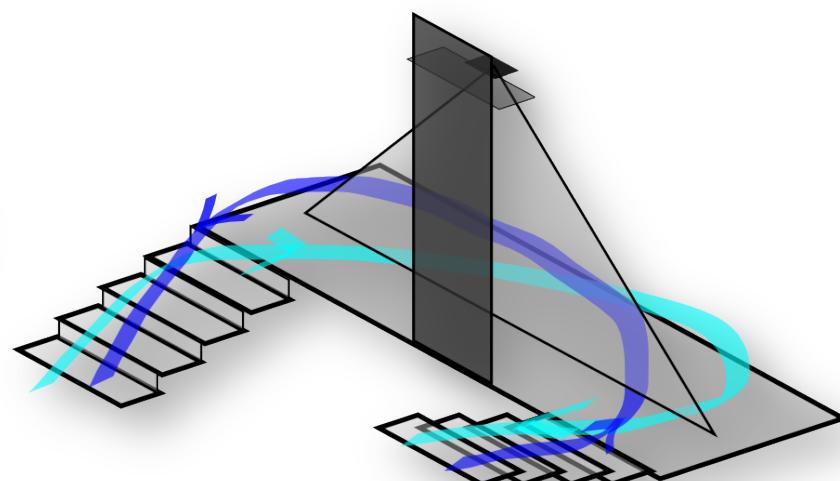
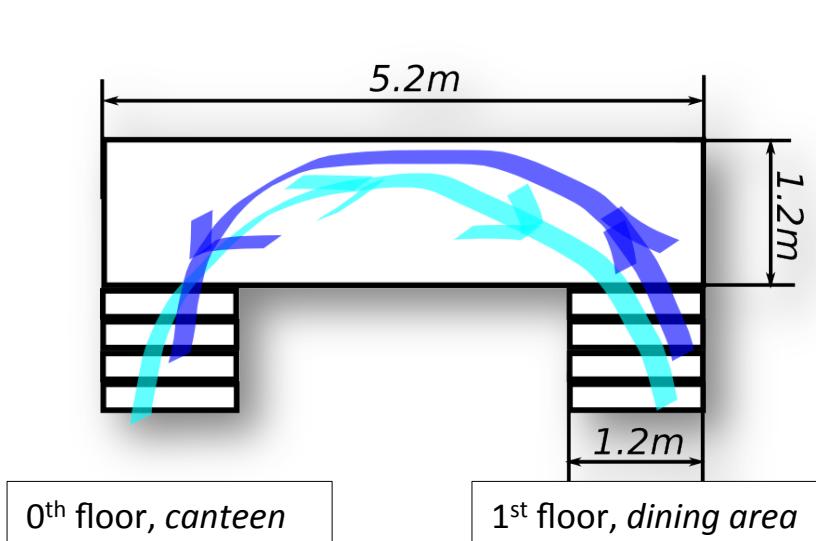
- This presentation:
  - “low density” pedestrian dynamics in a corridor
    - Quantitative-(statistical) models?
- Content:
  1. High statistic resolution measurements
  2. Analysis of stochastic fluctuations

Quantitative model up to rare events

# High statistics measurements approach



*Metaforum building, TU/e*

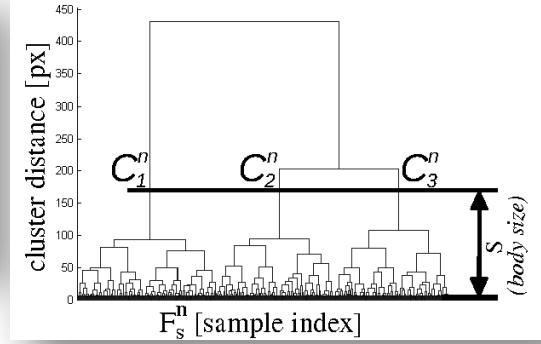
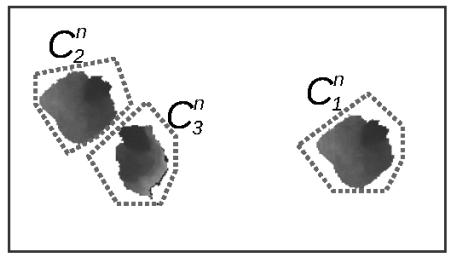


# Pedestrian tracking technique

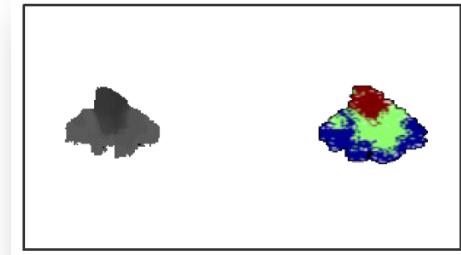
- **1. Heads detection**

- Overhead, 3d view

- Depthmap-based, Via Microsoft Kinect
    - (Complete) clustering of “depth-cloud”
    - 15Hz sampling



Clusterization tree cut at “body scale”



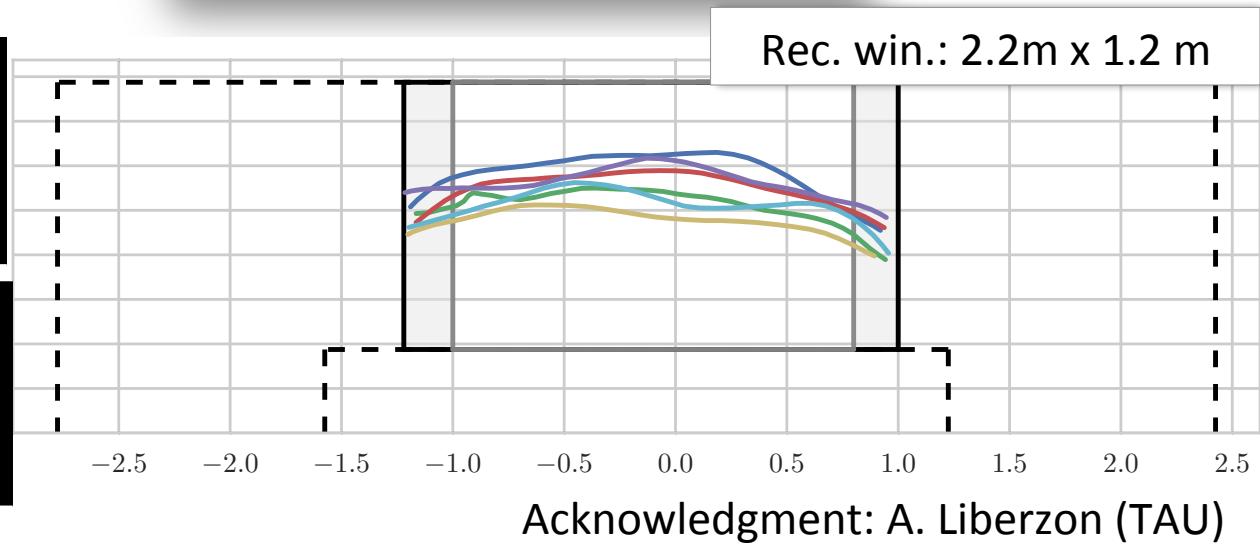
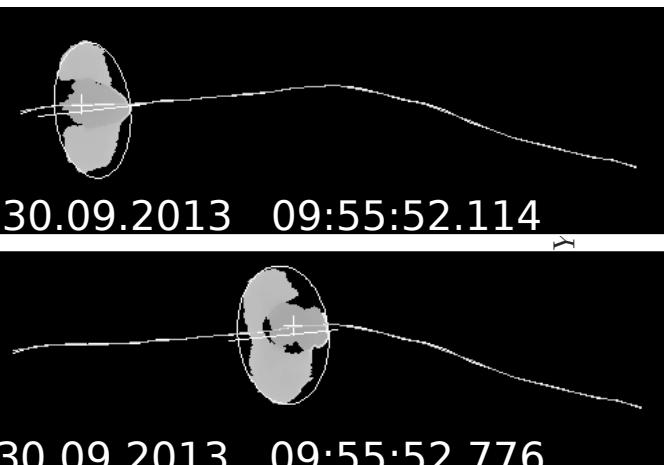
Heads marked as low depth (closest) percentiles

