



DYNAMIC MODEL FOR ASSIGNMENT IN "SKY-CAR" TRANSIT SYSTEM – SPATIAL INTERACTIONS WITH OTHER COMMON TRANSPORT MODES

11th CONFERENCE ON *Traffic & Granular Flow*
OCTOBER 28, 2015

KWAMI S. SOSOE (*Institute for Technological Research (IRT) SystemX*)

JOINT AUTHORS : JEAN-PATRICK LEBACQUE & HABIB HAJ-SALEM (*IFSTTAR*)



Projet porté par

Labellisation principale

Labellisations secondaires

Soutien de collectivités territoriales

Campus Paris Saclay
FONDATION DE COOPERATION SCIENTIFIQUE

SYSTEMATIC
PARIS REGION SYSTEMS & ICT CLUSTER

advancity
Ville & Mobilité Durables

AS^{Tech}
Paris Region

mov'eo

île de France

Erfone
LE CONSEIL GÉNÉRAL

CAPS

- 01** BACKGROUND AND MOTIVATION
- 02** THE TRAFFIC MODEL
- 03** CONCLUSIONS & FUTUR WORK

01 BACKGROUND AND MOTIVATION

| Personal Rapid Transit

Transport and Mobility

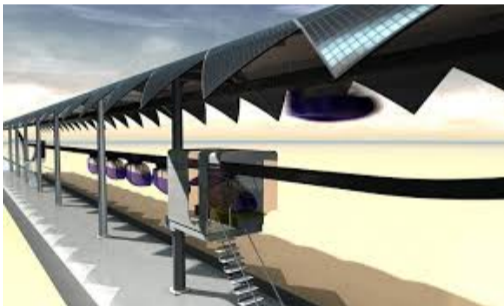
- ◆ Focus: Traffic modeling in Demand Responsive System equipped (DRS) with Personal rapid maglev travellers
- ◆ Traffic Demand optimization inside the DRS
- ◆ Reactive dynamical assignment - Stochasticity - Relocation
- ◆ Multimodality - Spatial interactions of the DRS with other common transport modes



1 - BACKGROUND AND MOTIVATION



New traffic game area - Personal maglev rapid travellers



DEFINITION:

Personal rapid transit (PRT), also called podcar, is a public transport mode featuring small automated vehicles operating on a network of specially built guideways.

PRT is a type of automated guideway transit (AGT), a class of system which also includes larger vehicles all the way to small subway systems.



02 THE TRAFFIC MODEL

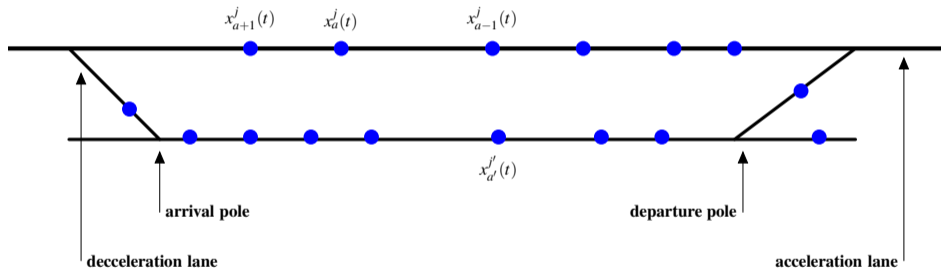
How do the sky-pods move ?

Intersection model

Demand optimization

Multimodality - Spatial interactions

Representation of portals, sky-lines



Motion of sky-pod in Lagrangian coordinates

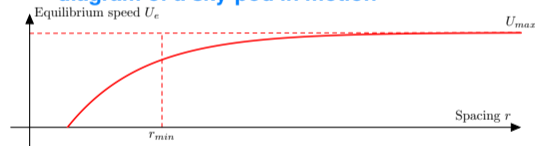
- a sky-pod label
 t time-step
 $x_a^j(t)$ position of sky-pod a at time t on the arc (j)
 $r_a^j(t)$ distance between the leader $a - 1$ and the follower a
 u_{p_a} velocity profile depending on its mission

$$\begin{cases} x_a^j(t+1) = x_a^j(t) + \delta t u_a^j(t) \\ u_a^j(t) = \min \left(U_e(r_a^j(t)), u_{p_a}(x_a^j(t)) \right) \end{cases}$$

