

Steady State of Pedestrian Flow in Bottleneck Experiments

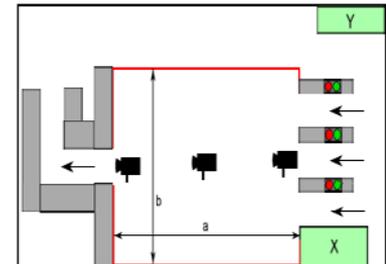
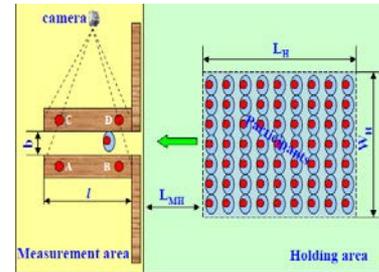
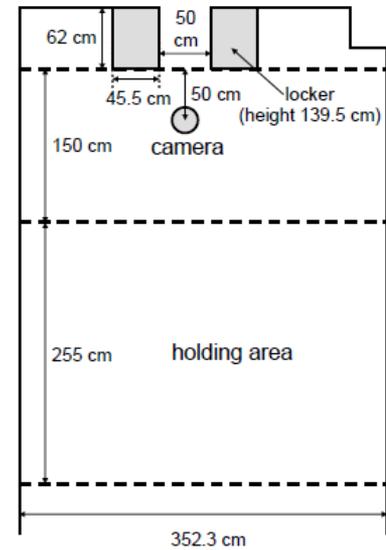
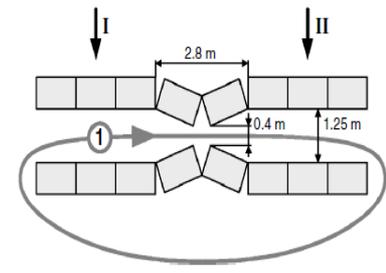
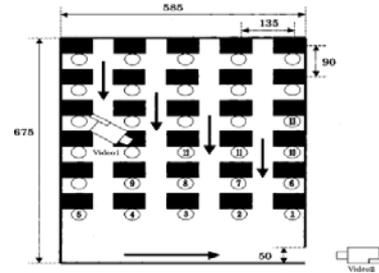
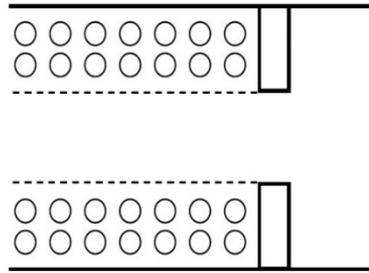
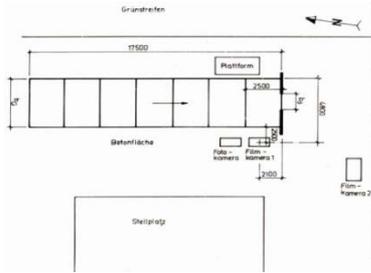
28. Oktober 2015 | Weichen Liao

Jülich Supercomputing Centre

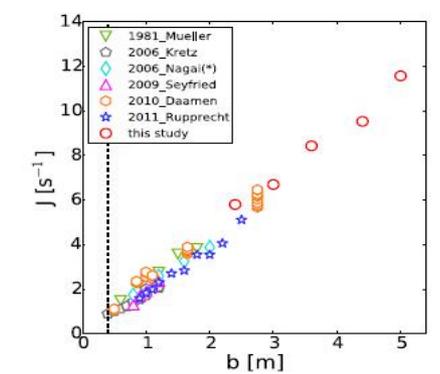
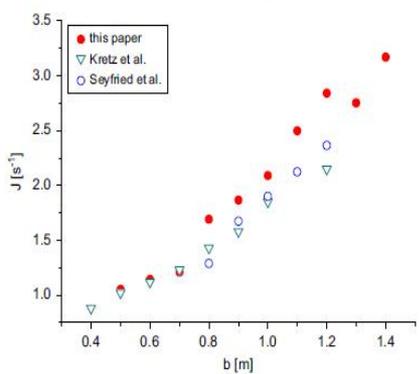
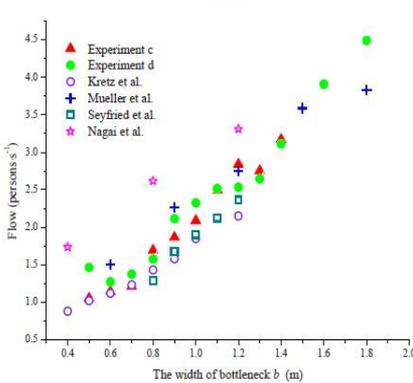
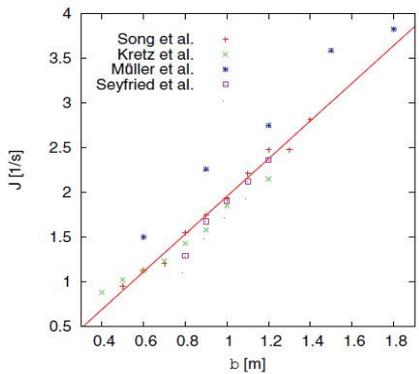
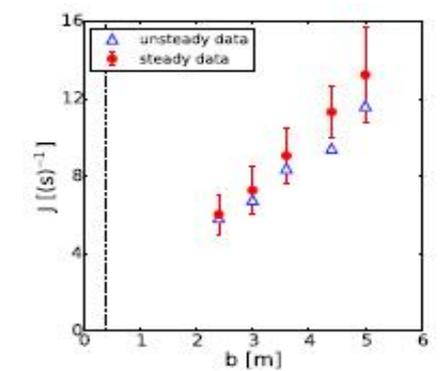
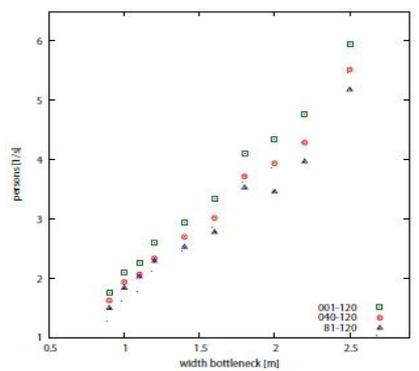
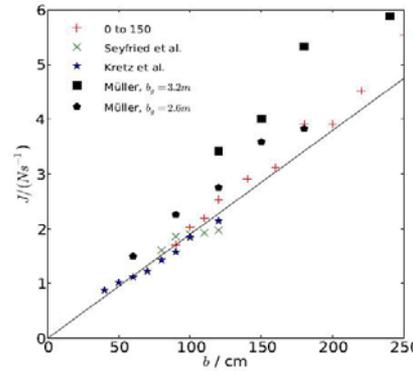
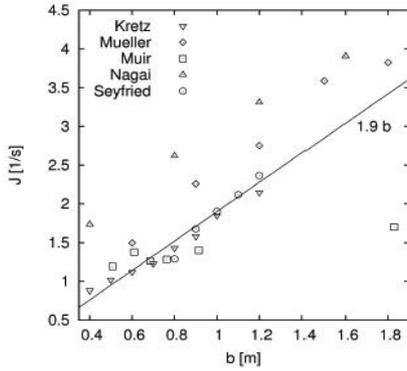
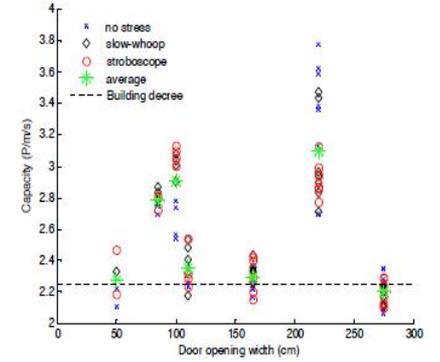
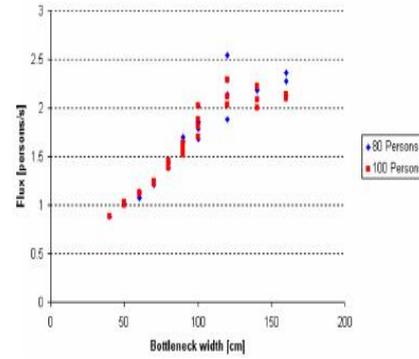
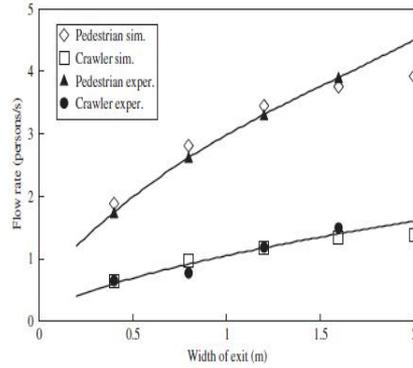
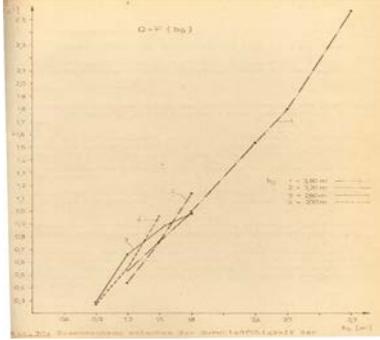
Overview

