

# Towards Exascale Computing Simulation on Millions of Cores

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*Mathematics in Waterland*  
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LEHRSTUHL FÜR INFORMATIK 10 (SYSTEMSIMULATION)

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# Friedrich-Alexander University Erlangen-Nürnberg

- # Founded 1743
- # 5 Schools, 22 Departments, 24 Clinics
- # 28,000 students in 132 programs
- # ~ 500 tenured faculty (full and associate profs)
- # ~ 900 PhD and Dr. habil. degrees in 2007
- # ~ 92 Mio Euro external funding/ year
- # School of Engineering founded in 1966
  - Currently about 6000 students



# Overview

- # Motivation: How fast are computers today (and tomorrow)
- # Scalable Parallel Multigrid Algorithms for PDE
  - Matrix-Free FE solver: Hierarchical Hybrid Grids
  - Experiments with Multigrid on GPUs
- # A Multi-Scale & Multi-Physics Simulation
  - Rigid Body Dynamics for Granular Media
  - Flow Simulation with Lattice Boltzmann Methods
  - Fluid-Structure Interaction with Moving Rigid Objects
    - particle laden flows
    - preliminary GPU performance comparison
- # Conclusions

# Motivation

# Example Peta-Scale System: Jugene @ Jülich

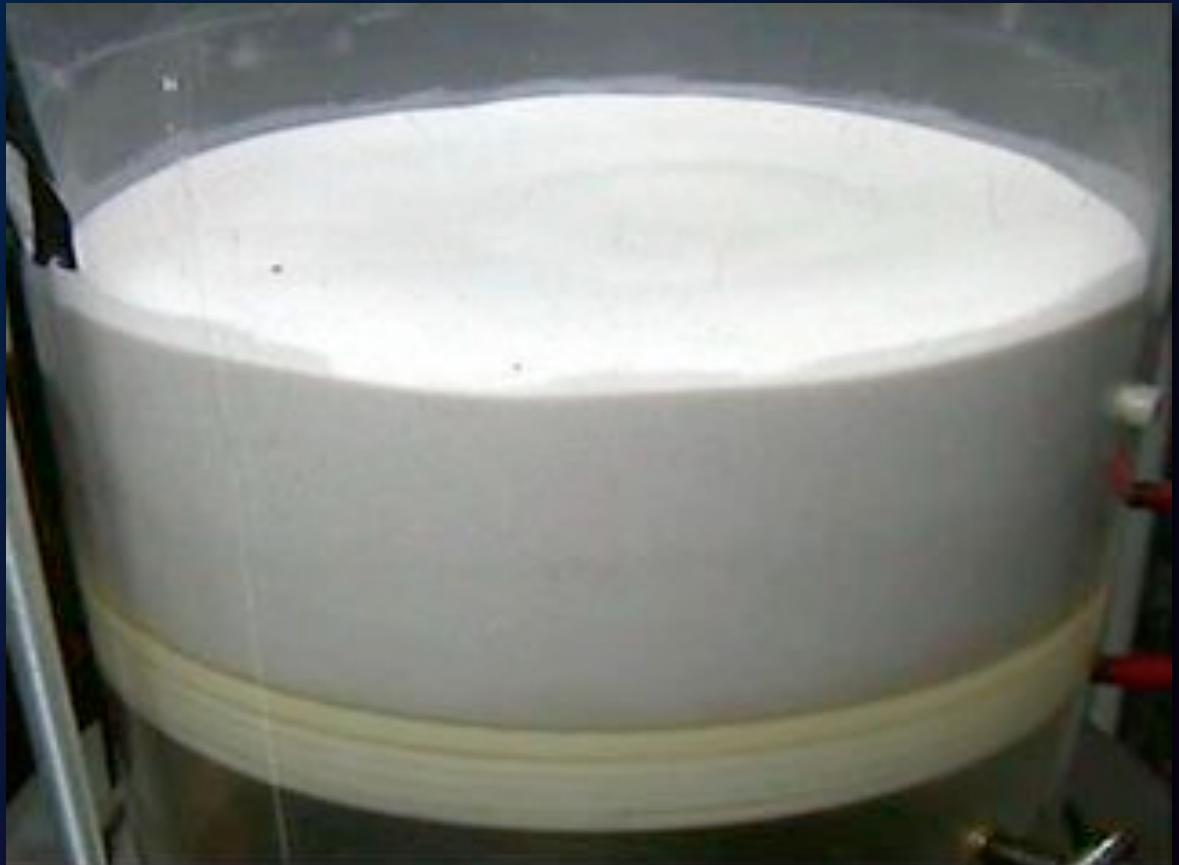


- # PetaFlops =  $10^{15}$  operations/second
- # IBM Blue Gene
- # Theoretical peak performance: 1.0027 Petaflop/s
- # 294 912 cores
- # 144 TBytes =  $1.44 \cdot 10^{14}$
- # #9 on TOP 500 List in Nov. 2010

- # For comparison: Current fast desktop PC is ~ 20.000 times slower
- # > 1 000 000 cores expected 2011
- # Exa-Scale System expected by 2018/19

# What can we do with Exa-Scale Computers?

- # Even if we want
  - to simulate a billion objects (particles): we can do a billion operations for each of them in each second
  - a trillion finite elements (finite volumes) to resolve a PDE, we can do a million operations for each of them in each second
- # Most existing software dramatically underperforms on contemporary HPC architectures
- # This will get more dramatic on future exa-scale systems



Fluidized Bed

(movie: thanks to K.E. Wirth)

# What's the problem?

with four strong jet engines  
(not those of Rolls-Royce of course)



Would you want to propel  
a Super Jumbo



or with 300,000  
blow dryer fans?



# How fast are our algorithms (multigrid) on current CPUs

- # Assumptions:
  - Multigrid requires 27.5 Ops/unknown to solve an elliptic PDE (Griebel '89 for 2-D Poisson)
  - A modern laptop CPU delivers >10 GFlops peak
- # Consequence:
  - We should solve one million unknowns in 0.00275 seconds
  - ~ 3 ns per unknown
- # Revised Assumptions:
  - Multigrid takes 500 Ops/unknown to solve your favorite PDE
  - you can get 5% of 10 Gflops performance
- # Consequence: On your laptop you should
  - solve one million unknowns in 1.0 second
  - ~ 1 microsecond per unknown
- # Consider Banded Gaussian Elimination on the Play Station (Cell Processor), single Prec. 250 GFlops, for 1000 x 1000 grid unknowns
  - # ~2 Tera-Operations for factorization - will need about 10 seconds to factor the system
  - # requires 8 GB Mem.
  - # Forward-backward substitution should run in about 0.01 second, except for bandwidth limitations