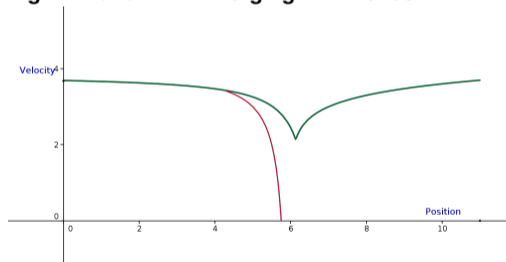
Choice of $U_e(r_a(t))$:

$$U_e(r) = U_{max} (1 - \exp(-r + \delta r))$$

Spacing-equilibrium speed fundamental diagram of a sky-pod in motion



Speed profile in Merging and Diverging zones



DECELERATION PROBLEM

$$Dist_{dec} = \frac{U_{max}^2}{2\gamma_{a-}}; \text{ (braking safety distance)}$$

$$u_a(t) = U_{max} - (t - t_0)\gamma_{a-}; \text{ (} t_0 \text{ the instant we decelerate)}$$

$$x_a(t) = x_0 + U_{max}(t - t_0) - \frac{(t - t_0)^2}{2}\gamma_{a-}$$

$$t_{dec} - t_0 = \frac{U_{max}}{\gamma_{a-}}$$

$W(t) \in \mathbb{R}_{Ns}^+$: the workload at time t in the system, *i.e.*
 $W_s(t)$ is the number of users at station s at time t .
 At time t , a user at station s requires service independently
 of the others with probability $\frac{1}{\sum_{s' \in \mathcal{V}_s} W_{s'}(t)}$. This user re-
 ceives service if he is the only user requiring service in \mathcal{V}_s
 at time t and when there is available offer at the station s or
 in its neighborhood.

Combined networks - Route and mode choices

Assumption:

Any pair OD pair could be joined with the below choices:

- ◆ **mode m_1** : use of road vehicle, then parking search availability to park and parking, and pedestrian walk for attending final destination, or
- ◆ **mode m_2** : use of sky-car and pedestrian walk, or
- ◆ **mode m_3** : use of modes m_1 and mode m_2 .

Logit-based rules

For $\forall k \in \{1, 2, 3\}$ (k being the index of the mode) and for $\forall w = (o, d)$,

$$\begin{aligned}\pi_{od}^k &= P[\text{choice} = m_k \mid (o, d) = w \in W] \\ &= \frac{\exp(-\theta C_{od}^{m_k})}{\sum_{p \in \{1, 2, 3\}, (o, d) = w \in W} \exp(-\theta C_{od}^{m_p})}\end{aligned}$$

The probability of choosing a mode m_k and a route w for an origin-destination pair (o, d) is given by the product of the probability of choosing the mode m_k and the probability of choosing the route w given the mode m_k .

$$P[\text{choice} = m_k \mid (o, d) = w \in W] = \frac{\exp(-\theta C_{od}^{m_k})}{\sum_{p \in \{1, 2, 3\}, (o, d) = w \in W} \exp(-\theta C_{od}^{m_p})}$$

The probability of choosing a route w given the mode m_k is given by the product of the probability of choosing the route w and the probability of choosing the mode m_k .

$$P[w \mid \text{choice} = m_k] = \frac{\exp(-\theta C_{od}^{m_k})}{\sum_{p \in \{1, 2, 3\}, (o, d) = w \in W} \exp(-\theta C_{od}^{m_p})}$$

Combined networks - Route and mode choices

Assumption:

Any pair OD pair could be joined with the below choices:

- ◆ **mode m_1** : use of road vehicle, then parking search availability to park and parking, and pedestrian walk for attending final destination, or
- ◆ **mode m_2** : use of sky-car and pedestrian walk, or
- ◆ **mode m_3** : use of modes m_1 and mode m_2 .

Logit-based rules

For $\forall k \in \{1, 2, 3\}$ (k being the index of the mode) and for $\forall w = (o, d)$,

$$\begin{aligned}\pi_{od}^k &= P[\text{choice} = m_k \mid (o, d) = w \in W] \\ &= \frac{\exp(-\theta C_{od}^{m_k})}{\sum_{p \in \{1, 2, 3\}, (o, d) = w \in W} \exp(-\theta C_{od}^{m_p})}\end{aligned}$$

The probability of choosing a mode well verifies:

$$\left\{ \begin{array}{l} 0 \leq P[\text{choice} = m_k \mid (o, d) = w \in W] \leq 1, \\ \quad \forall k = 1, 2, 3, \forall w = (o, d) \in W, \\ \sum_{k=1}^3 P[\text{choice} = m_k] = 1. \end{array} \right.$$

Combined networks - Route and mode choices

Assumption:

Any pair OD pair could be joined with the below choices:

- ◆ **mode m_1** : use of road vehicle, then parking search availability to park and parking, and pedestrian walk for attending final destination, or
- ◆ **mode m_2** : use of sky-car and pedestrian walk, or
- ◆ **mode m_3** : use of modes m_1 and mode m_2 .