- **Background**
- **Detection of steady state**
- **Pedestrian flow in bottleneck experiments**
- **Conclusions and outlook**

Background

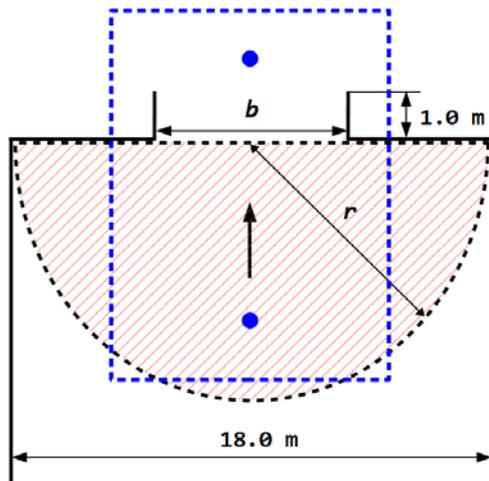


Background



Background

Experiment AO



$$l = 1.0 \text{ m}$$

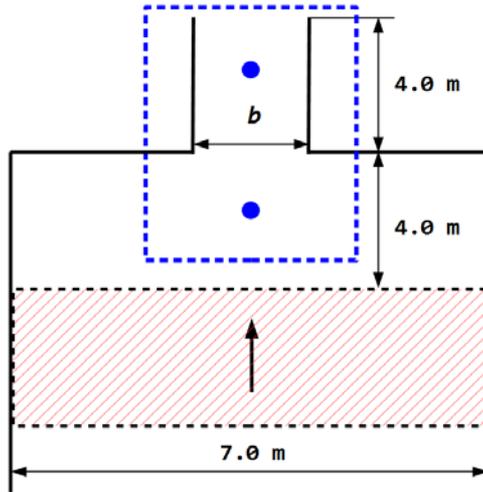
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$$d = 0 \text{ m}$$

$$\rho_{\text{ini}} = 3.0 \text{ m}^{-2}$$

$$N = 350 \text{ pers}$$

Experiment EG



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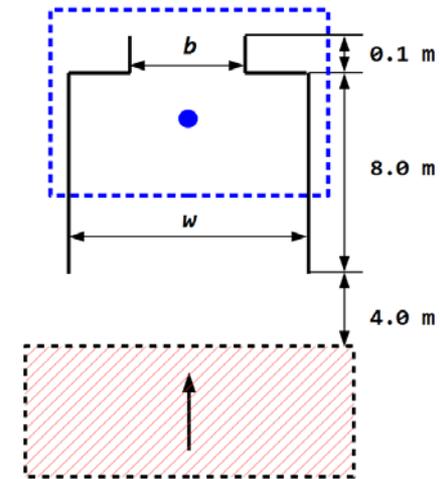
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Experiment UO



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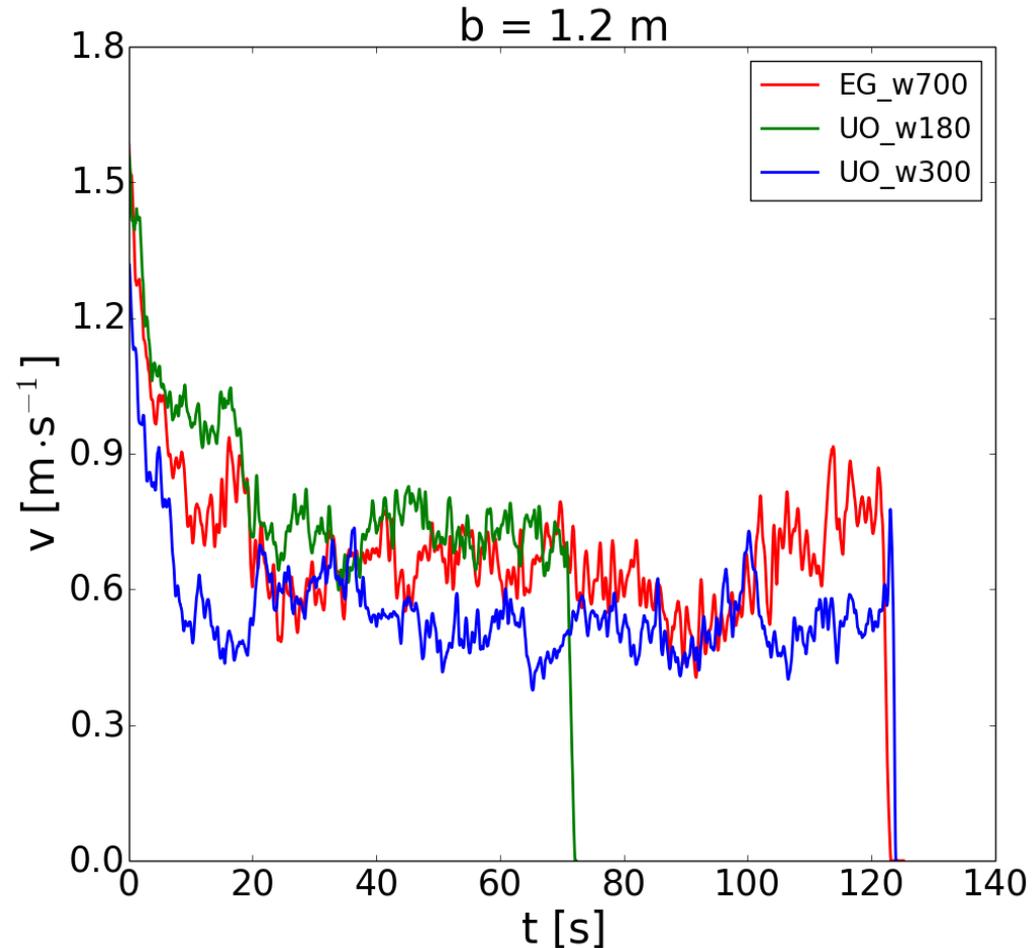
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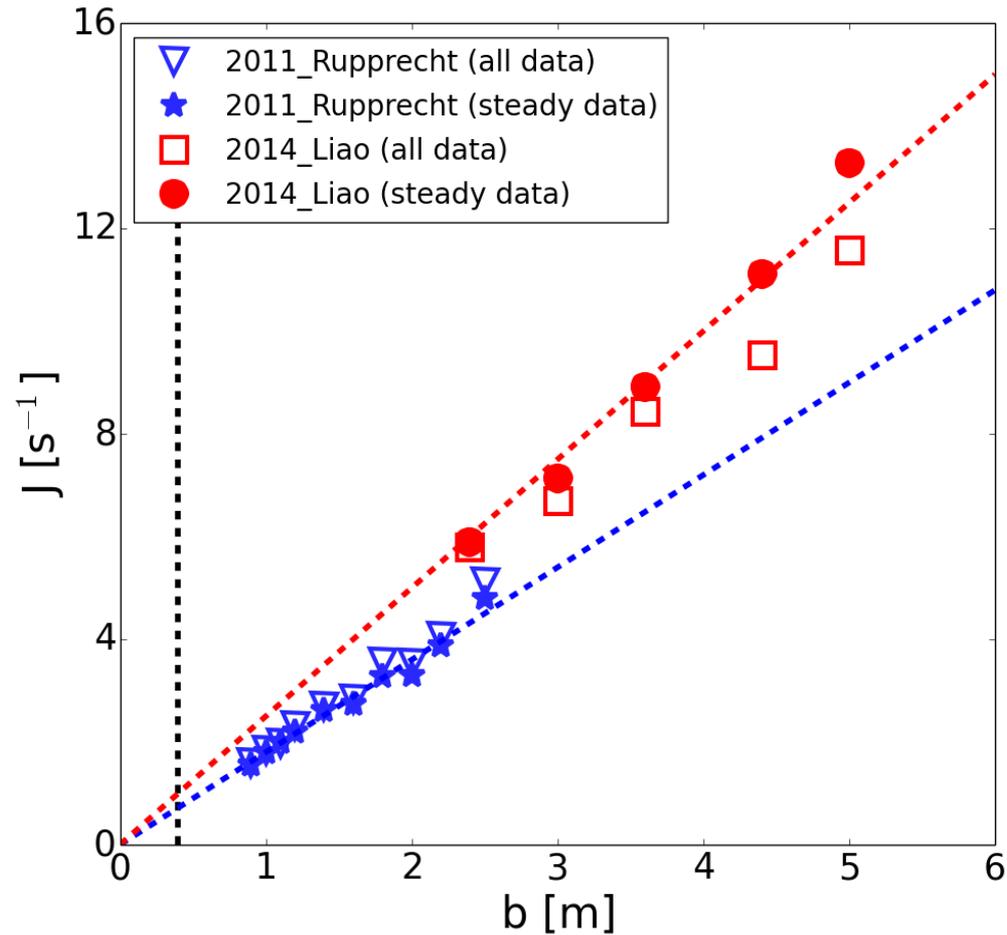
$$N = 150, 250, 400 \text{ pers}$$