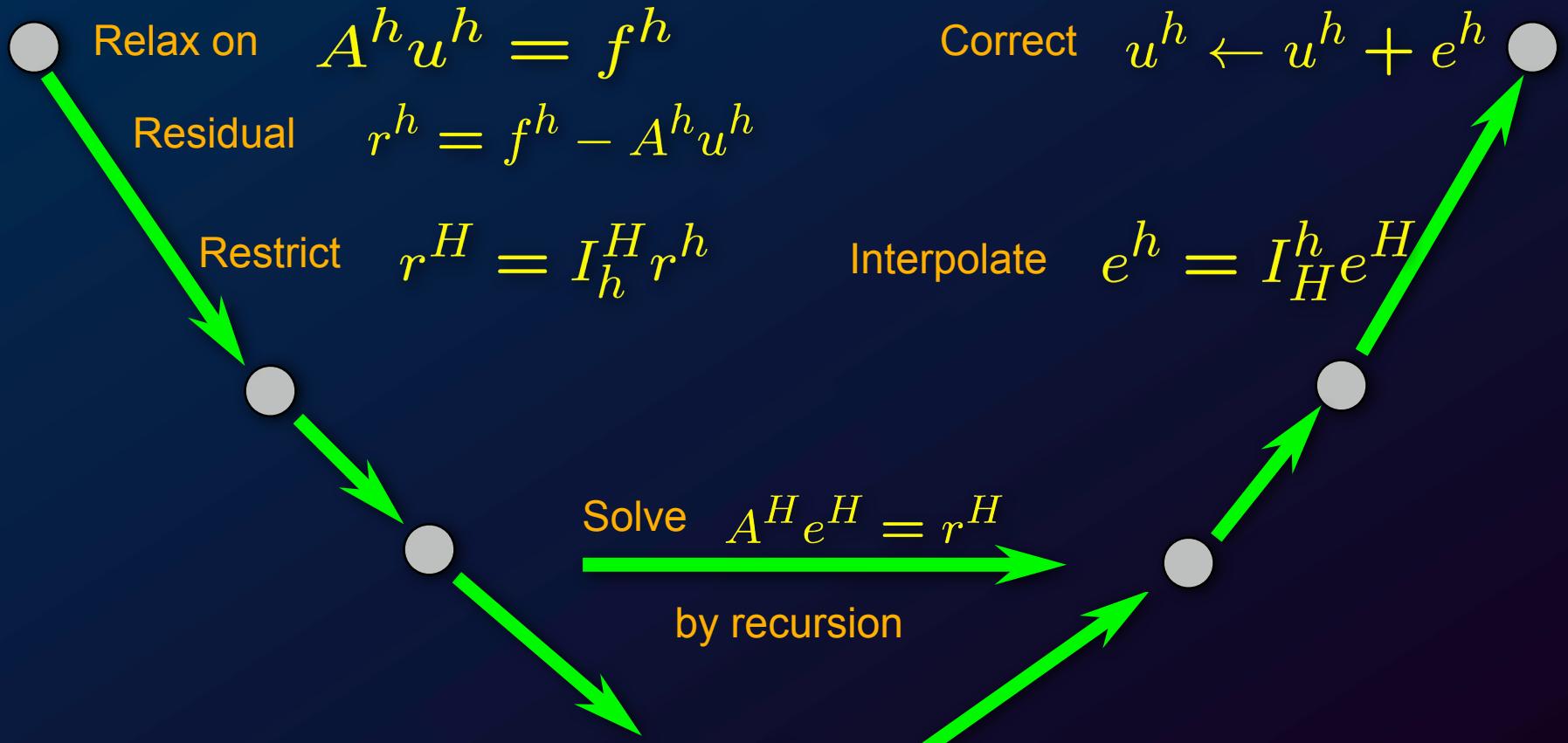
# Towards Scalable FE Software

## Scalable Algorithms and Data Structures

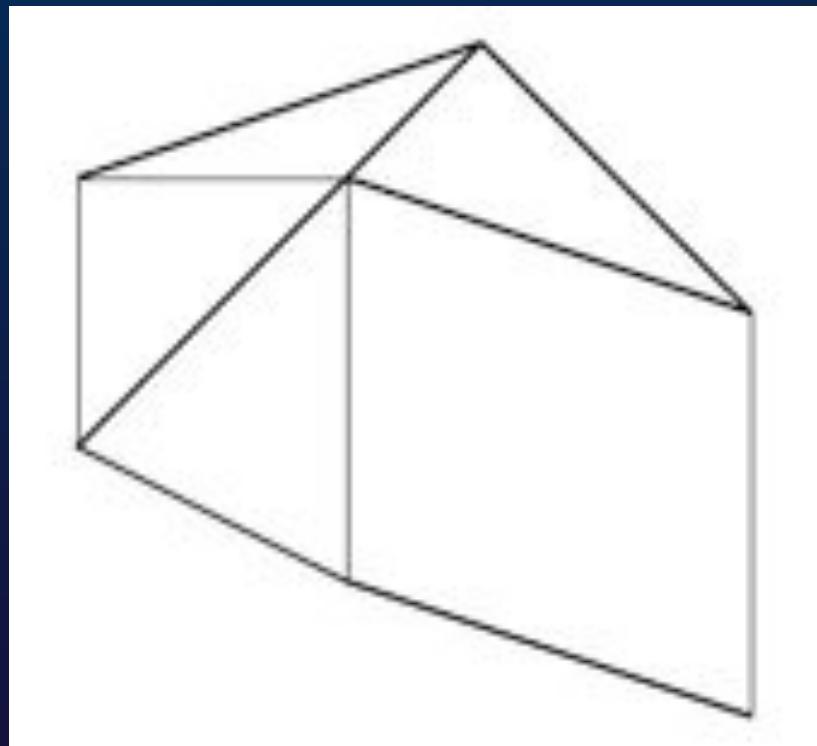


# Multigrid: V-Cycle

Goal: solve  $A^h u^h = f^h$  using a hierarchy of grids

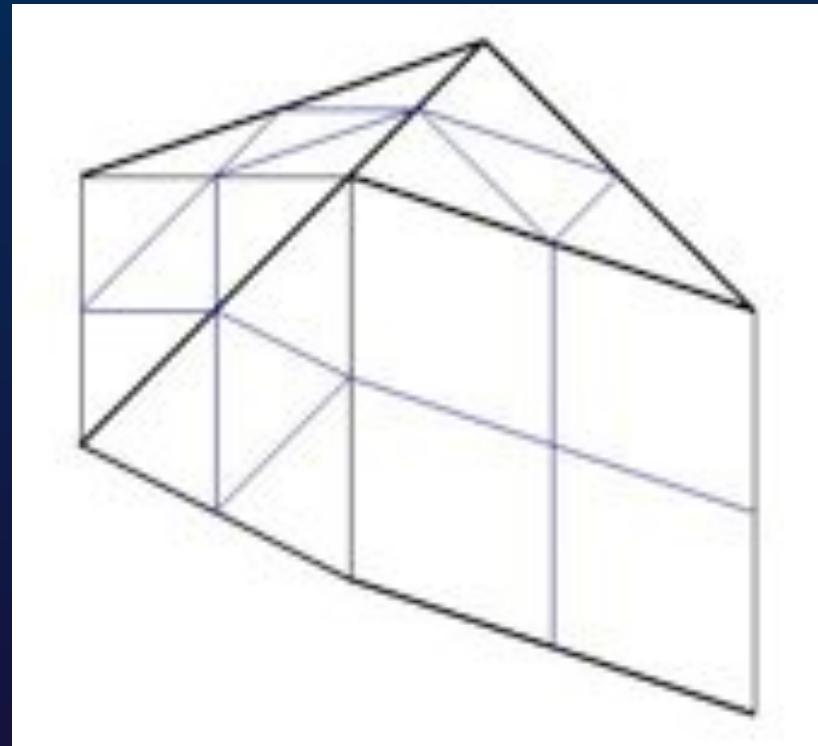


# HHG refinement example



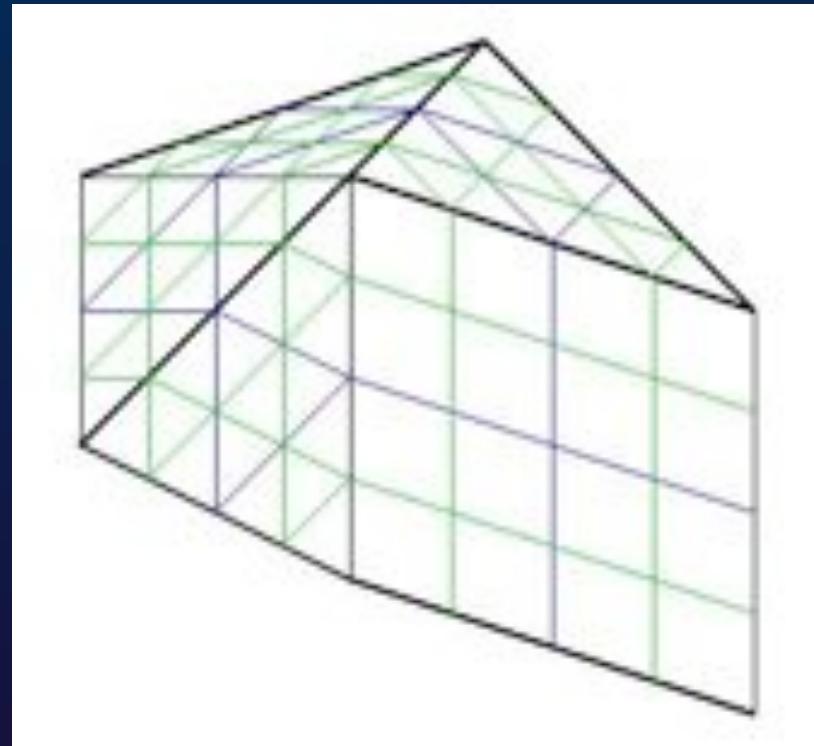
Input Grid

# HHG Refinement example



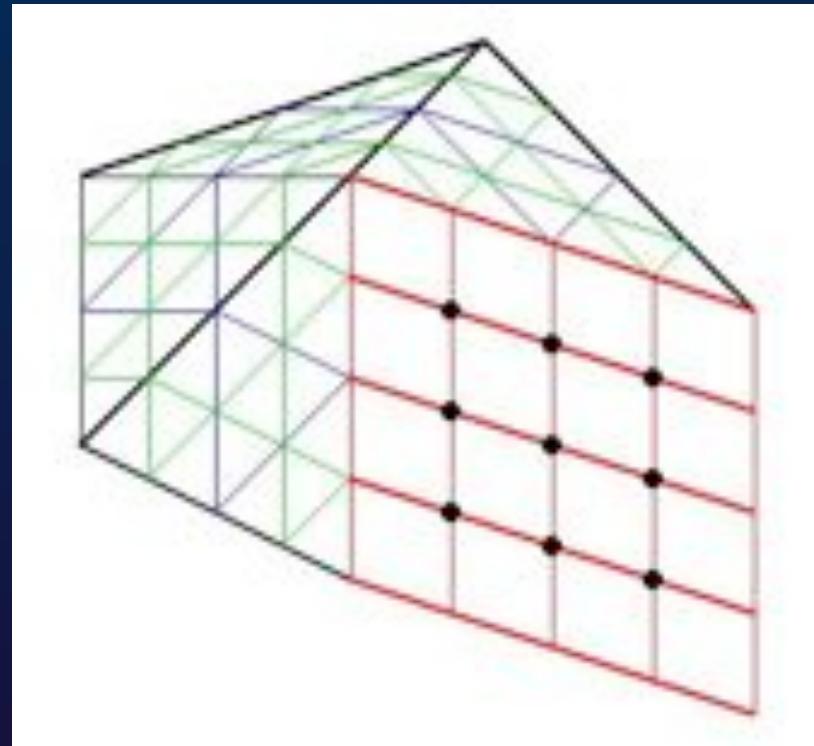
Refinement Level one

# HHG Refinement example



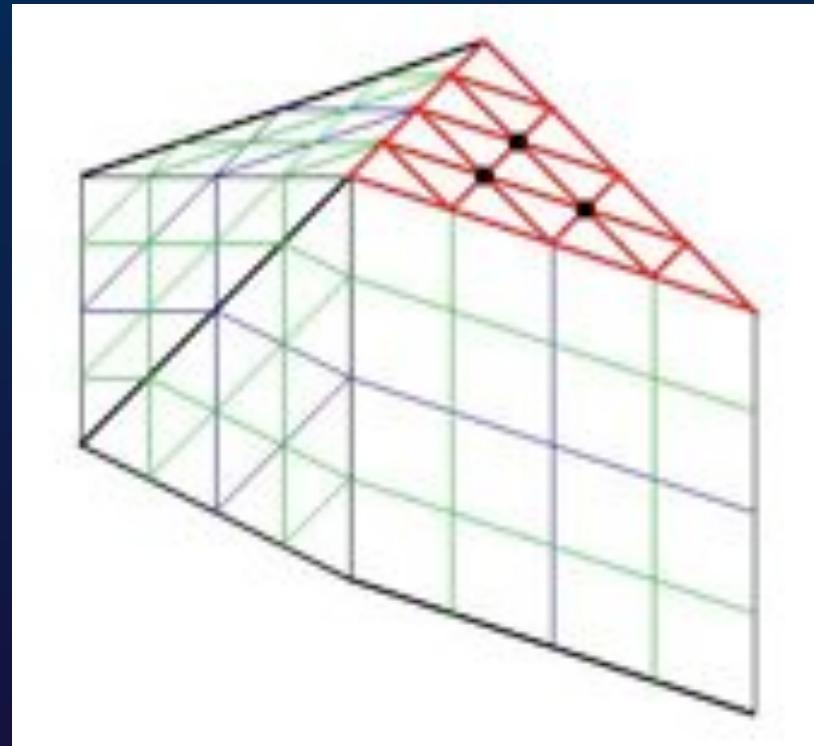
Refinement Level Two

# HHG Refinement example



Structured Interior

# HHG Refinement example



Structured Interior

