The limit distribution of the L_{∞} -error of Grenander type estimators

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Let f be a non-increasing function defined on [0, 1]. Under standard regularity conditions, we derive the asymptotic distribution of the supremum distance between f and its isotonic estimator on any interval $(\alpha_n, 1 - \alpha_n] \subset$ [0, 1], where α_n tends to zero at a suitable rate. The rate of convergence of the supremum distance is found to be of order $(\log n/n)^{1/3}$ and the limiting distribution turns out to be Gumbel with a parameter depending on a functional of f and f'. The results are obtained in a general framework, which includes the Grenander estimator of a decreasing density, the least squares estimator of a monotone regression curve or an isotonic estimator of a decreasing hazard of right-censored observations.

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