(Seer et Al., 2014)

# Pedestrian tracking technique

- **2. Head tracking**
  - Head Spatio-Temporal matching via 3DPTV
    - from experimental fluid mechanics  
(Willneff et Al. 2002, Willneff 2003)
    - Nearest search with velocity prediction

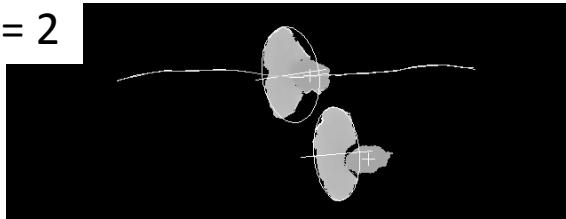
- Implementation:



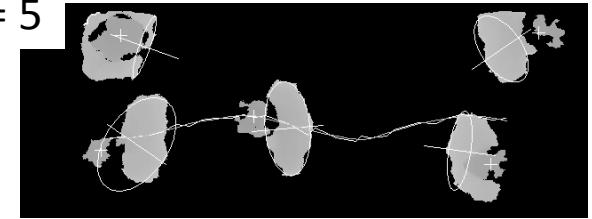
Acknowledgment: A. Liberzon (TAU)

# Traffic - local occupancy

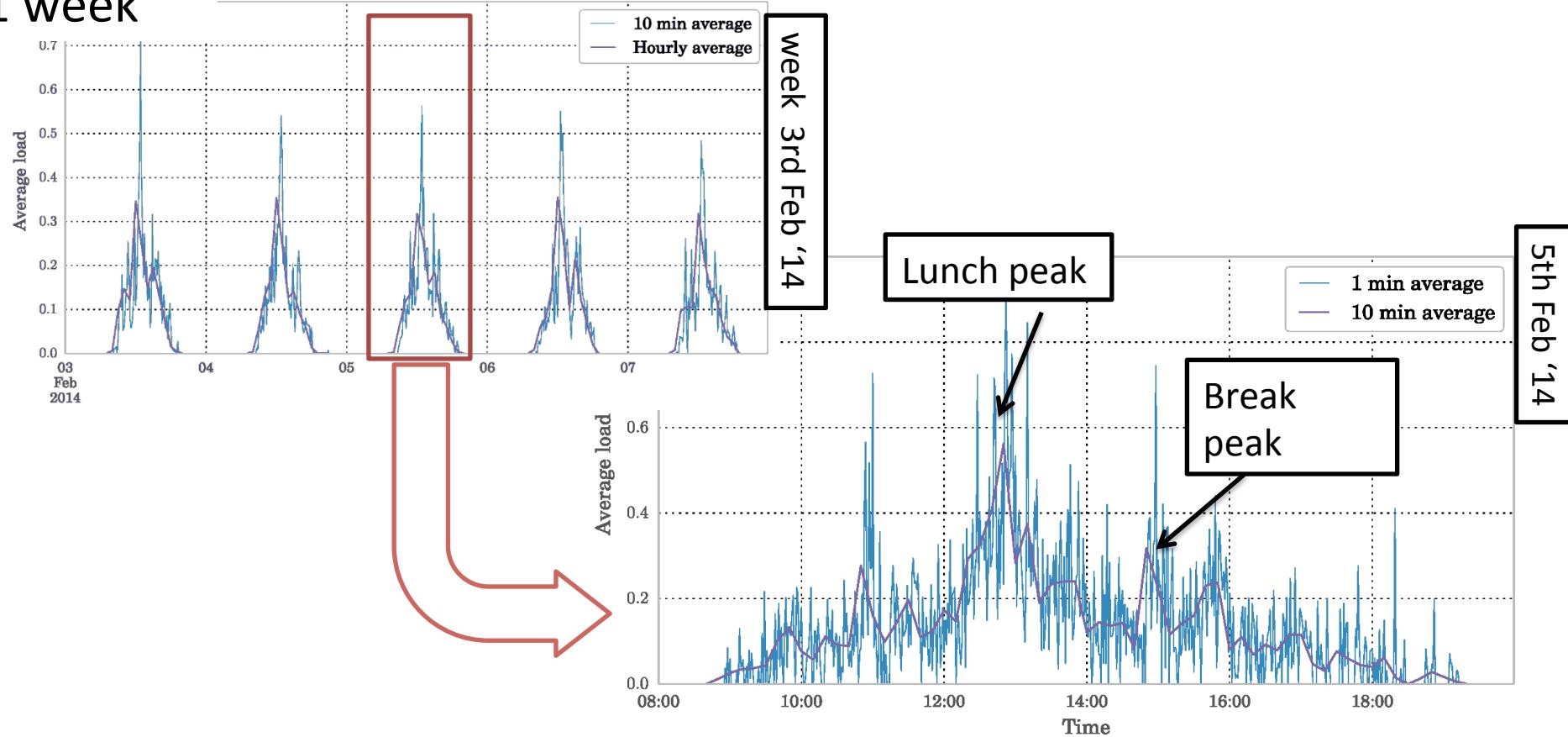
Occupancy = 2



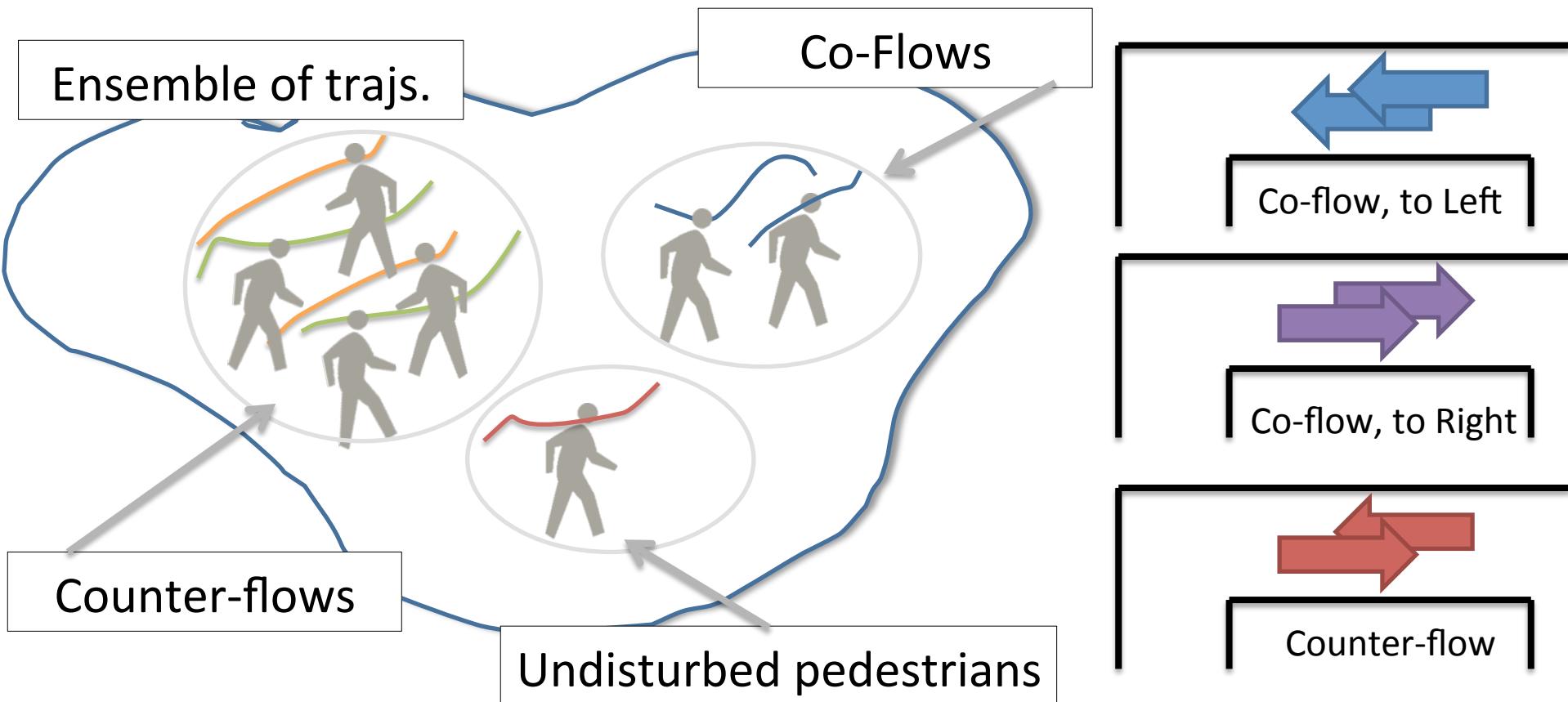
Occupancy = 5



1 week



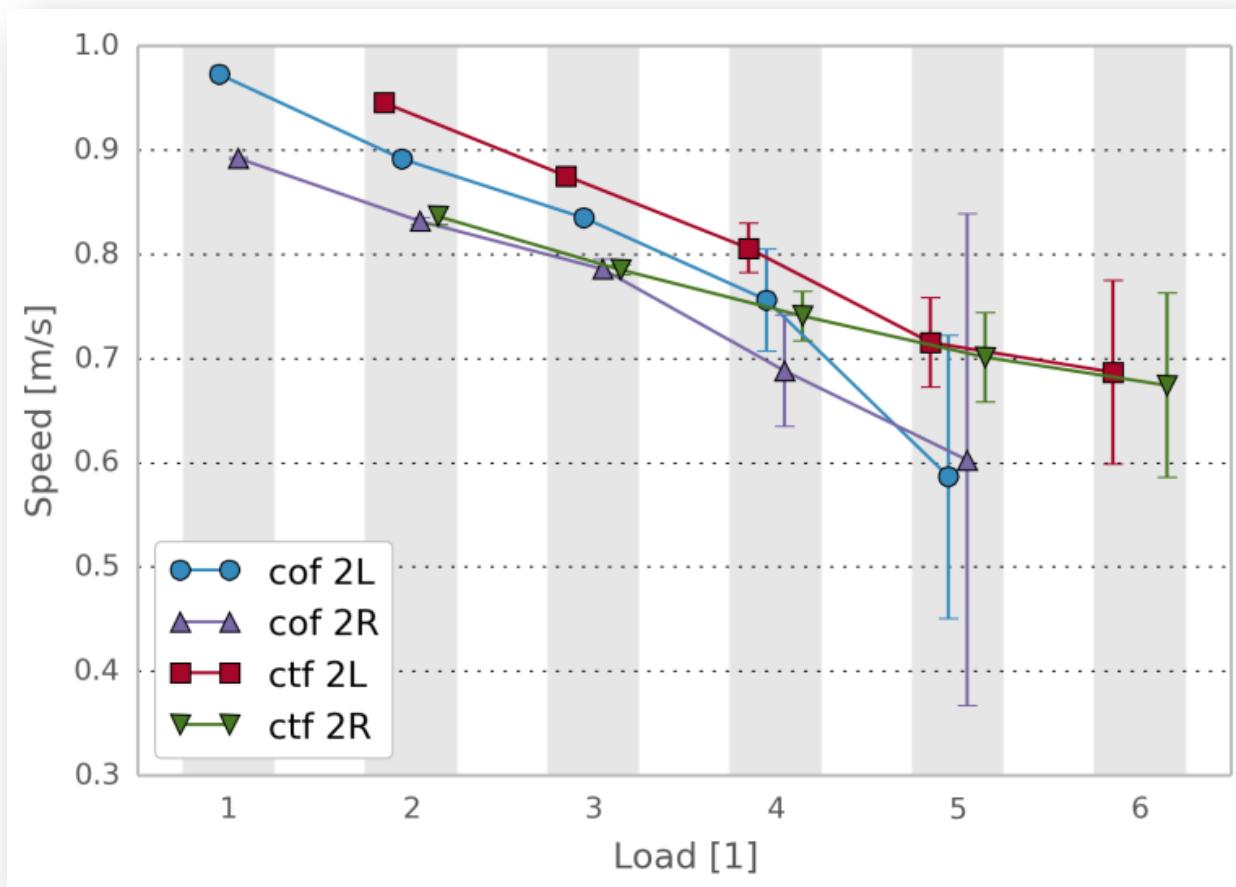