# HHG Scalability on Jugene

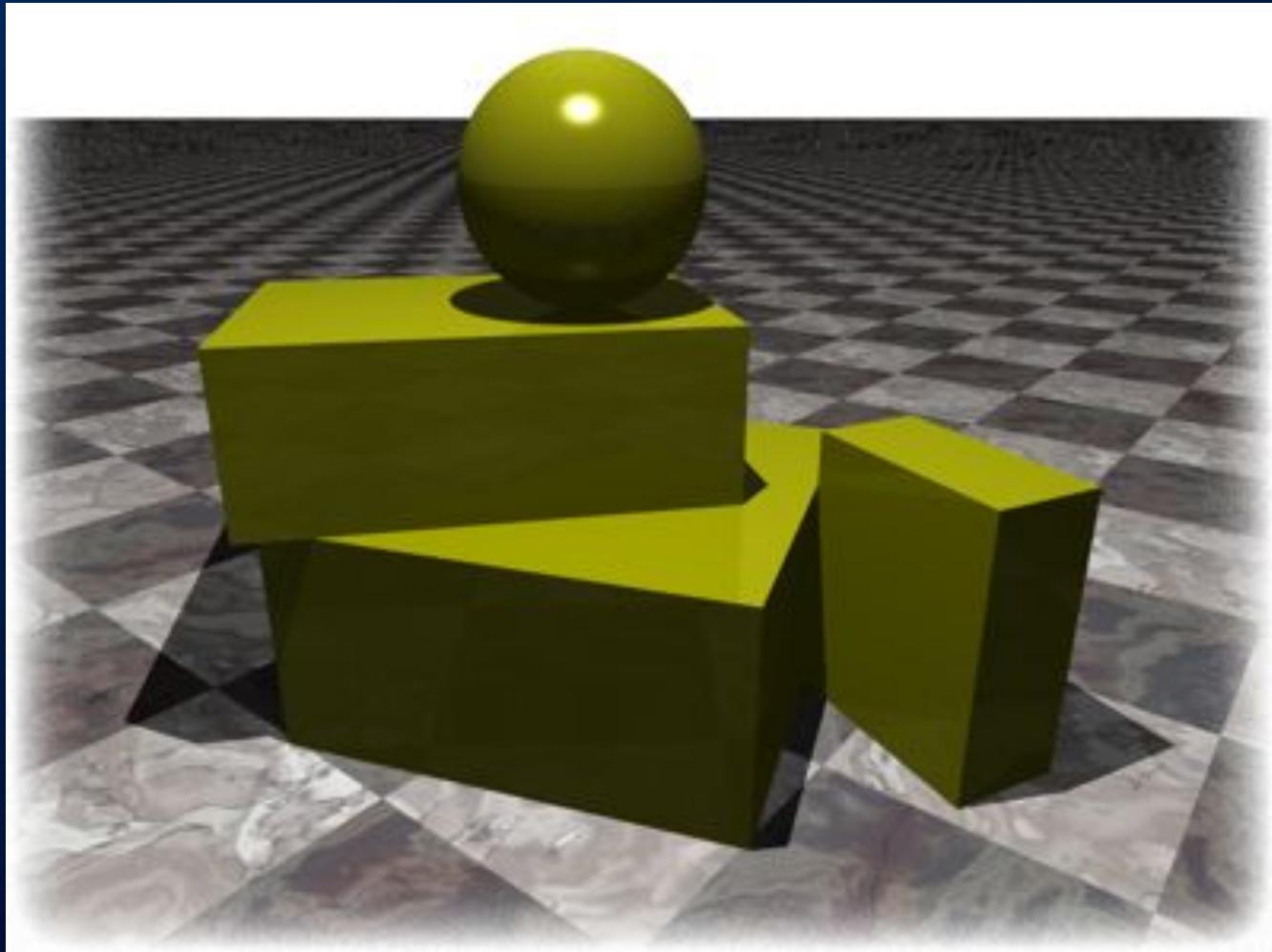
Cores	Struct.	Regions	Unknowns	CG	Time
128		1 536	534 776 319	15	5.64
256		3 072	1 070 599 167	20	5.66
512		6 144	2 142 244 863	25	5.69
1024		12 288	4 286 583 807	30	5.71
2048		24 576	8 577 357 823	45	5.75
4096		49 152	17 158 905 855	60	5.92
8192		98 304	34 326 194 175	70	5.86
16384		196 608	68 669 157 375	90	5.91
32768		393 216	137 355 083 775	105	6.17
65536		786 432	274 743 709 695	115	6.41
131072		1 572 864	549 554 511 871	145	6.42
262144		3 145 728	1 099 176 116 223	180	6.81
294912		294 912	824 365 314 047	110	3.80