Background



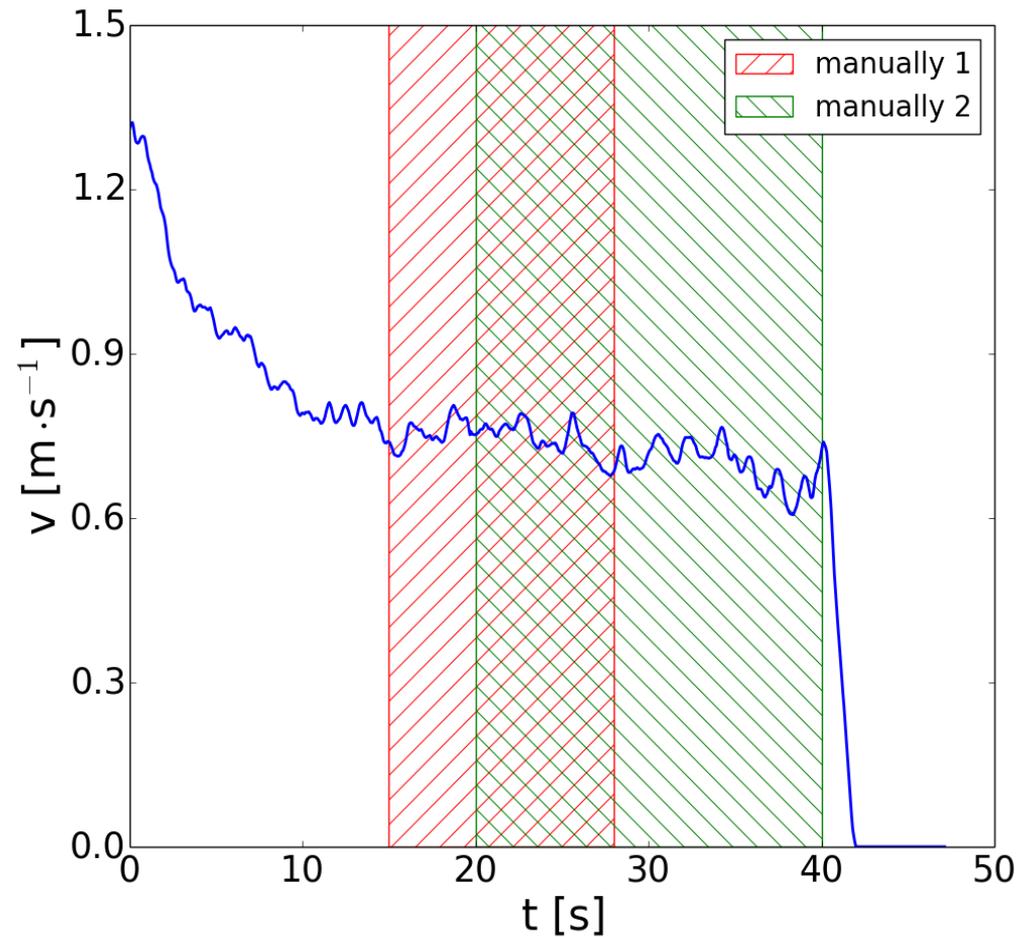
Steady state: mean, standard deviation and autocorrelation are constants

Background



W. Liao et al., PED 2014, 2: 26-33 (2014)

Background



How to detect steady state reproducibly?

Detection of Steady State - Variables

- **Classic definition of flow: $J = N/T = 1/\overline{\Delta t_i}$ (1)**

Microscopic measurements of flow could lead to strong fluctuations.

