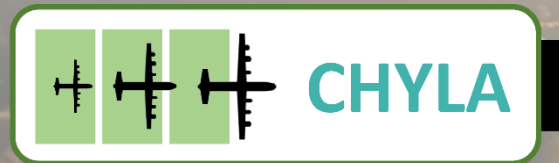




Credibility-based MDO Results

NICOLAS WAHLER, ALI ELHAM



CREDIBLE HYBRID ELECTRIC AIRCRAFT





Credibility Quantification



Credibility quantification

- Different parameters have different levels
 - Data
 - Forecasts
 - Variability
 - TRL
- Different approaches necessary for each type of data
- Determining what type of distribution is sensible or possible



Uncertain variables

- Energy storage
 - Gravimetric energy density of batteries
- Electric motors
 - Gravimetric power density of electrical machines
 - Volumetric power density of electrical machines
- Airframe parameters
 - Structural wing weight reductions
 - Area of laminar flow over the wing



Uncertain variables

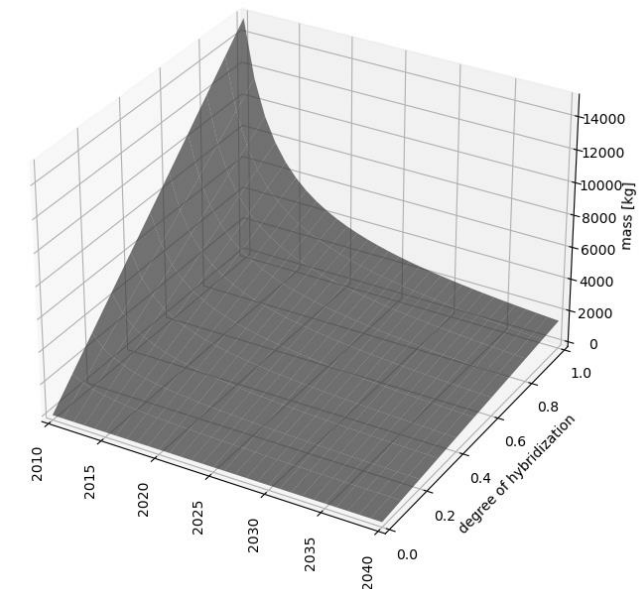
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Battery gravimetric density

- Most challenging parameter for electric flight
- Battery performance also dependent on cell composition
 - Generic approach necessary
 - Transformation from **cell** to **pack** level
- Lithium-based batteries will remain predominant
 - Advances in cathode and anode materials

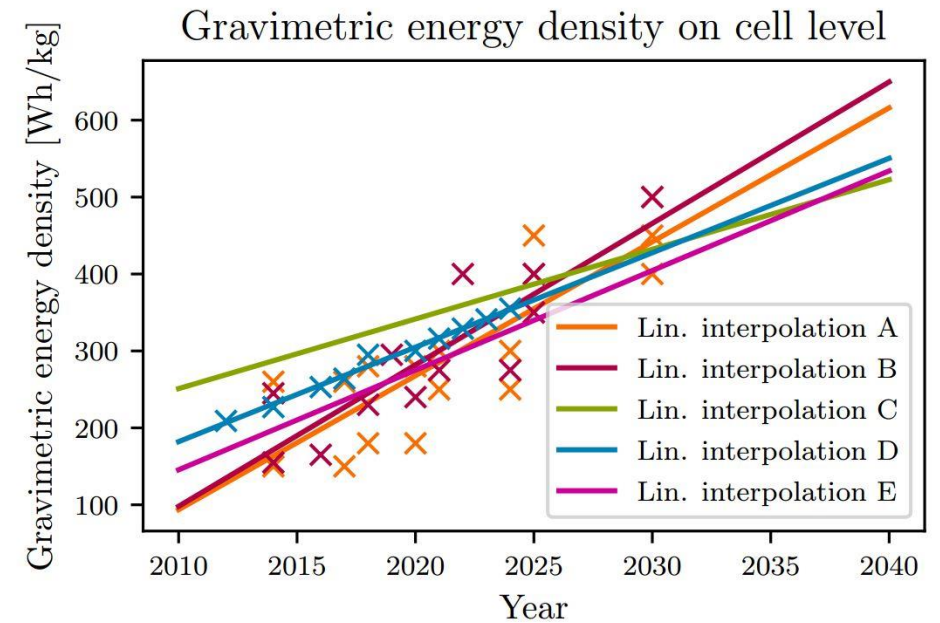
Estimated weight reduction of the battery cell mass for a consistent battery configuration (2010 to 2040, for different degrees of hybridization)





