

**TU**Delft

## MULTI-STAGE OPTIMIZATION OF ROAD NETWORKS FOR AUTOMATED DRIVING

## HEAT LAB SEMINAR: 06-12-2019



Bahman Madadi

Dr. Rob van Nes Dr. Maaike Snelder Prof. dr. Bart van Arem



### AUTOMATED DRIVING AND ROAD NETWORKS: AN INCREMENTAL APPROACH













## **RESEARCH QUESTION**

What are the possible network configurations for AVs? (e.g., dedicated lanes, zones, links, everywhere) We chose AD subnetworks: Delft case







## **EXPLORING AD SUBNETWORKS**

## **Purpose:**

Macroscopic static TA & explore subnetwork concept

## Methodology steps:

Subnetwork concept

Feasible road selection

Scenarios

**ŤU**Delft

Impacts



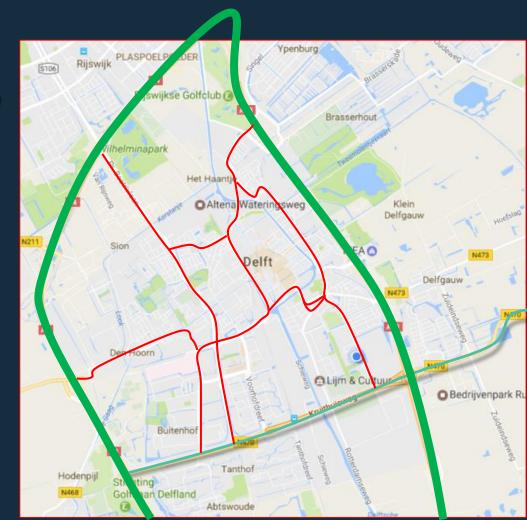
**ŤU**Delft

## **DELFT CASE 1:**

### INTRODUCING AD SUBNETWORKS

A priori link selection based on:

✓ Road function
✓ Potential quality
✓ Traffic segregation
✓ Complexity





## **DELFT CASE 1:** INTRODUCING AD SUBNETWORKS









## INTRODUCING AD SUBNETWORKS: FORMULATION

#### Minimize

$$\begin{split} Z &= \sum_{m} \frac{1}{\mu_{m}} \sum_{w \in W} \sum_{r \in \mathbb{R}^{W}} F_{m}^{w,r} \ln F_{m}^{w,r} - \sum_{m} \frac{1}{\beta_{m}} \sum_{w \in W} \sum_{r \in \mathbb{R}^{W}} F_{m}^{w,r} \ln PS_{m}^{w,r} & P_{m}^{w,r} = \frac{1}{2} \\ &+ \sum_{m \in M} \sum_{a \in A} \int_{0}^{q_{a}} c_{m,a}(x) dx, & (1) \\ \text{ s.t.} & (1) \\ q_{a} &= \gamma_{0} f_{0,a} + \gamma_{1,a} ), \quad \forall \ a \in A_{0}, & (2) \\ q_{a} &= \gamma_{0} f_{0,a} + \gamma_{1,a} ), \quad \forall \ a \in A_{1}, & (3) \\ \sum_{r \in \mathbb{R}^{W}} F_{m}^{w,r} &= D_{m}^{W}, \quad \forall \ w \in W, \forall \ m \in M, & (4) \\ \sum_{w \in W} \sum_{r \in \mathbb{R}^{W}} F_{m}^{w,r} \delta_{m,a}^{w,r} &= f_{m,a}, \quad \forall \ a \in A, \forall \ m \in M, & (5) \\ F_{m}^{w,r} &\geq 0, \quad \forall \ w \in W, \forall \ m \in M, \forall \ r \in \mathbb{R}^{w}. & (6) \\ T_{1}^{w,r} &= \frac{1}{2} \\ t_{a}(q_{a}) &= t_{a}^{0} \left[ 1 + \alpha_{a} \left( \frac{q_{a}}{\Lambda_{a}} \right)^{b_{a}} \right], & (7) \\ \text{And link cost per class is:} \\ c_{0,a}(q_{a}) &= \theta_{0} l_{a} + \eta_{0} t_{a}(q_{a}), \quad \forall \ a \in A_{1}. & (10) \\ TTT &= \sum_{a \in A} t_{a}(q_{a}) = \theta_{1} l_{a} + \eta_{1} t_{a}(q_{a}), \quad \forall \ a \in A_{1}. & (10) \\ \end{array}$$

$$P_m^{w,r} = \frac{\exp(-\mu_m C_m^{w,r} + \beta_m \ln PS_m^{w,r})}{\sum_{r \in R^w} \exp(-\mu_m C_m^{w,r} + \beta_m \ln PS_m^{w,r})}, \ \forall \ w \in W, \ \forall \ m \in M, \ \forall \ r \in R^w,$$
(11)

$$PS_m^{w,r} = \sum_{a \in r} \left(\frac{l_a}{l_r}\right) \left(\frac{1}{\sum_{r \in \mathbb{R}^w} \delta_{m,a}^{w,r}}\right),\tag{12}$$

and route-based travel cost (generalized travel cost) for two classes are given as:

$$C_0^{w,r} = \sum_{a \in A} \delta_{0,a}^{w,r} F_0^{w,r}(\theta_0 l_a + \eta_0 t_a(q_a)),$$
(13)

$$C_1^{w,r} = \sum_{a \in A_0} \delta_{1,a}^{w,r} F_1^{w,r}(\theta_0 l_a + \eta_0 t_a(q_a)) + \sum_{a \in A_1} \delta_{1,a}^{w,r} F_1^{w,r}(\theta_1 l_a + \eta_1 t_a(q_a)).$$