# An Example of High Performance Multi-Scale and Multi-Physics Simulation

(without multigrid)



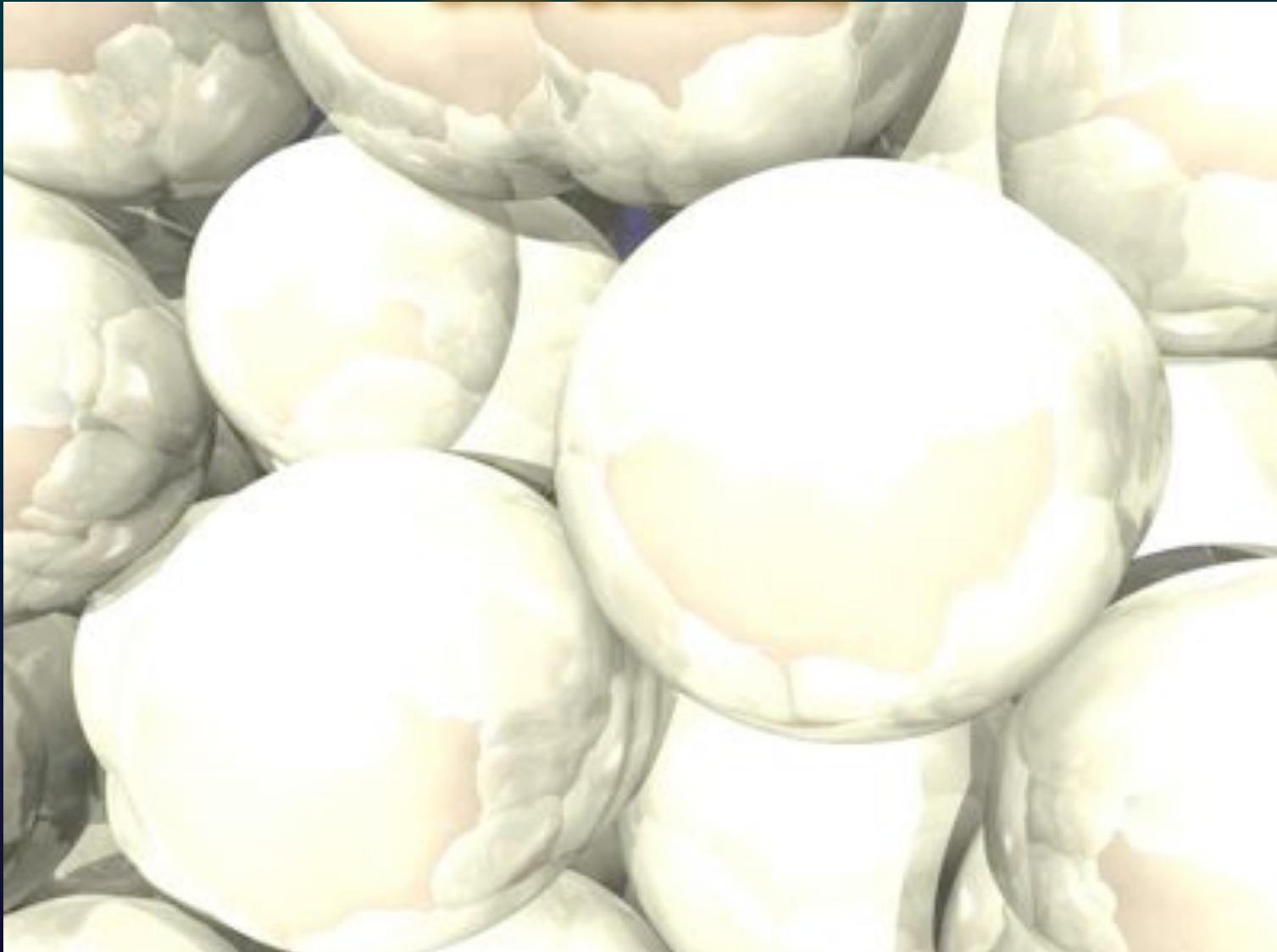
# Collisions & Contacts between Rigid Objects



# Granular Media Simulations

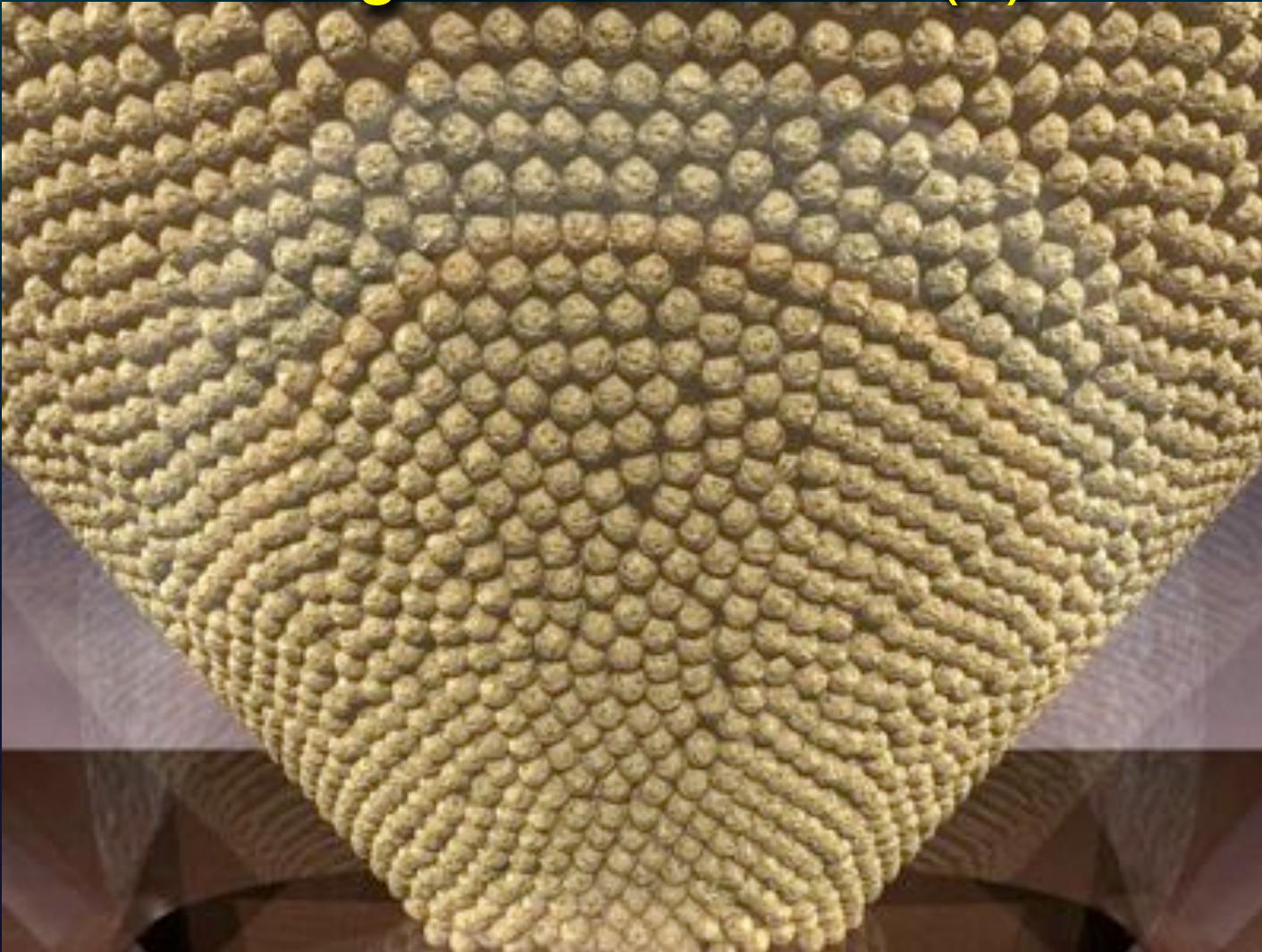


# Silo Scenario



27270 randomly generated, non-spherical particles, 256 CPUs, 379300 time steps,  
runtime: 16.4h (including data output), 0.154s per time step

# Hourglass Simulation (1)



1250000 spherical particles, 256 CPUs, 300300 time steps, runtime: 48h (including data output)

# How far can we go? Scaling Results!

# Cores	# Particles	Partitioning	Runtime [s]
128	2000 000	8 x 4 x 4	727.096
256	4 000 000	8 x 8 x 4	726.991
512	8 000 000	8 x 8 x 8	727.150
1 024	16 000 000	16 x 8 x 8	727.756
2 048	32 000 000	16 x 16 x 8	727.893
4 096	64 000 000	16 x 16 x 16	728.593
8 192	128 000 000	32 x 16 x 16	728.666
16 384	256 000 000	32 x 32 x 16	728.921
32 768	512 000 000	32 x 32 x 32	729.094
65 536	1 024 000 000	64 x 32 x 32	728.674
131 072	2 048 000 000	64 x 64 x 32	728.320

\* Jugene simulation results of 1000 time steps of a dense granular gas contained in an evacuated box without external forces. Klaus Iglberger, PRACE Award, 2010.