# Many flow conditions



Partitioning ensemble trajectories in flow classes  
=> statistics *per-class*

# Fundamental diagrams

Simple *per-class* statistics on velocities

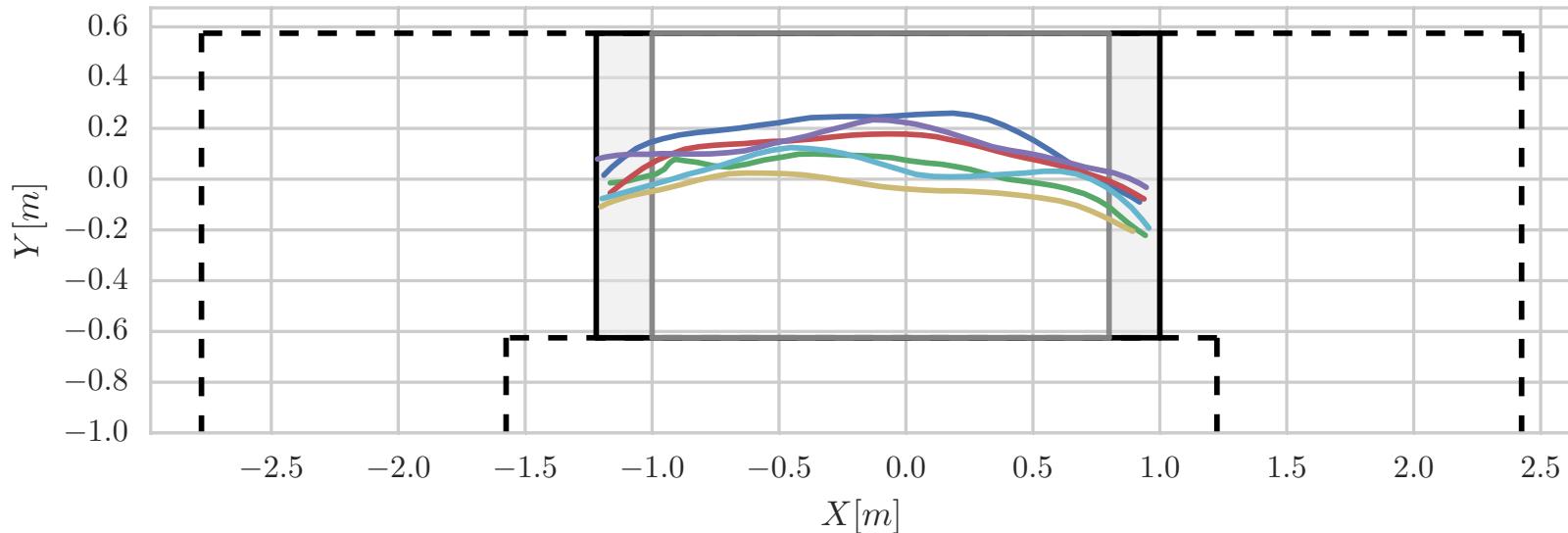


- L-R symmetry broken
- Descending direction faster
- Counter-flow > Co-flow (at same load)
  - Ped. ascending might have trays

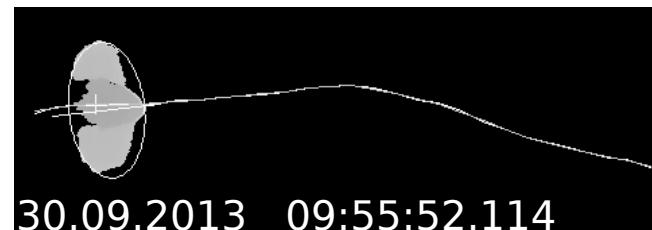
# Beyond average values...

- Full probability distribution functions
  - Analyze stochasticity
  - Mathematical models
- Now: **undisturbed pedestrians**