Logit-based rules

For $\forall k \in \{1, 2, 3\}$ (k being the index of the mode) and for $\forall w = (o, d)$,

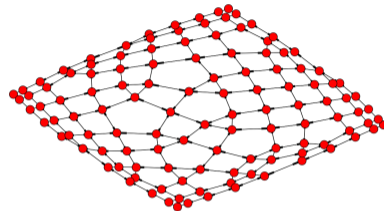
$$\begin{aligned}\pi_{od}^k &= P[\text{choice} = m_k \mid (o, d) = w \in W] \\ &= \frac{\exp(-\theta C_{od}^{m_k})}{\sum_{p \in \{1, 2, 3\}, (o, d) = w \in W} \exp(-\theta C_{od}^{m_p})}\end{aligned}$$

The probability of choosing a mode well verifies:

$$\left\{ \begin{array}{l} 0 \leq P[\text{choice} = m_k \mid (o, d) = w \in W] \leq 1, \\ \quad \forall k = 1, 2, 3, \forall w = (o, d) \in W, \\ \sum_{k=1}^3 P[\text{choice} = m_k] = 1. \end{array} \right.$$

03 CONCLUSIONS & FUTUR WORK

- ◆ Lagrangian model for Sky-pods in motion
- ◆ We provide intersection model for autonomous Demand-responsive system of personal maglev rapid travellers
- ◆ Demand optimization due to a Random Multiple Access Protocol with Spatial Interactions.
- ◆ **Challenges:**
 - ◆ Method to reduce computational tasks in Large-scale Autonomous Demand responsive system of Personal maglev rapid travellers.
 - ◆ Traffic simulation.
 - ◆ Stability analysis of the Random Multiple Access Protocol with Spatial Interactions.



Some references



Bordenave, C.; Foss, S. and d Shneer, V., 2006. *A Random Multiple Access Protocol with Spatial Interactions*. RR-5975 inria-00090762v2, 2006.



Luca Quadrifoglio, Maged M. Dessouky, Fernando Ordóñez. 2008. *A simulation study of demand responsive transit system design*. Transportation Research Part A 42 (2008) 718–737.



M.E. Bruni, F. Guerriero, P. Beraldi. 2014. *Designing robust routes for demand-responsive transport*. Transportation Research Part E 70 (2014) 1–16.



Bilge Atasoy, Takuro Ikeda, Moshe E. Ben-Akiva. *The Concept and Impact Analysis of a Flexible Mobility on Demand System*.



Philip Kilby, Matt Robards, 2013. *Simulation Of an Innovative Public Transport System*. 20th International Congress on Modelling and Simulation, Adelaide, Australia, 1–6 December 2013.



Hoogendoorn, S. and Bovy, P., 2004. *Pedestrian route-choice and activity scheduling theory and models*. Transportation Research Part B: Methodological, 2004, 38, 169-190.



Khoshyaran, M. and Lebacque, J.P., 2011. *URBASIMCE: A dynamic model for assignment and cold start emission*. Procedia Social and Behavioral Science, 2011, 20, 714-722.

THANKS FOR YOUR ATTENTION

QUESTIONS ?

`kwami.sossoe@irt-systemx.fr`



DYNAMIC MODEL FOR ASSIGNMENT IN "SKY-CAR" TRANSIT SYSTEM – SPATIAL INTERACTIONS WITH OTHER COMMON TRANSPORT MODES

11th CONFERENCE ON *Traffic & Granular Flow*
OCTOBER 28, 2015

KWAMI S. SOSOE (*Institute for Technological Research (IRT) SystemX*)

JOINT AUTHORS : JEAN-PATRICK LEBACQUE & HABIB HAJ-SALEM (*IFSTTAR*)



Projet porté par

Labellisation principale

Labellisations secondaires

Soutien de collectivités territoriales

Campus Paris Saclay
FONDATION DE COOPERATION SCIENTIFIQUE

SYSTEMATIC
PARIS REGION SYSTEMS & ICT CLUSTER

advancity
Ville & Mobilité Durables

AS^{Tech}
Paris Region

mov'eo

île de France

Erfone
LE CONSEIL GÉNÉRAL

CAPS