# Flow Simulation with Lattice Boltzmann Methods

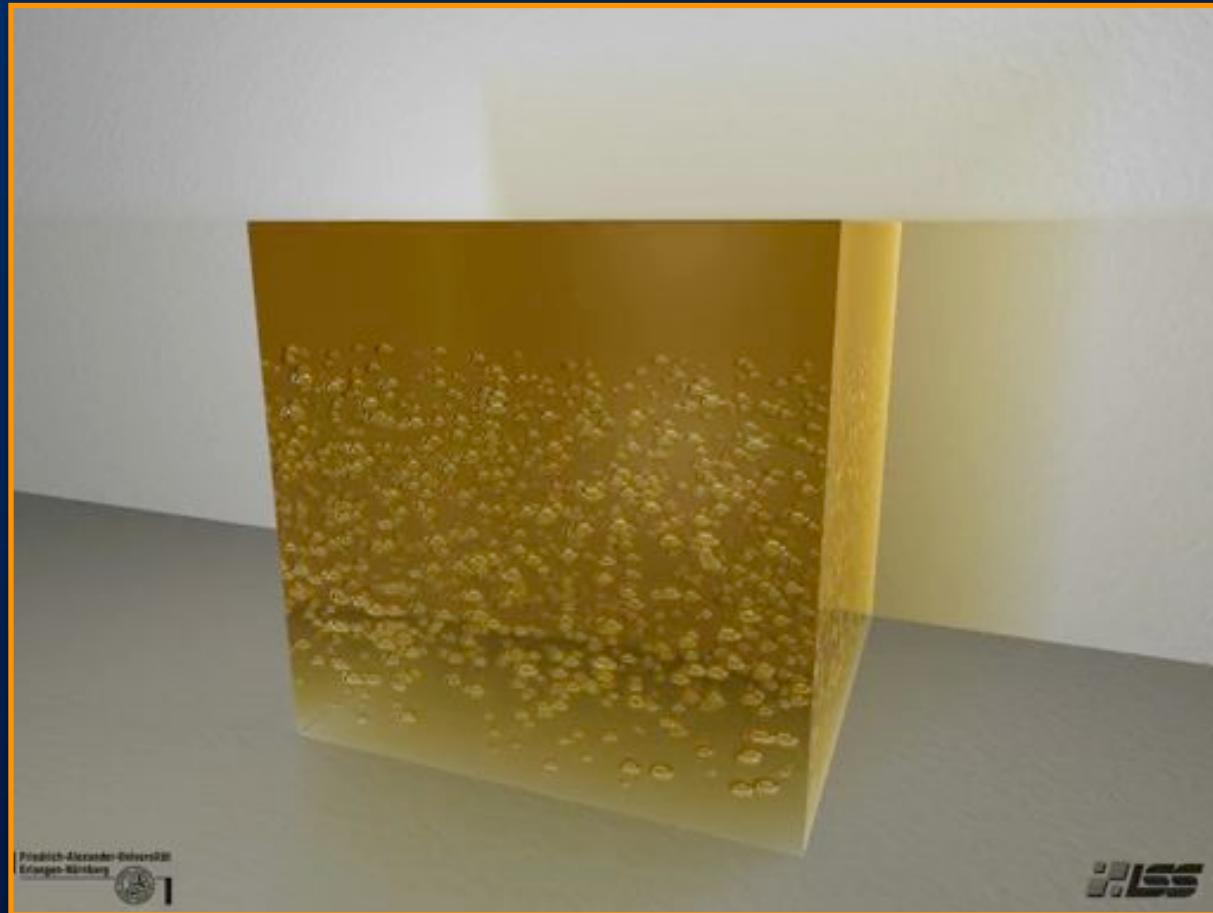


# Simulation of Metal Foams

- # Example application:
  - Engineering: metal foam simulations
- # Based on LBM:
  - Free surfaces
  - Surface tension
  - Disjoining pressure to stabilize thin liquid films
  - Parallelization with MPI and load Balancing
- # Collaboration with C. Körner (Dept. of Material Sciences, Erlangen)
- # Other applications:
  - Food processing
  - Fuel cells



# Larger-Scale Computation: 1000 Bubbles



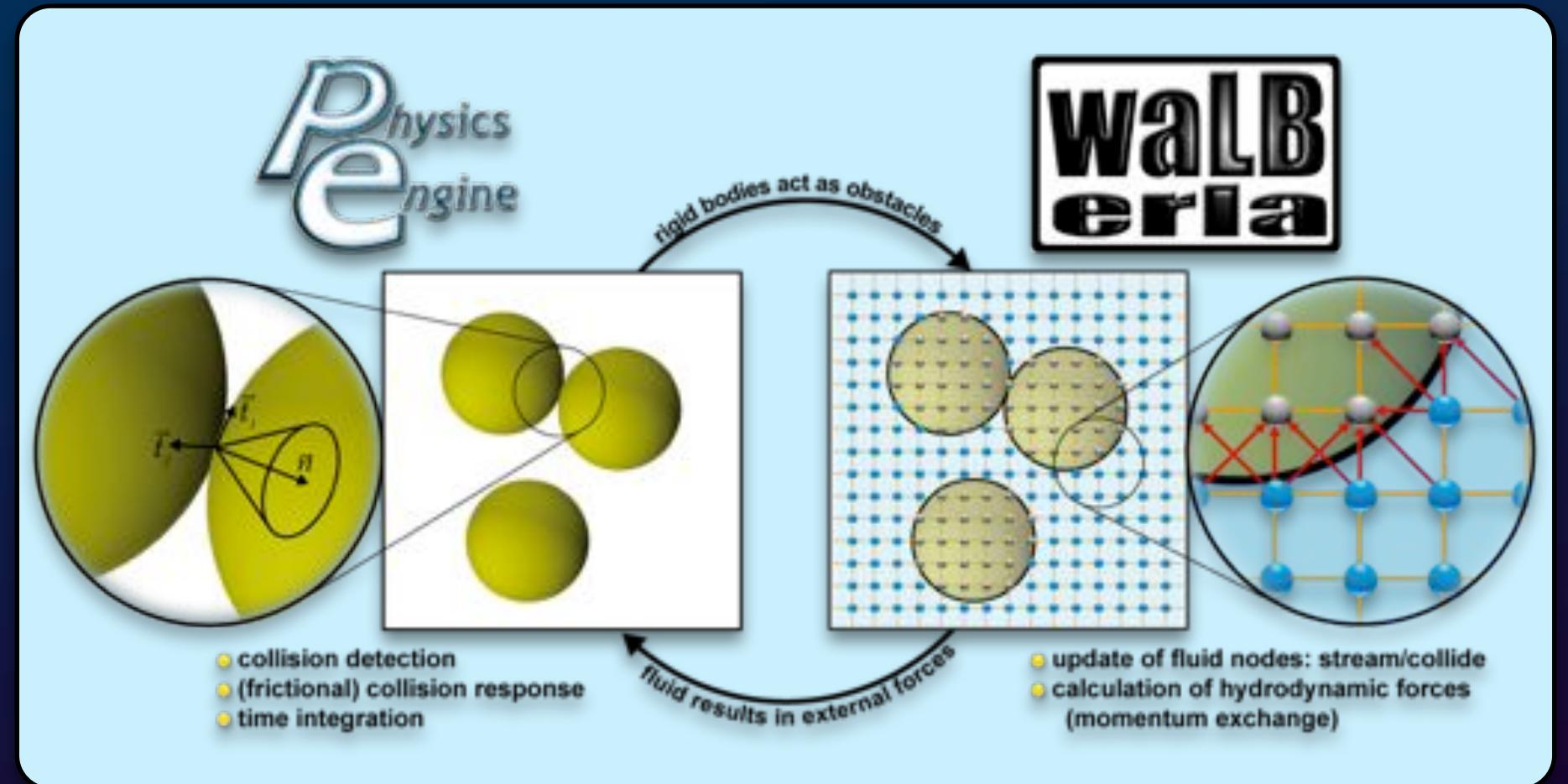
Simulation  
1000 Bubbles  
 $510 \times 510 \times 530 =$   
 $1.4 \cdot 10^8$  lattice cells  
70,000 time steps  
77 GB  
64 processes  
72 hours  
4,608 core hours