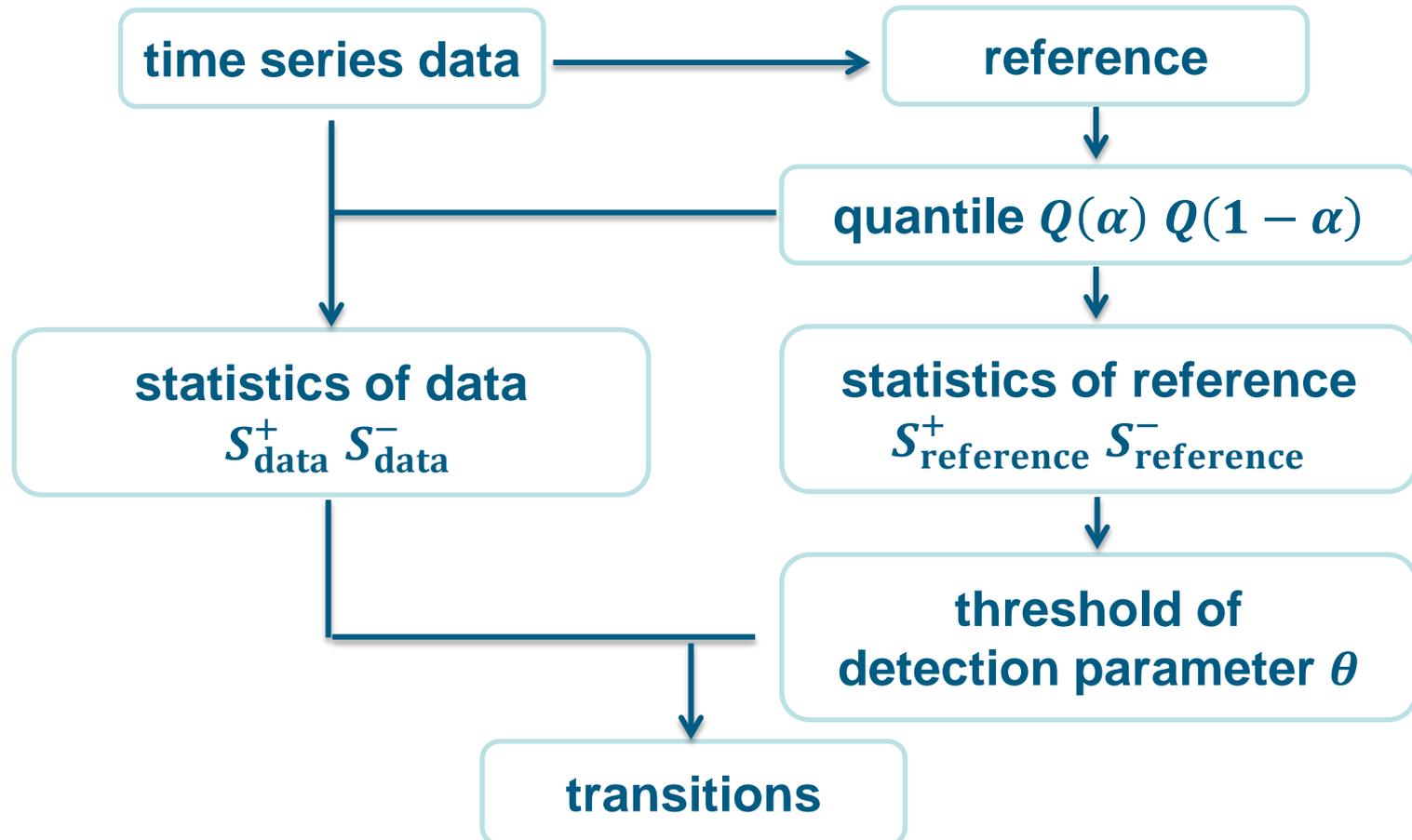
- **Flow equation from fluid dynamics: $J = \rho \cdot v \cdot W$ (2)**

The steady state of both density and speed is the steady state of flow.

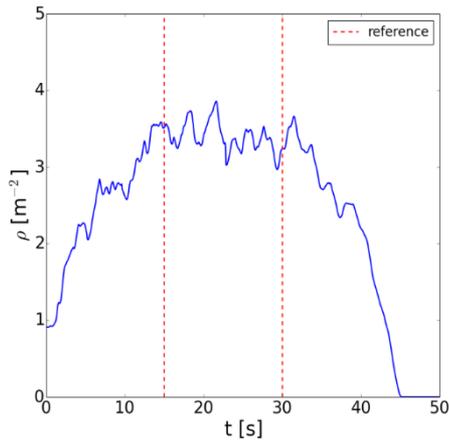
Detection of Steady State - CUSUM

CUSUM (Cumulative Sum Control Chart)

E. S. Page, Biometrika, 41(1/2): 100-115 (1954)



Detection of Steady State - CUSUM

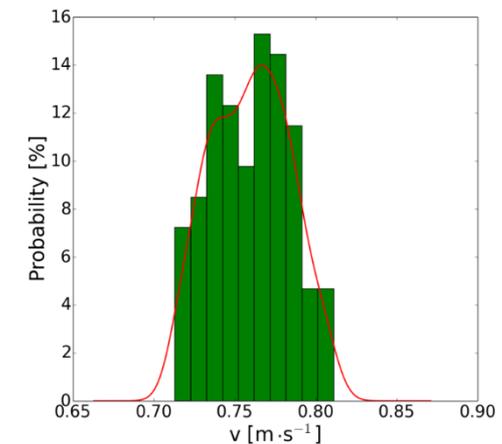
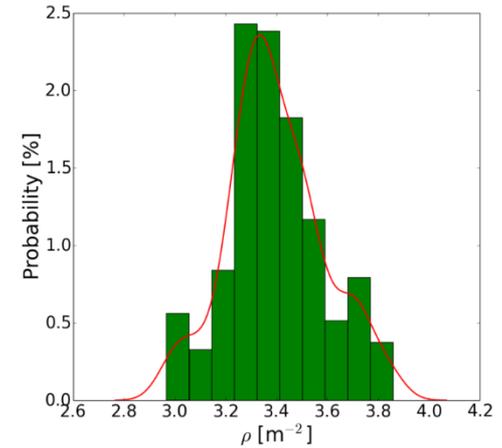
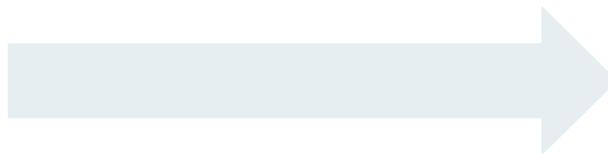
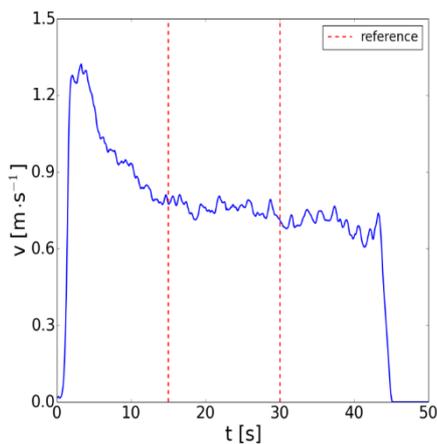


Reference:

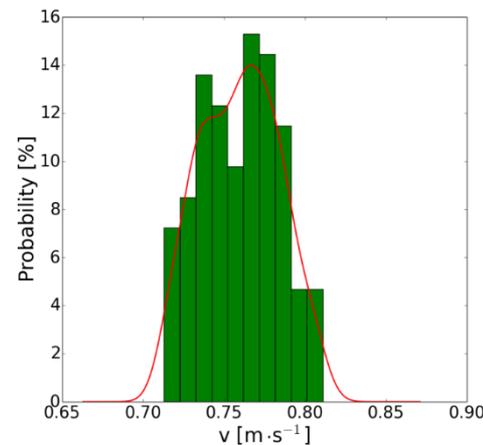
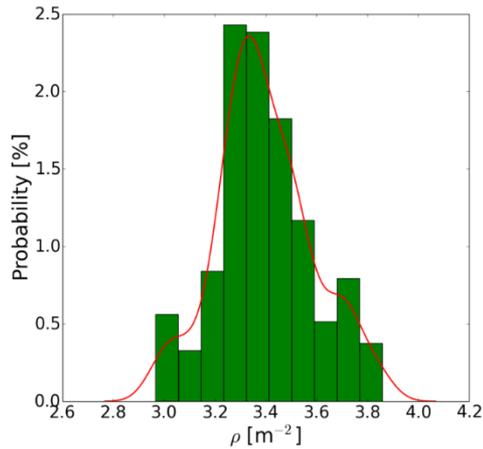
- Observations

Quantile $Q(\alpha)$ and $Q(1 - \alpha)$:

- Histogram distribution
- Kernel estimation



Detection of Steady State - CUSUM

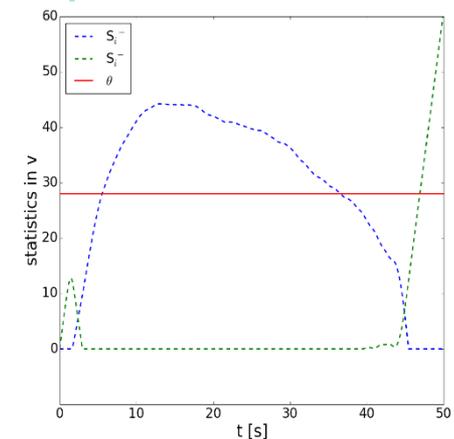
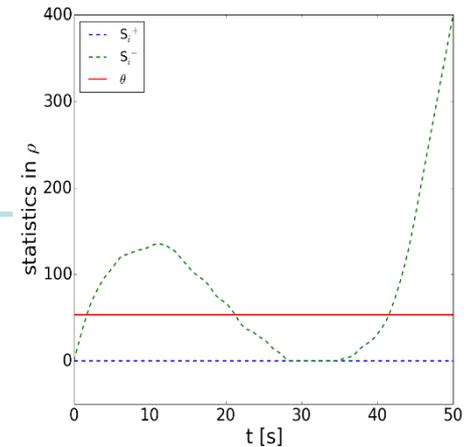