7) 
$$TTC = \sum_{a \in A_0} (\eta_0 \bar{t}_a + \theta_0 l_a) (\bar{f}_{0,a} + \bar{f}_{1,a}) + \sum_{a \in A_1} [(\eta_0 \bar{t}_a + \theta_0 l_a) \bar{f}_{0,a} + (\eta_1 \bar{t}_a + \theta_1 l_a) \bar{f}_{1,a}],$$
(15)

9) 
$$TTT = \sum_{a \in A} \bar{t}_a (\bar{f}_{0,a} + \bar{f}_{1,a}), \qquad (16)$$

10) 
$$TTD = \sum_{a \in A} l_a (\bar{f}_{0,a} + \bar{f}_{1,a}).$$
(17)





### DELFT CASE 1: INTRODUCING AD SUBNETWORKS (SUMMARY)

#### Scenarios:

3 (5) subnetworks & 5 (7) demand scenarios

#### Impacts:

TTC,TTT,TTD & distribution in different road types

Sensitivity analysis:

TA AV parameters

**Conclusion**:

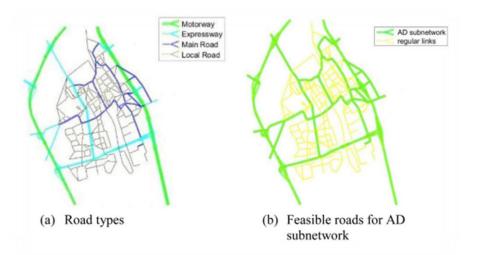
**TU**Delft

Optimizing trade-offs between costs and benefits



## **RESEARCH QUESTION**

## How can we optimize this configuration (selection)? Delft case 2: Optimizing urban road networks for AD







## OPTIMIZING URBAN ROAD NETWORKS FOR AD

## **Purpose:**

Define optimization problem, solutions, future extensions

## **Methodology:**

Formulate a bi-level optimization problem

Find (develop) solution methods & measure performance

Find methodology shortcomings & best extensions (future steps)





**ŤU**Delft

#### OPTIMIZING URBAN ROAD NETWORKS FOR AD: FORMULATION

	ULMP
$PS_m^{w,r}$	$\min_{I_a}$ s.t.
	TTC
(1)	
(2)	TAC $I_a(1$
(3)	$p_{a}^{s,t}$
(4)	$ P_{_{\hat{G}_1}} $
(5)	
(6)	
(7)	
	<ol> <li>(1)</li> <li>(2)</li> <li>(3)</li> <li>(4)</li> <li>(5)</li> <li>(6)</li> </ol>

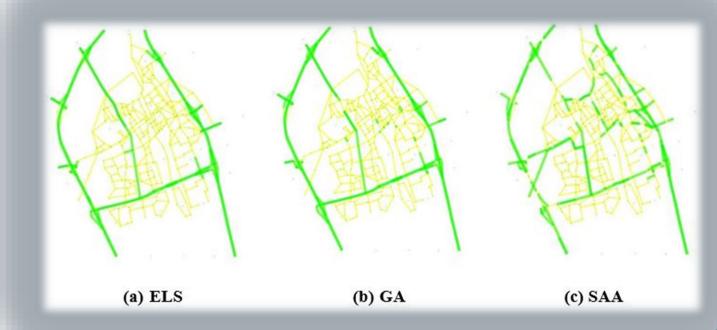
$$\begin{split} & \underset{I}{\inf} \qquad Z_{u} = TTC(I_{a}) + \frac{TAC(I_{a})}{\sigma}, \quad (9) \\ & \underset{I}{\text{t.}} \\ & TTC(I_{a}) = \sum_{a \in A} \left\{ (1 - I_{a}) [(\eta_{0}\tilde{t}_{a} + \theta_{0}l_{a})(\overline{f}_{0,a} + \overline{f}_{1,a})] \\ & \quad + I_{a} [(\eta_{0}\tilde{t}_{a} + \theta_{0}l_{a})\overline{f}_{0,a} + (\eta_{1}\tilde{t}_{a} + \theta_{1}l_{a})\overline{f}_{1,a}] \right\} \quad (10) \\ & TAC(I_{a}) = \sum_{a \in A} I_{a} a c_{a} \quad (11) \\ & I_{a} (1 - I_{a}) = 0 \quad , \forall a \in A \quad (12) \end{split}$$

$$\left| p_{_{\dot{G}_1}}^{s,t} \right| \ge 1 \qquad , \forall s,t \in N_1 \tag{13}$$