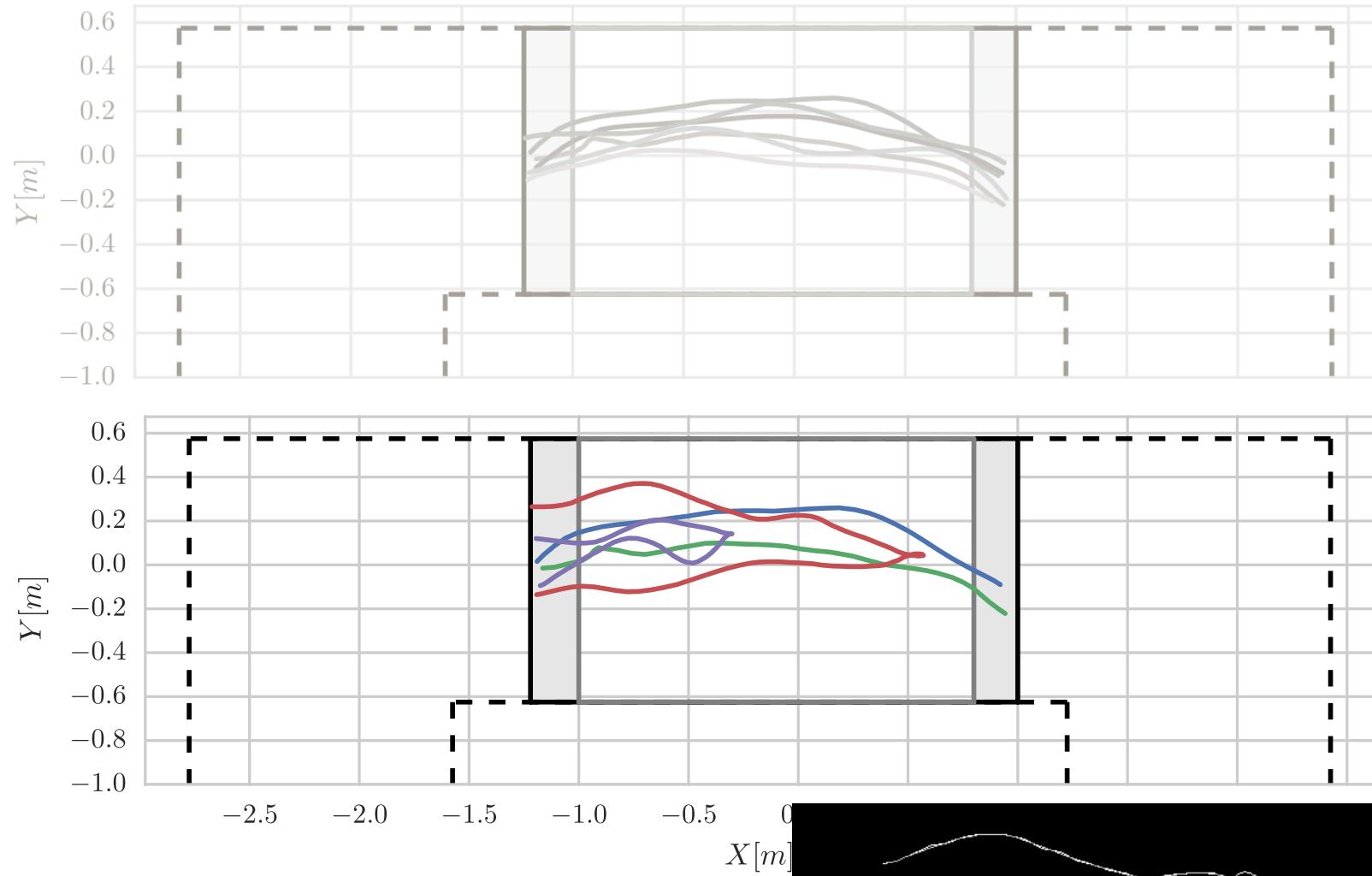
# Undisturbed pedestrian dynamics



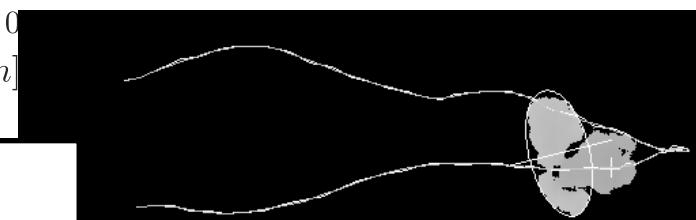
- Simple scenario
  - Pedestrians **cross** the corridor ( $L \rightarrow R$ )
  - No reasons to stop