Visualization  
770 images  
Approx. 12,000 core  
hours for rendering

Best Paper Award for Stefan Donath (LSS Erlangen) at  
ParCFD, May 2009 (Moffett Field, USA)

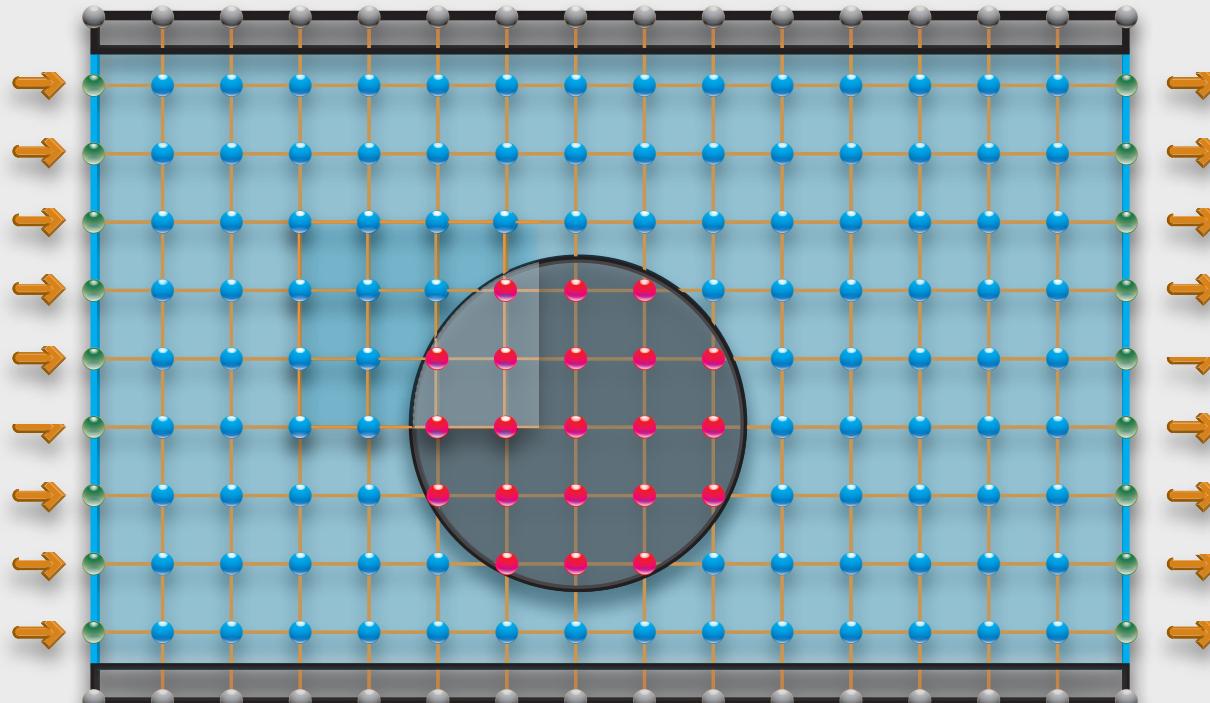
# Fluid-Structure Interaction with Moving Rigid Bodies