## DELFT CASE 2: LESSONS LEARNED

## **Disconnected Subnetworks!**

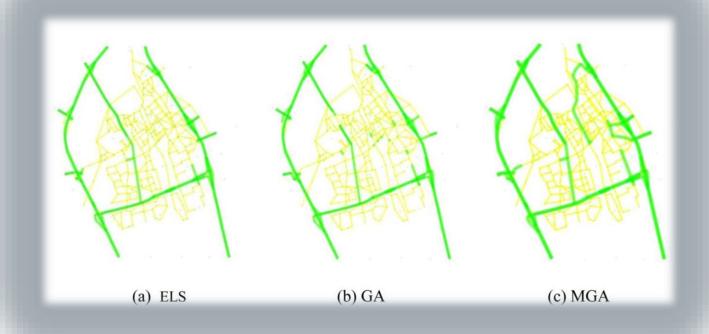






## DELFT CASE 2: LESSONS LEARNED

## **Disconnected Subnetworks!**







## **DELFT CASE 2: LESSONS LEARNED**

#### Dependency on adjustment cost and demand





90% low cost



10% high cost



## **RESEARCH QUESTION**

## What is the optimal order and timing for the adjustments? Amsterdam case study 1







#### **Purpose:**

**Tri-level** optimization problem

Can we solve this for a realistic network?

Behavioral (transport-related) insights from case study

## **Methodology:**

Formulate the optimization problem

Find (develop) solution methods & measure performance

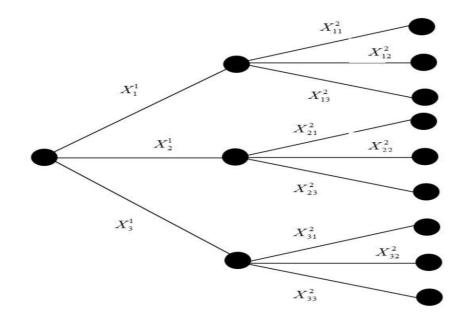
Analyze results





Upper level decision choice tree

 $\tau = 0$ 



 $\tau = 1$ 

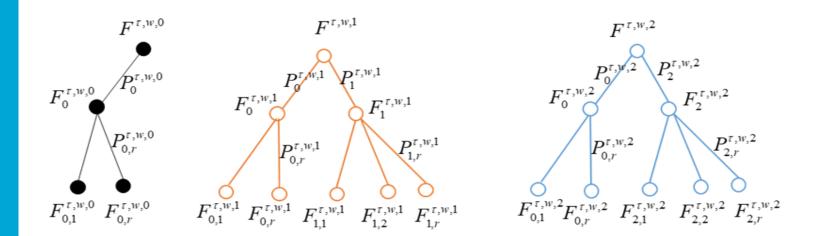


17

 $\tau = 2$ 



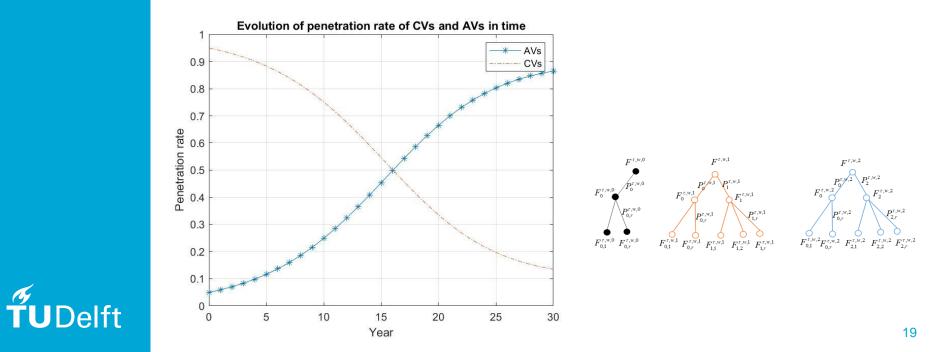
#### Lower level decision choice tree







#### **AV Diffusion model**





## AMSTERDAM CASE STUDY (VENOM MODEL)

#### 52,810 links 10,124 OD pairs

Several municipalities







## AMSTERDAM CASE STUDY

#### 52,810 links in the network (52,810 lower level decision variables)







## **AMSTERDAM CASE STUDY**

#### 5801 feasible links (2<sup>5804</sup> combinations for upper level solution)







## AMSTERDAM CASE STUDY: UPPER LEVEL SOLUTION ALGORITHMS

#### GA

#### EPS

Out of the box Augmented time Connectivity penalty Adapted Tailored

#### EGS

Novel Fully tailored







## Evolution of networks and connectivity t = 0









## Evolution of networks and connectivity t = 0







## **AMSTERDAM CASE 1:** LESSONS LEARNED

## More cars and increased TT! Shift towards the main roads





Before

After



## **AMSTERDAM CASE 1:**

## To do: Distribution of accessibility and mode choice

## Demand supply interactions: proactive v.s. reactive Waiting for the demand or provoking it?







# **QUESTIONS?**