Statistics S_i^+ and S_i^- :

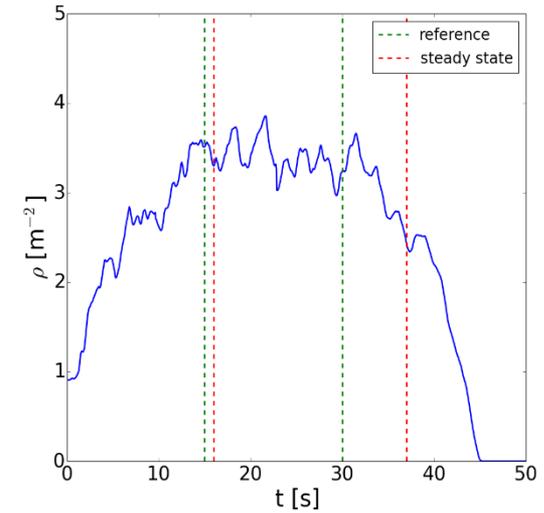
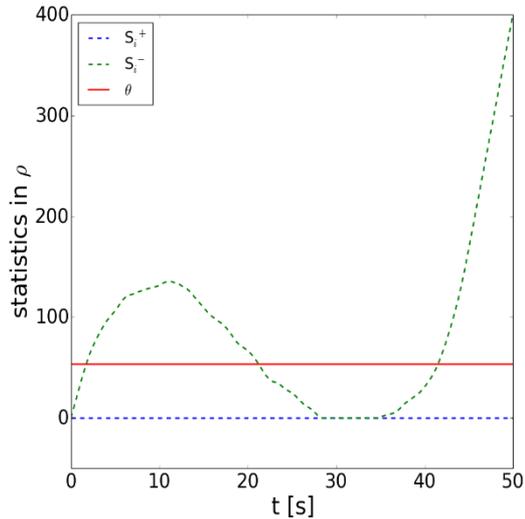
- $S_0^+ = S_0^- = 0$
- $S_i^+ = \max\{0, S_{i-1}^+ + x_i - Q(\alpha)\}$
- $S_i^- = \max\{0, S_{i-1}^- + Q(1 - \alpha) - x_i\}$

Criteria θ :

- Quantile of $S_{\text{reference}}$



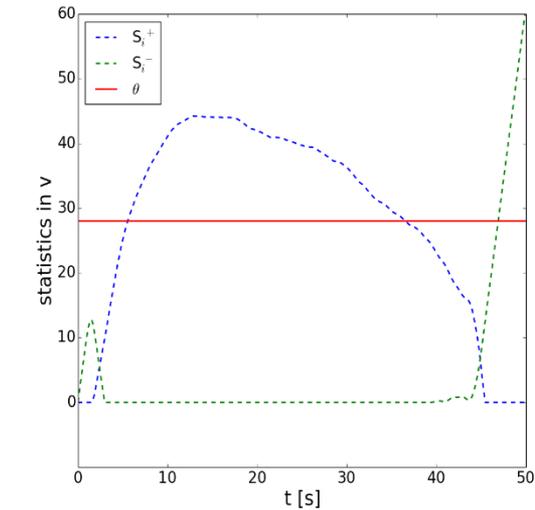
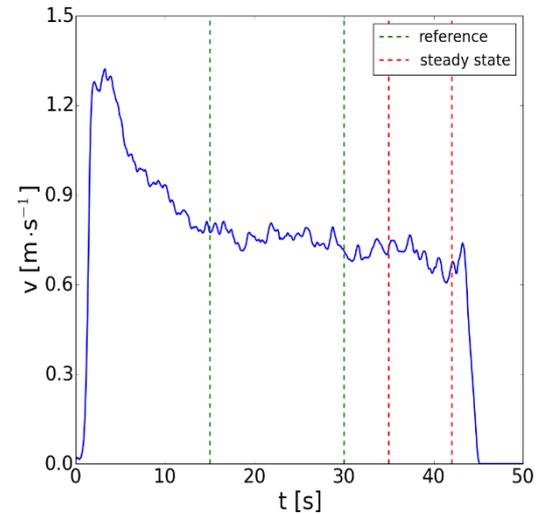
Detection of Steady State - CUSUM



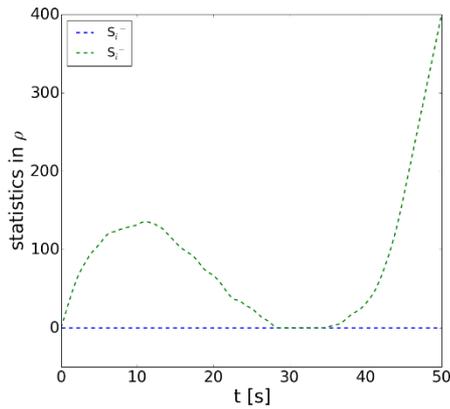
Reaction time:

- $t_{\text{reaching}} = \frac{s' - \theta}{f}$

- $t_{\text{leaving}} = \frac{\theta}{f}$

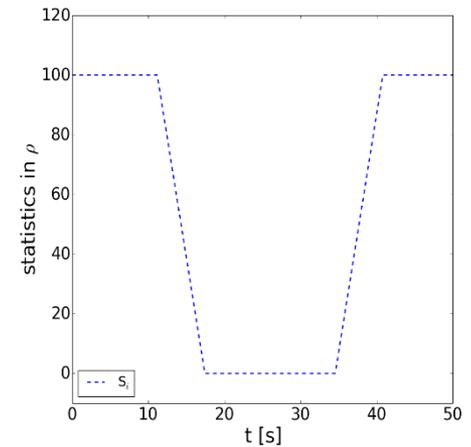


Detection of Steady State - CUSUM



Problems about statistics:

- Not sensitive
- No boundary
- Redundant

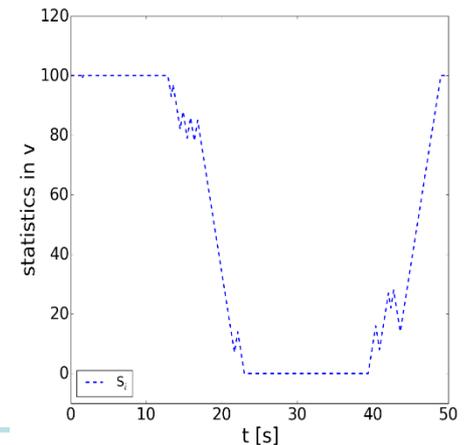
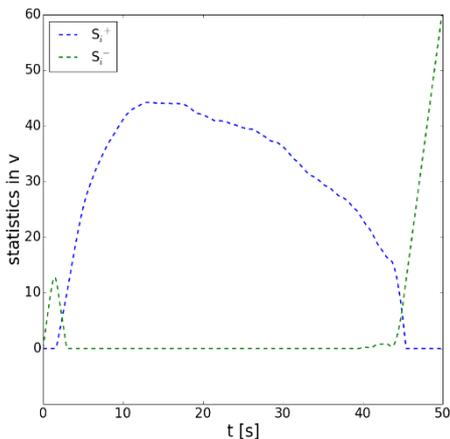


Improvement:

- $$F(\tilde{x}_i) = \begin{cases} 1 & \text{if } |\tilde{x}_i| > q(\alpha) \\ -1 & \text{if } |\tilde{x}_i| \leq q(\alpha) \end{cases}$$