# Fluid-Structure Interaction

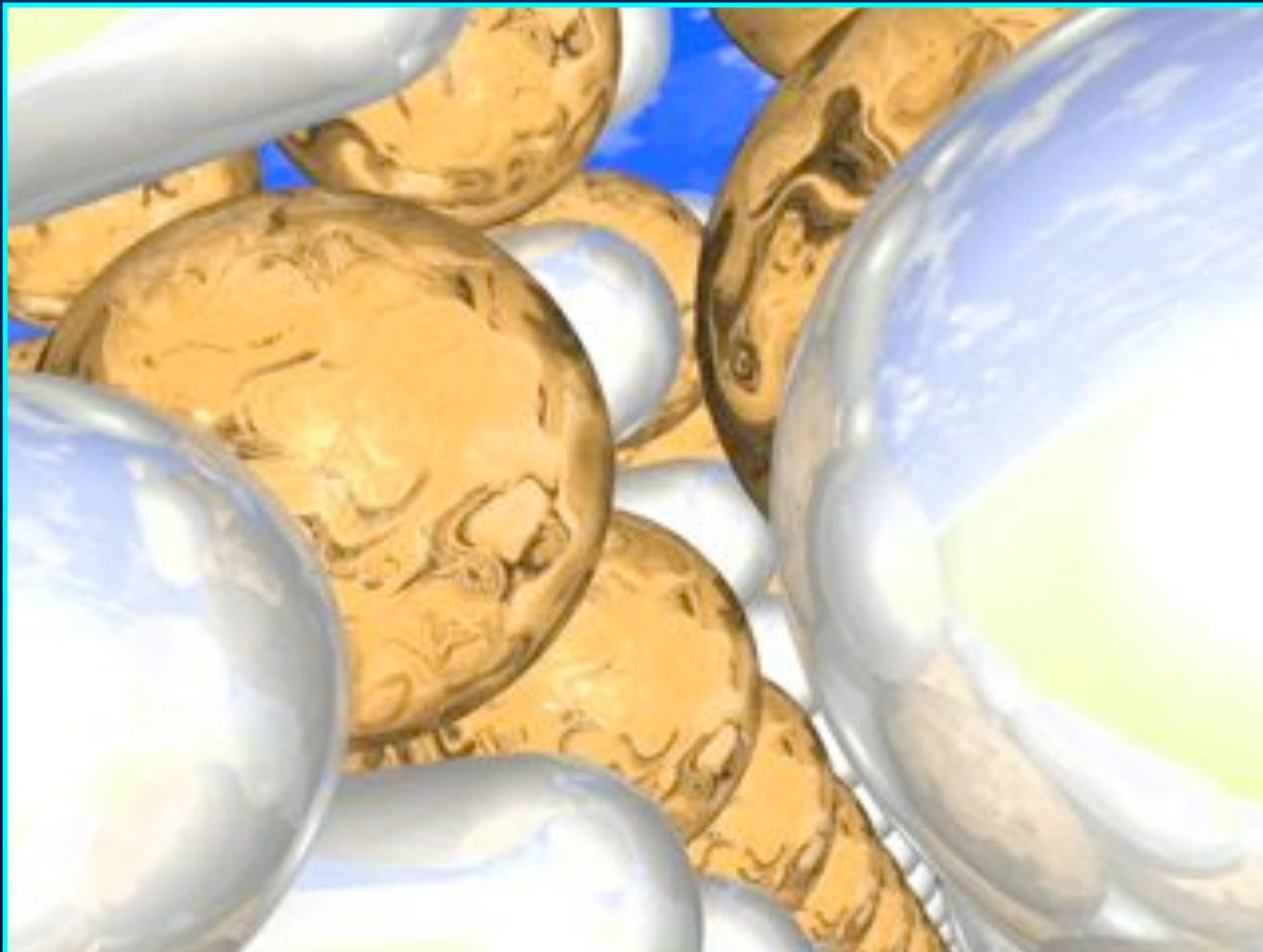


# Mapping Moving Obstacles into the LBM Fluid Grid

## An Example



# Virtual Fluidized Bed



512 processors

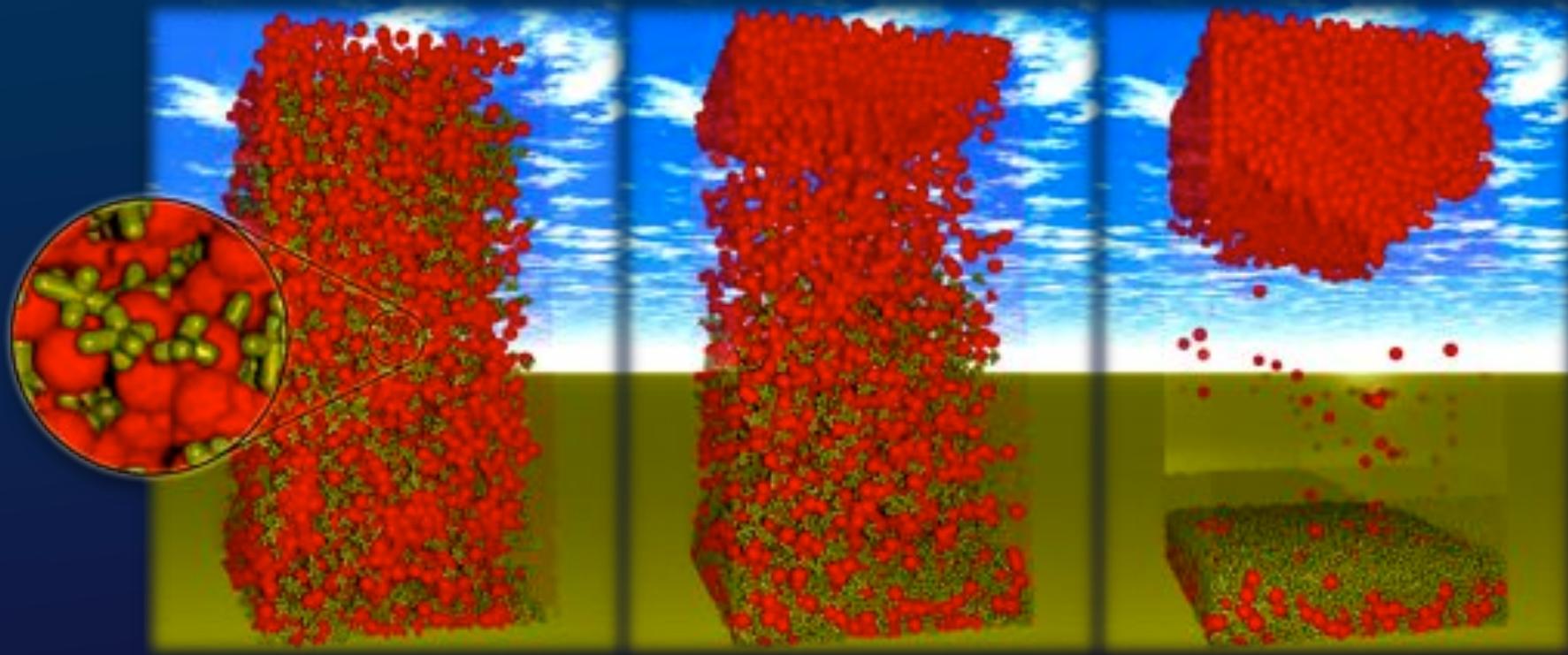
Simulation Domain  
Size: 180x198x360  
cells of LBM