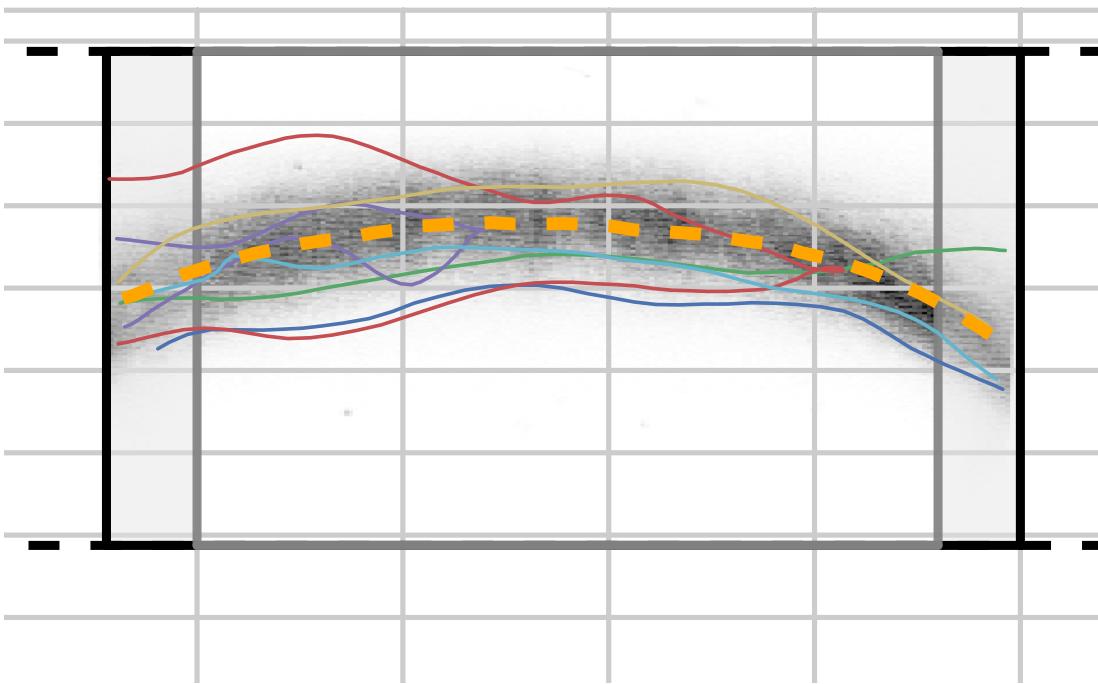
# Undisturbed pedestrian dynamics



- Rare events: trajectory inversions

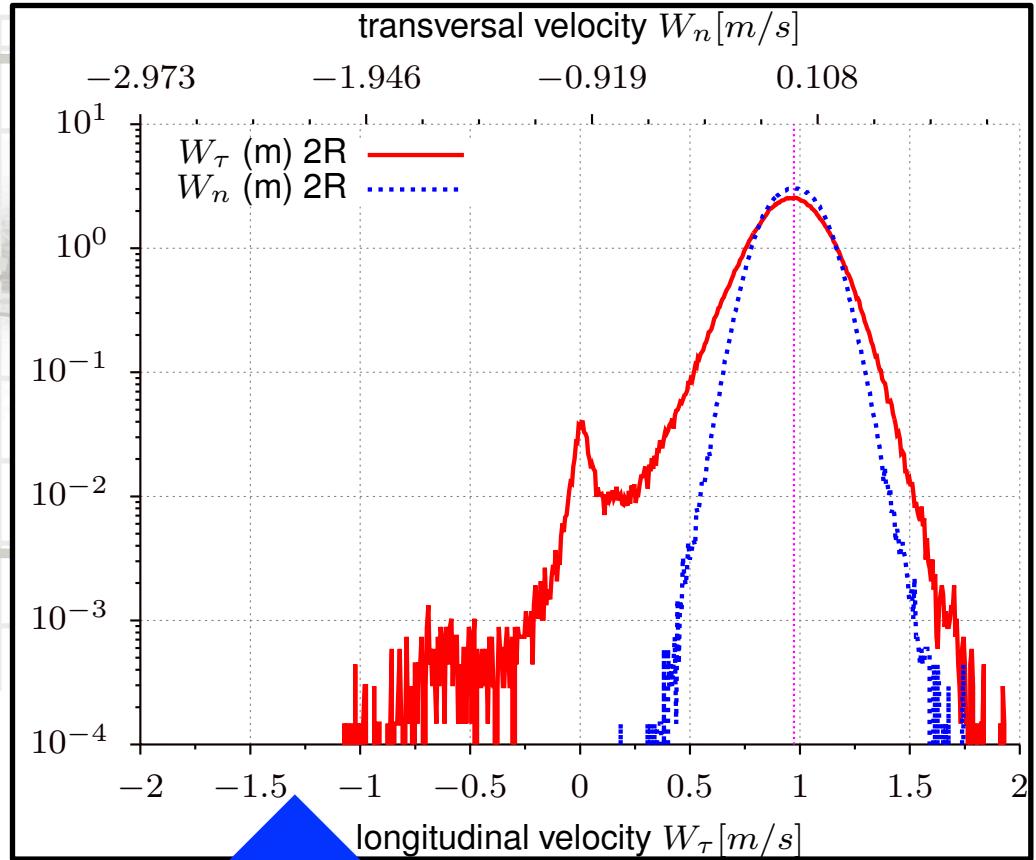
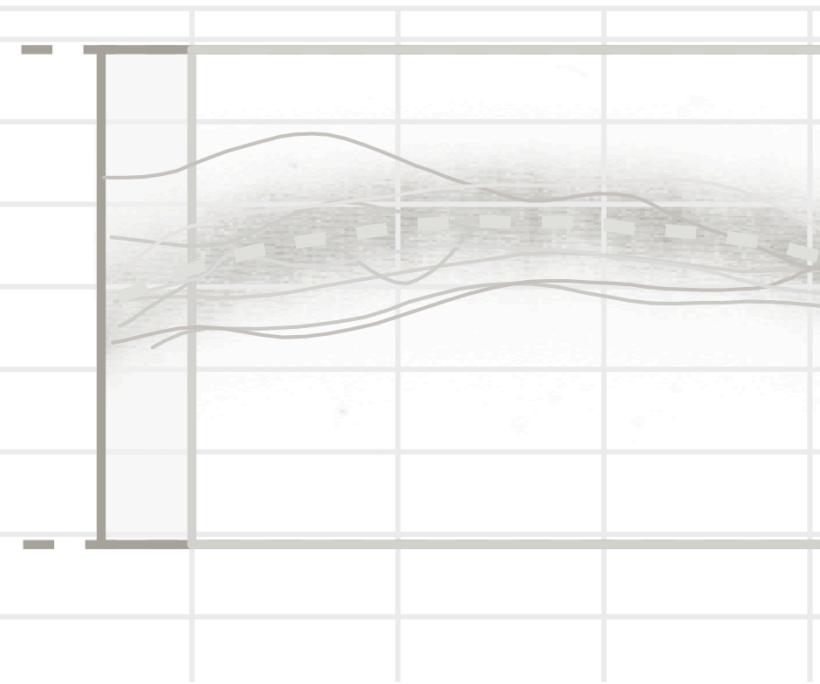


# High-statistics perspective



1. Preferred walking path
2. “Confined” transversal motion
3. longit. & transv. fluctuations

# High-statistics perspective



# Can we reproduce this behavior in statistical sense?

## Langevin-like equation

Second order stochastic dynamics:

$$\dot{\mathbf{x}} = \mathbf{v}$$

$$\dot{\mathbf{v}} = -\nabla_{\mathbf{v}} K(\mathbf{v}) - \nabla_{\mathbf{x}} V(\mathbf{x}) + \dot{\mathbf{W}}$$

Activity

(active friction for propulsion)

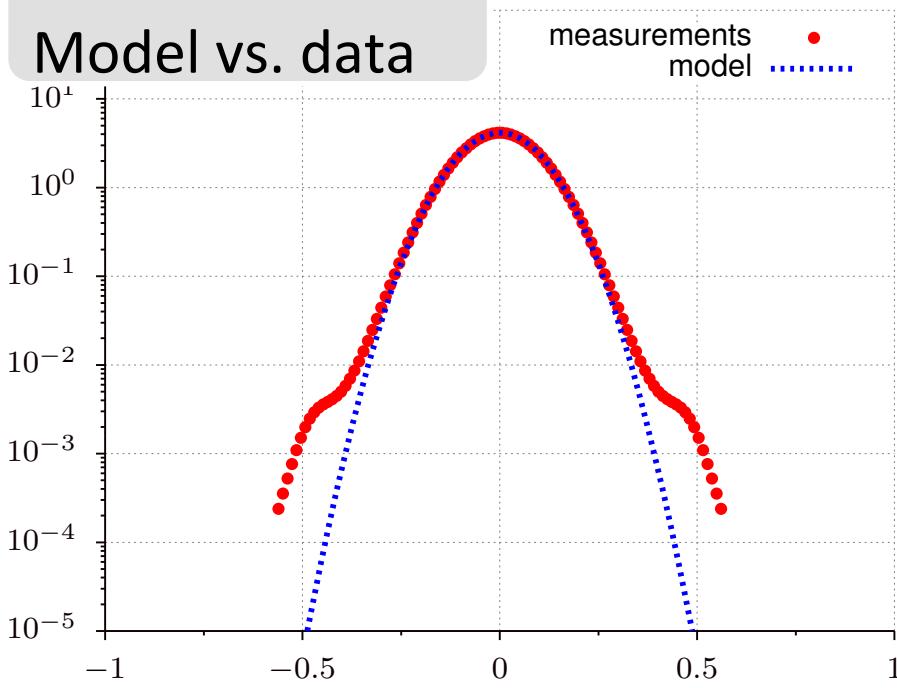
Spatial confinement

Random external factors

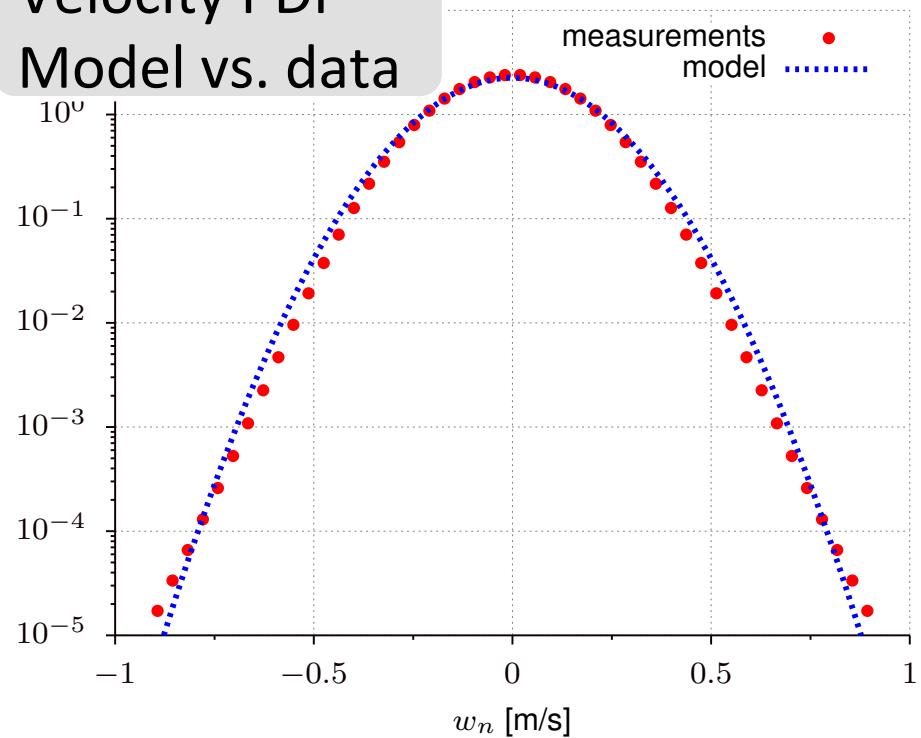
# Transversal fluctuations

Stochastic motion around preferred path:  
Quadratic potential for position (V) and velocity (K)