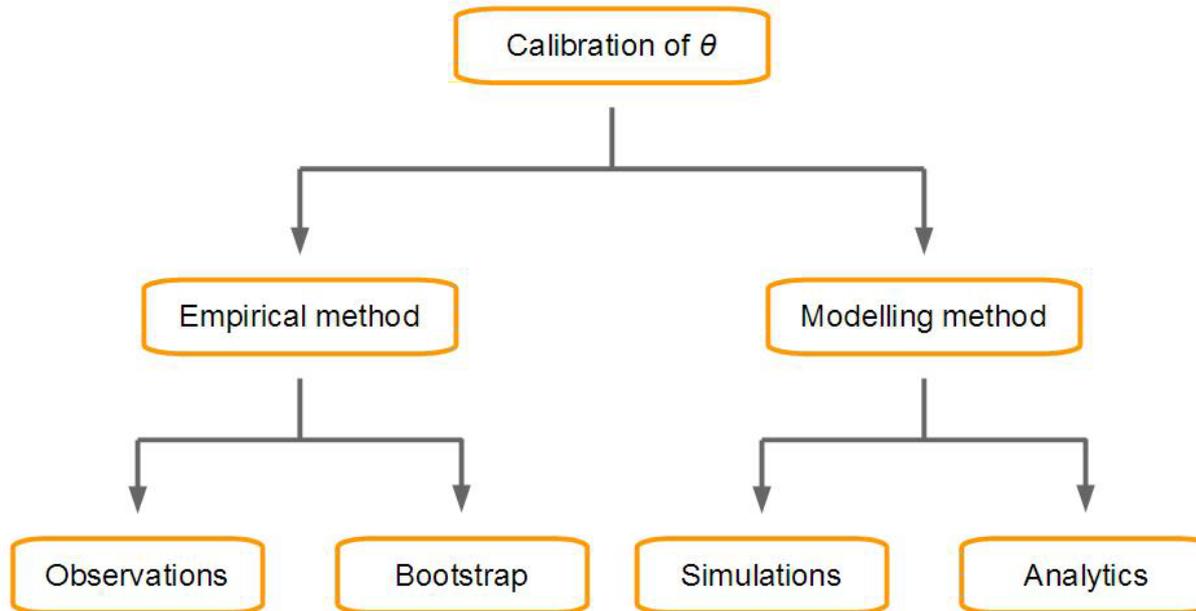
where $\tilde{x}_i = (x_i - \mu) / \sigma$

- $S_{\max} = 100$
- $S_0 = S_{\max}$
- $$S_i = \min\{\max\{0, S_{i-1} + F(\tilde{x}_i)\}, S_{\max}\}$$



Detection of Steady State - CUSUM

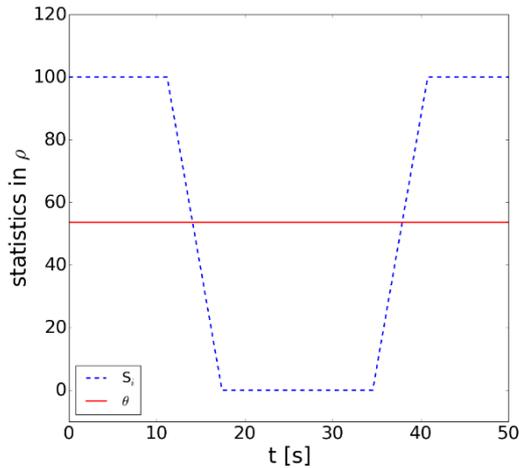
Calibrating the threshold of detection parameter θ



Autoregressive Model:

- $y_0 = 0$
- $y_i = c \cdot y_{i-1} + \sqrt{1 - c^2} \cdot \varepsilon_i$

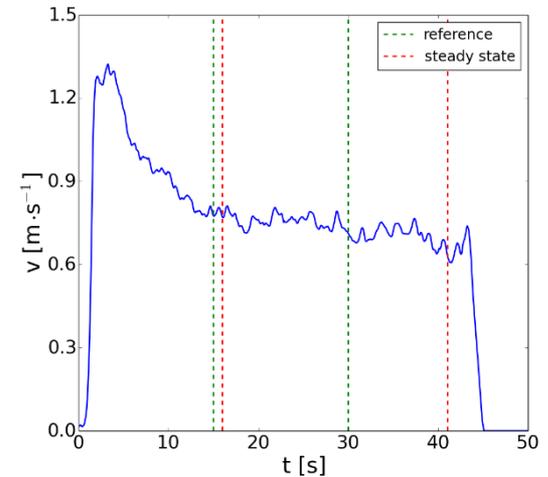
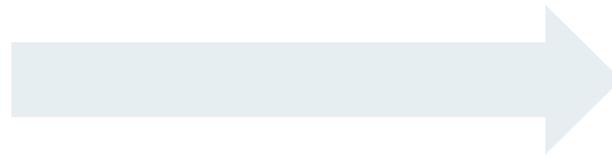
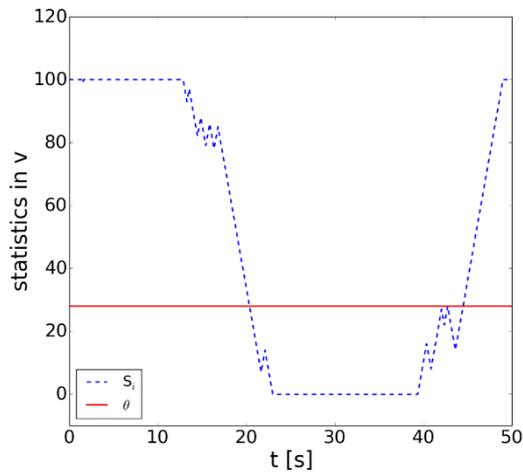
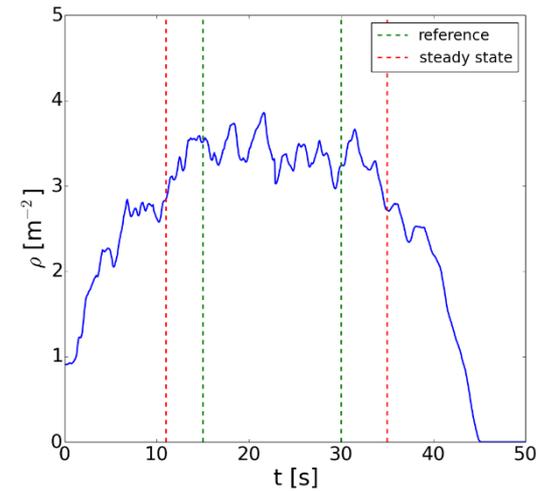
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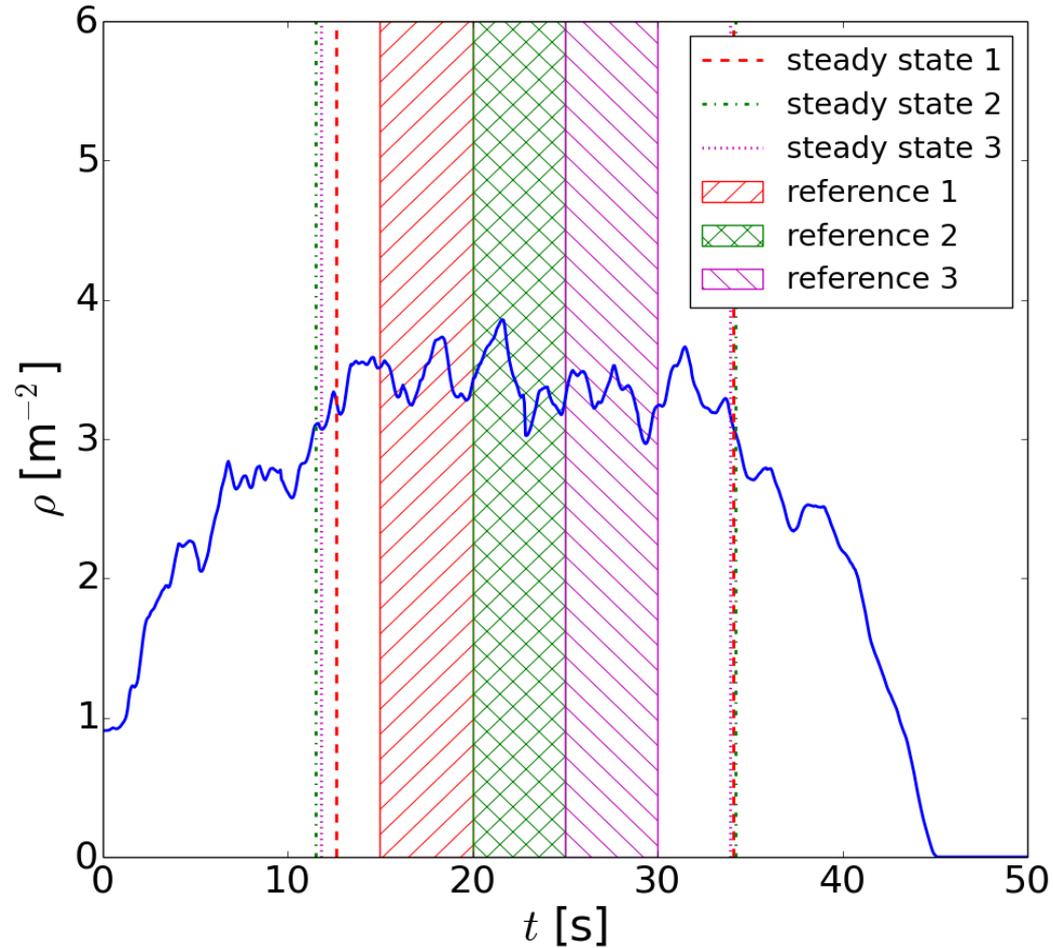
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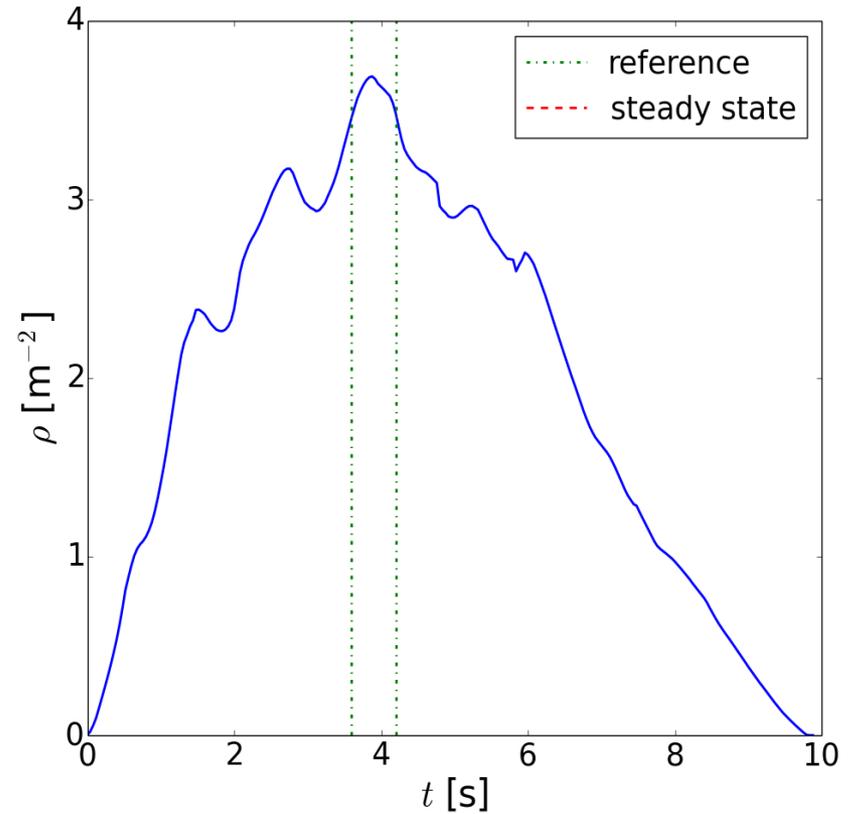
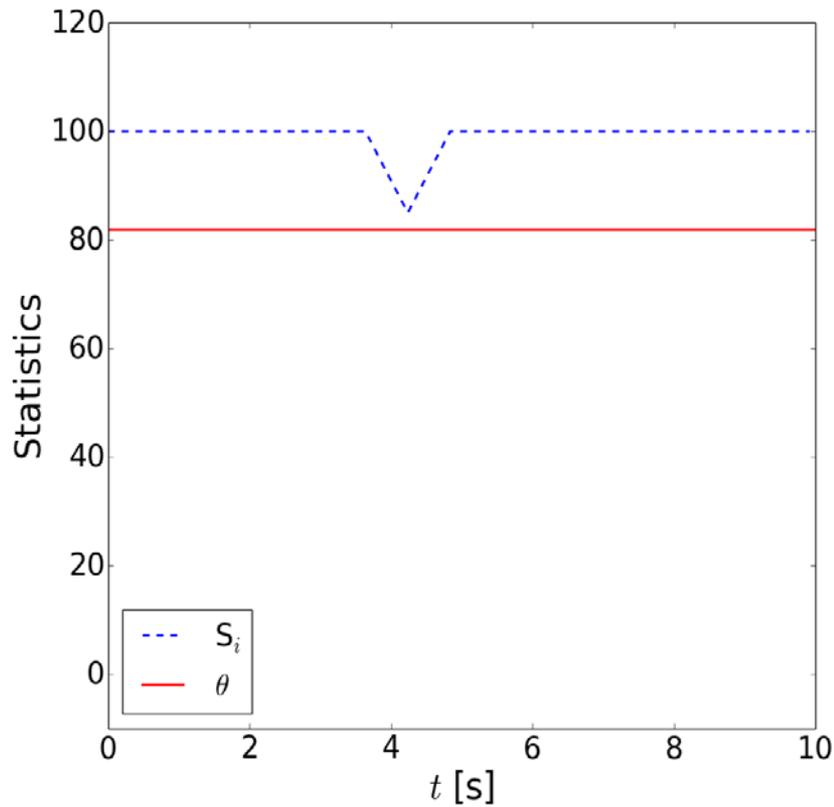


Detection of Steady State - Robustness



Reproducible steady state

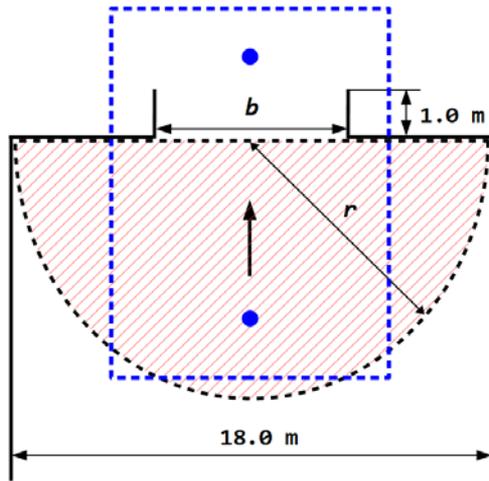
Detection of Steady State - Robustness



No steady state

Pedestrian Flow in Bottleneck Experiments

Experiment AO



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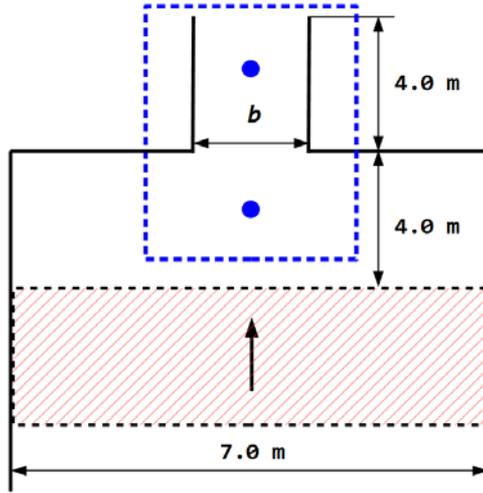
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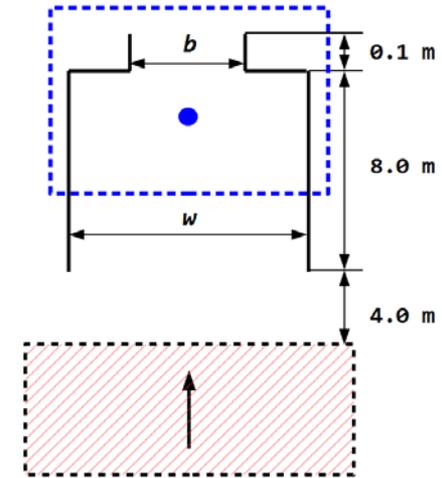
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Experiment UO