900 capsules and  
1008 spheres  
= 1908 objects

Number time steps:  
252,000

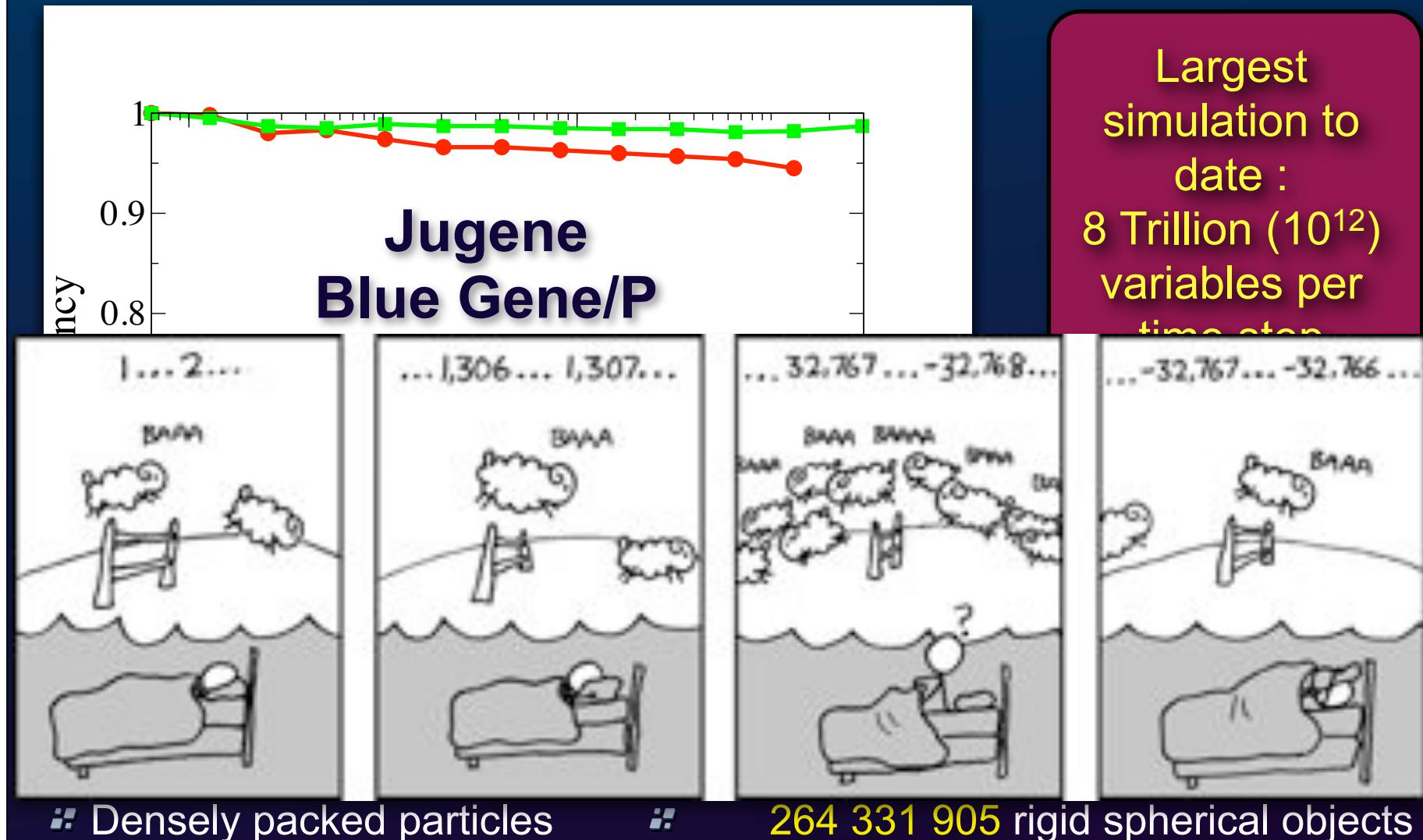
Run Time:  
07h 12 min

# Simulation of a Segregation Process



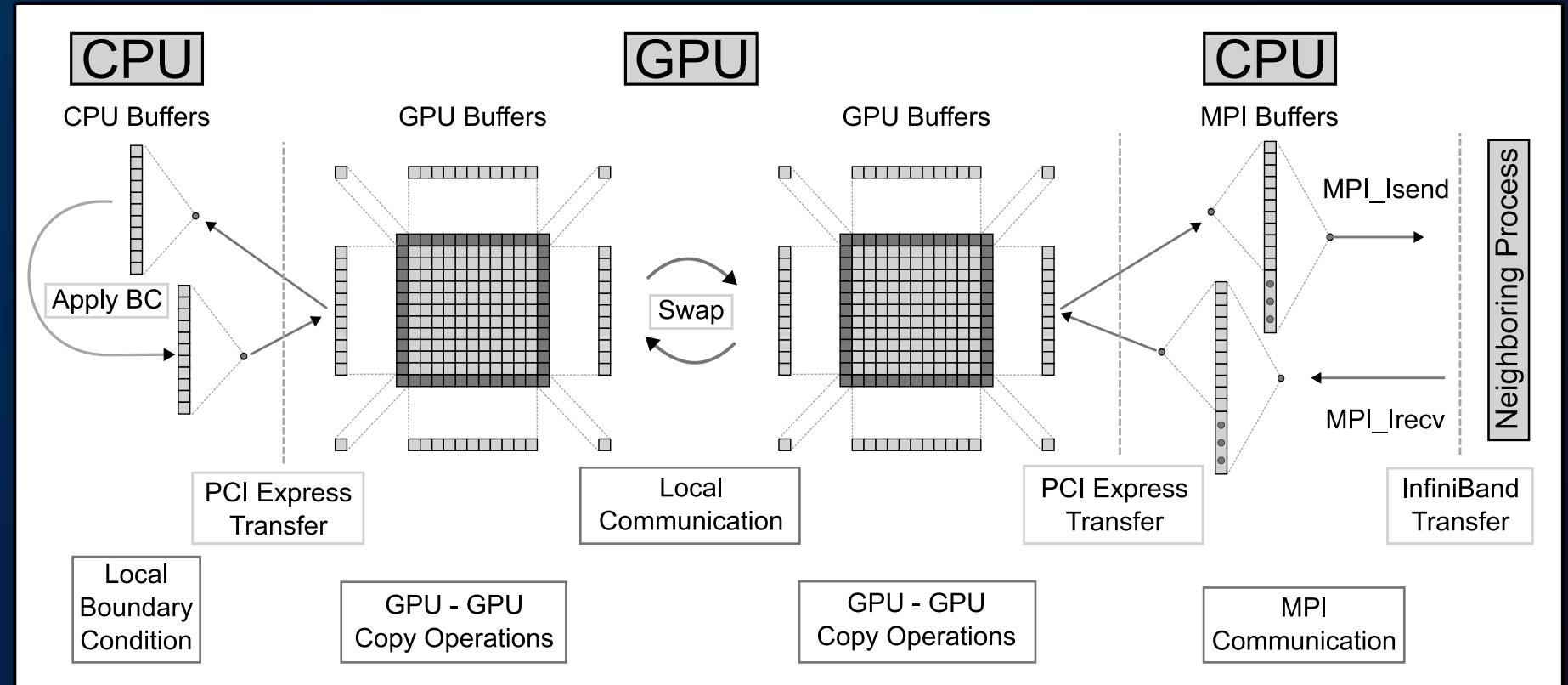
Segregation simulation of 12 013 objects. Density values of  $0.8 \text{ kg/dm}^3$  and  $1.2 \text{ kg/dm}^3$  are used for the objects in water.

# Weak Scaling



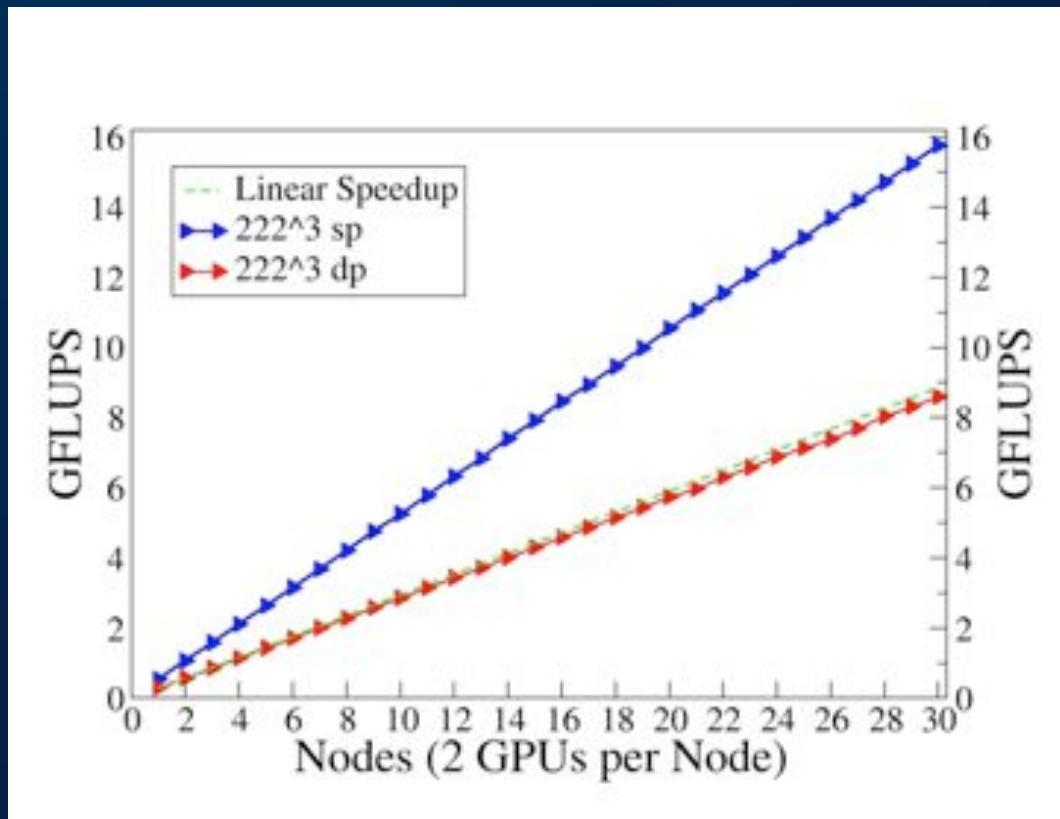
# LBM on Clusters with GPUs

# waLBerla Software Architecture for GPU Usage



- # Patch Architecture
- # Only LBM on GPU
  - no free surfaces
  - no FSI
- # NEC Nehalem
  - Xeon E5560
  - 2.8 GHz
  - 12 GB per Node
  - 2 GPUs per Node
- # nVIDIA TESLA S1070
  - 30 Nodes
  - up to 60 GPUs

# GPU Performance Results and Comparison



How far is it to do „Real Time CFD“?

25 GLups would compute

- 25 Frames per second for a LBM grid with
- resolution 1000 x 1000 x 1000

- Up to 500 MLup/s on a single GPU for plain LBM kernel (SP)
- 250 MLups/s for GPU in cluster
- Compares to 75 MLup/s for Nehalem Node (8 cores)
- A GPU node (2 GPUs) delivers performance like
  - 6 Nehalem Nodes (48 cores)
  - 75 IBM Blue Gene/P Nodes
- 30 GPU nodes (60 GPUs) are equivalent to
  - 137 Nehalem nodes (1096 cores)
  - 1275 Jugene/P nodes (5100 cores)

# Conclusions

# The ~~Two~~ Principles of Science

## Three

### Theory

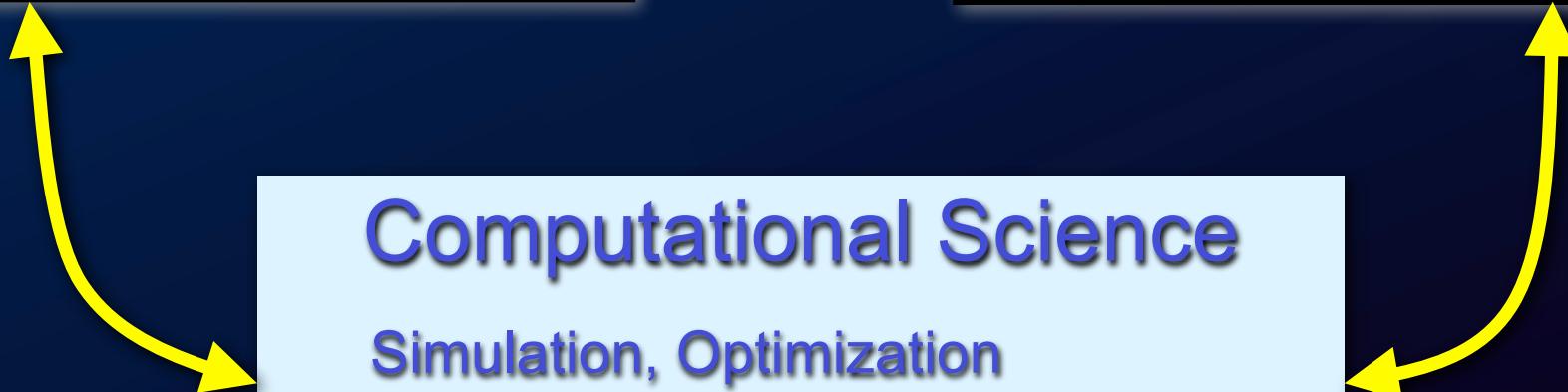
Mathematical Models,  
Differential Equations,  
Newton

### Experiments

Observation and  
prototypes  
empirical Sciences

### Computational Science

Simulation, Optimization  
(quantitative) virtual Reality



# Thank you for your attention!



Questions?

A grayscale microscopic image showing a close-up view of a microorganism, possibly a rotifer or similar ciliated microorganism, with its internal structures and cilia clearly visible.

Slides, reports, thesis, animations available for download at:  
[www10.informatik.uni-erlangen.de](http://www10.informatik.uni-erlangen.de)

