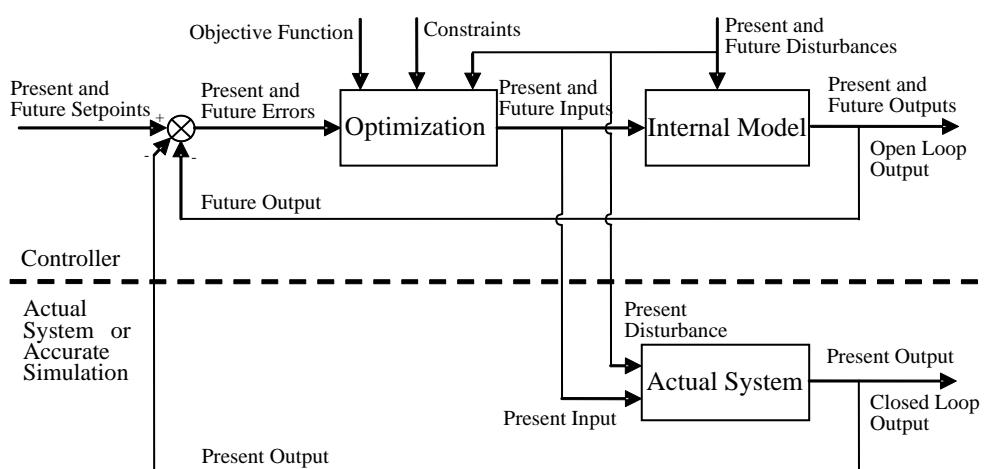


# Model Predictive Control on Irrigation Canals

## Application on the Central Main Canal in Arizona

Master Thesis



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