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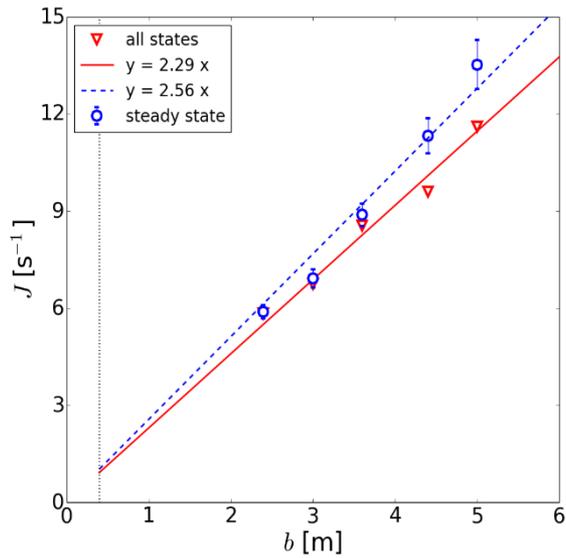
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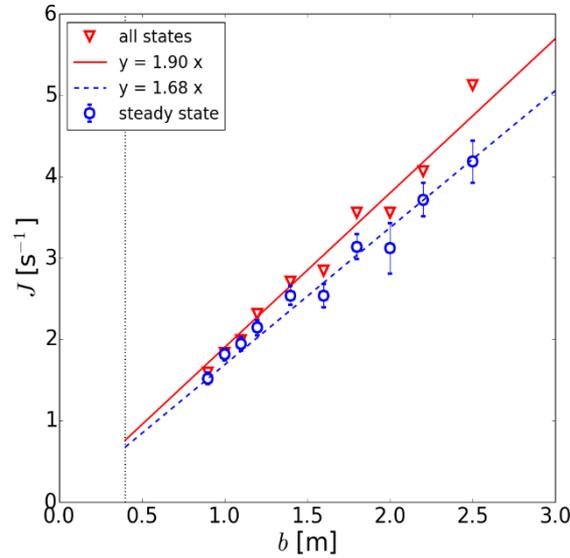
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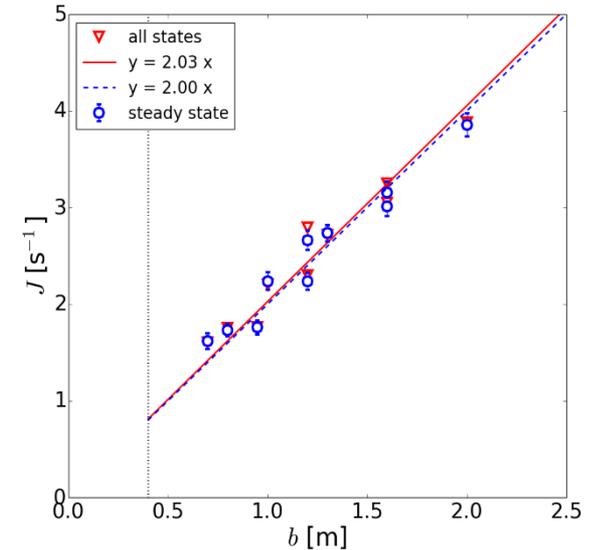
Experiment AO



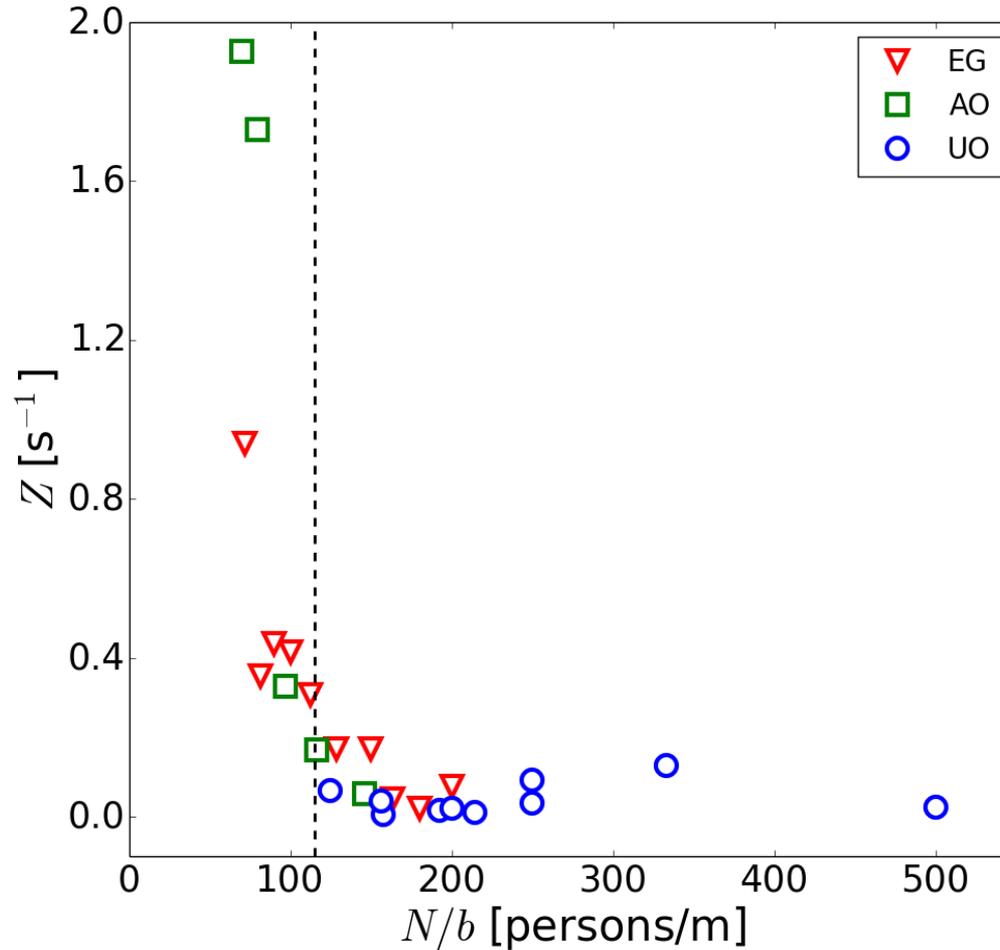
Experiment EG



Experiment UO



Detection of Steady State - Robustness



Critical value: $N/b = 115$ persons/m

Conclusions and outlook

- **Comparison of pedestrian experiments requires to distinguish carefully between transient state and steady state.**
- **For existing bottleneck experiments:**
 - ✓ **If $N/b \geq 115$ persons/m, the flow in all states can be used.**
 - ✓ **If $N/b < 115$ persons/m, first use the modified CUSUM algorithm to detect steady state, then use the flow in steady state.**
- **For the future design of bottleneck experiments:**
 - ✓ **Better to meet the requirement of $N/b \geq 115$ persons/m.**
 - ✓ **If not, pay attention to the analysis.**

Thank you!