Position PDF  
Model vs. data



Velocity PDF  
Model vs. data



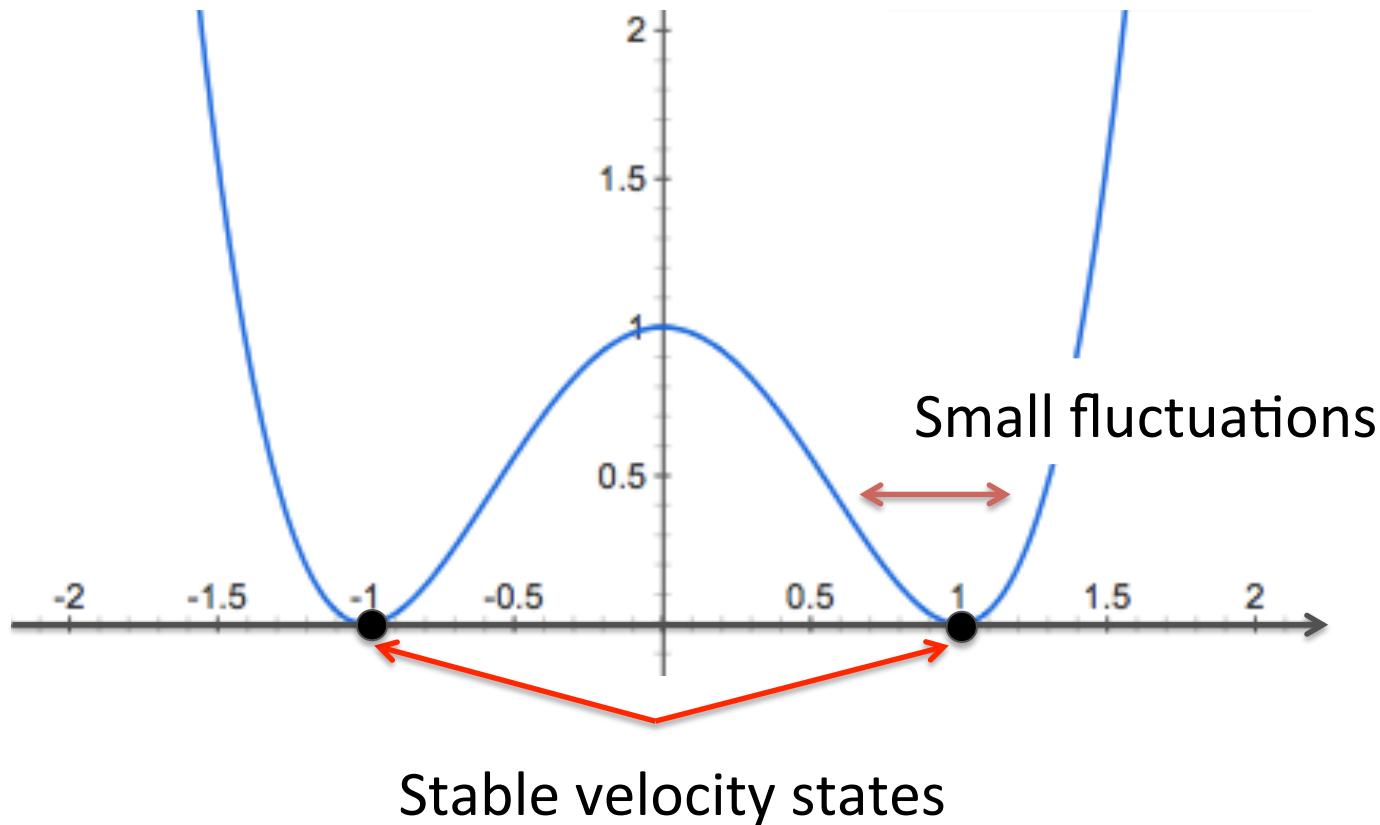
Confined Gaussian fluctuation:

$$\dot{v} = -2\gamma v - 2\beta y + \sigma_y \dot{w}$$

# Bi-stable longitudinal motion

4<sup>th</sup> order velocity potential velocity (K)

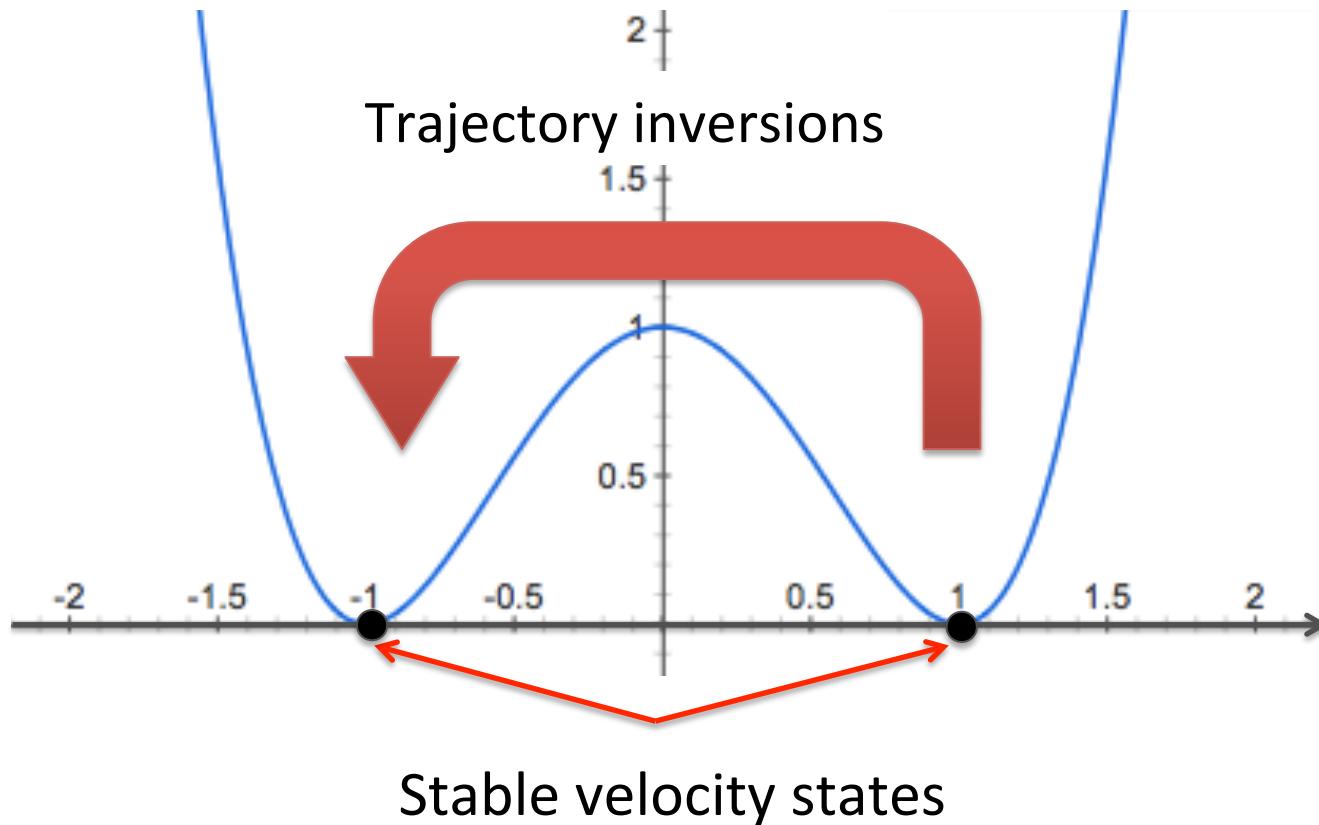
Simplest bi-stable stochastic velocity dynamics



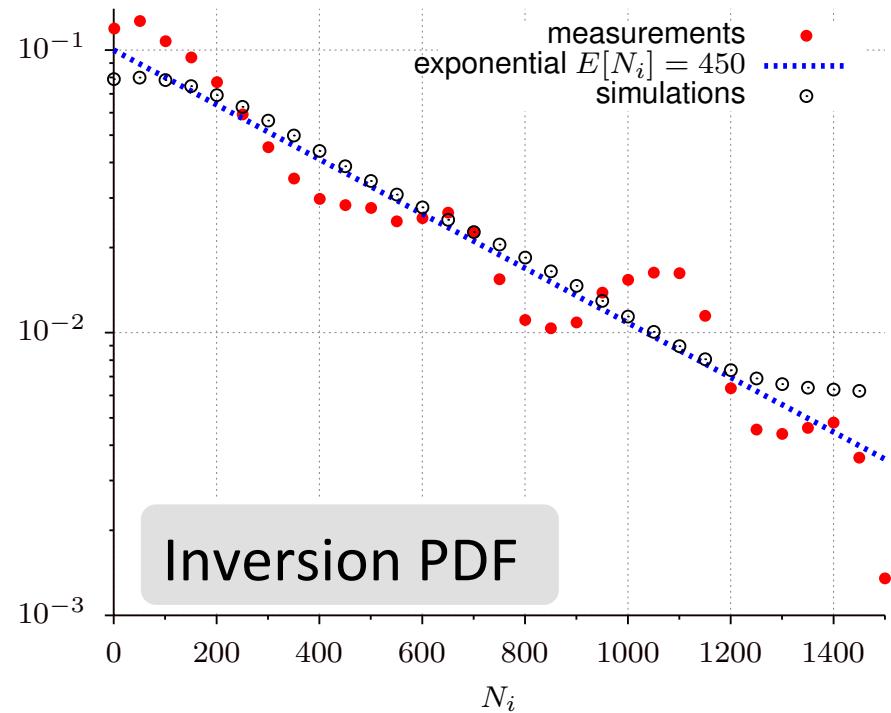
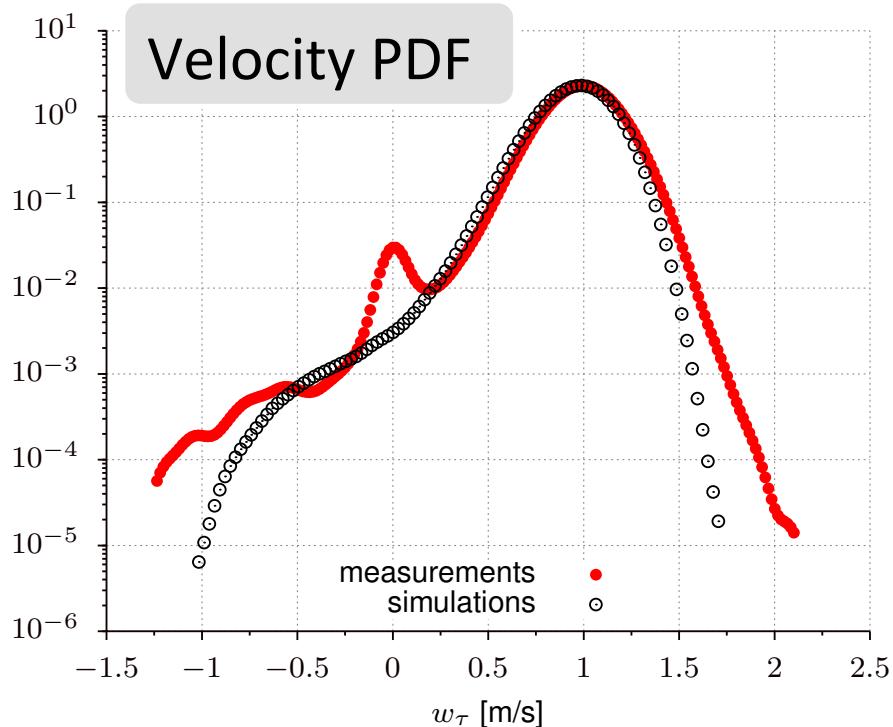
# Bi-stable longitudinal motion

4<sup>th</sup> order velocity potential velocity (K)

Simplest bi-stable stochastic velocity dynamics



# Bi-stable longitudinal motion



- Inversion dynamics captured in velocity pdf
- Rare and uncorrelated => **Poisson statistics**

$$\dot{u} = 4\alpha u(u^2 - u_p^2) + \sigma_x \dot{w}$$

[A. Corbetta *et. al.*, to be submitted]

# Conclusion

- Analyzed pedestrian dynamics via large experimental datasets
  - Statistic insights possible
  - Analogous features expected in low density crowds
- Simple Langevin-like model to reproduce stochastic features of undisturbed pedestrians motion
  - Quantitative
  - Small fluctuations and rare inversions captured within same model
- Next:
  - Avoidance dynamics in pairs & higher order interactions  
[A. Corbetta, Phd Thesis, 2015 – soon online]
  - Statisticity investigation at high density regimes?

# References

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