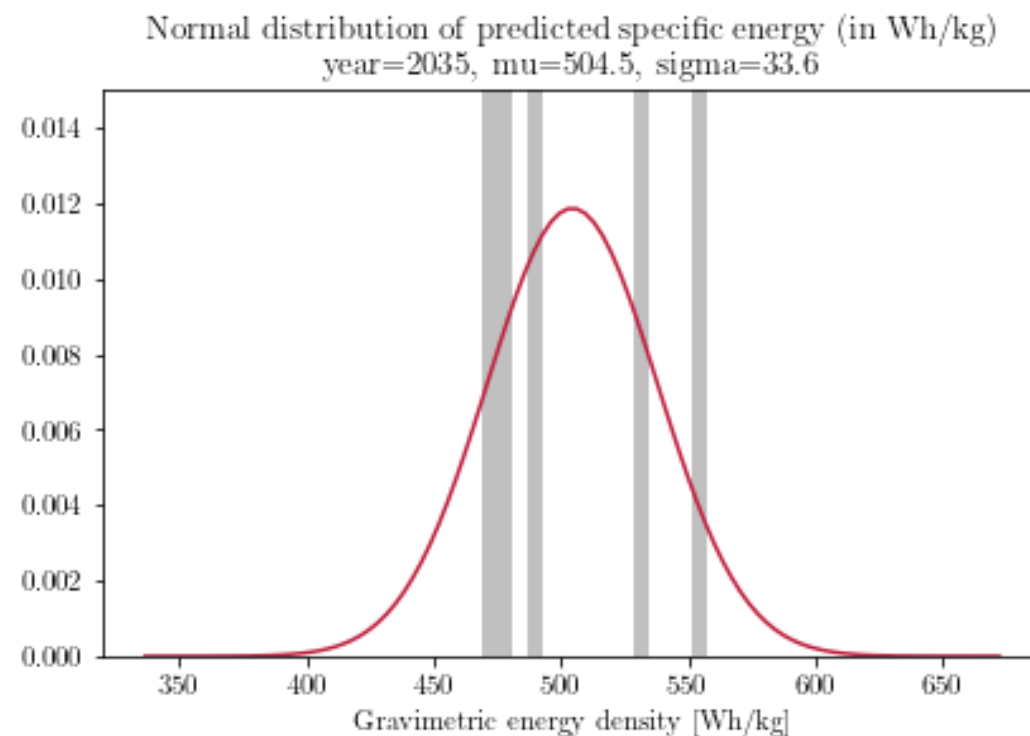
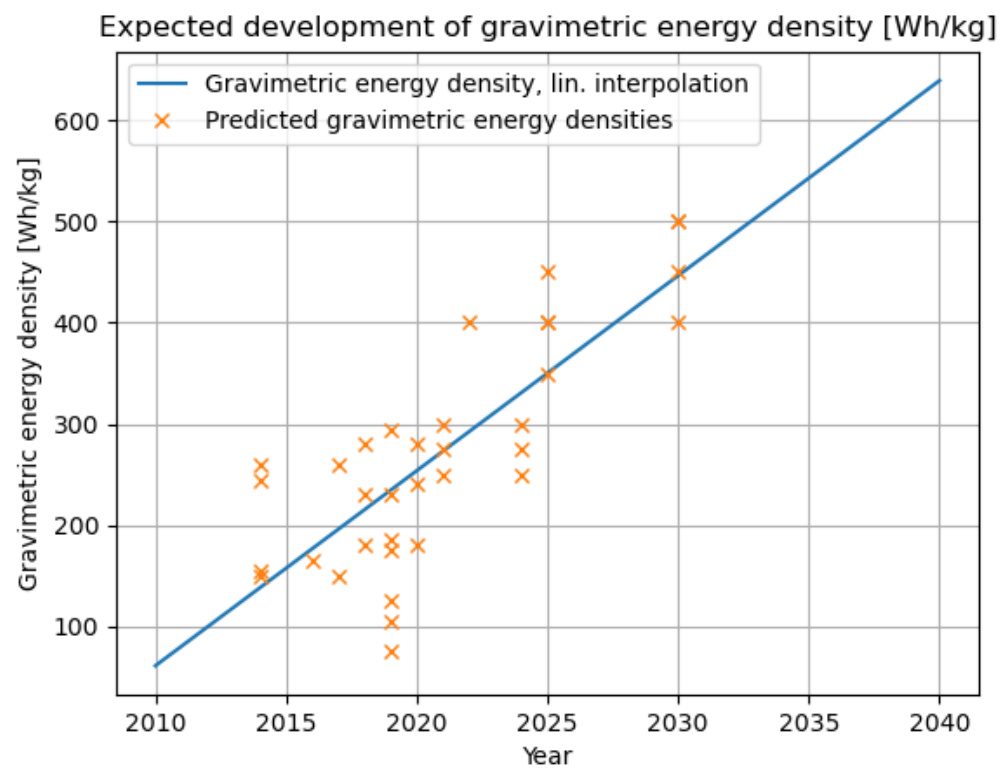
Battery gravimetric density

- Future performance predictions
 - Wide range of literature
 - Range of applications for more robust results
- Time-based regression over datapoints
 - Linear interpolation for mean
 - Normal distribution for credibility





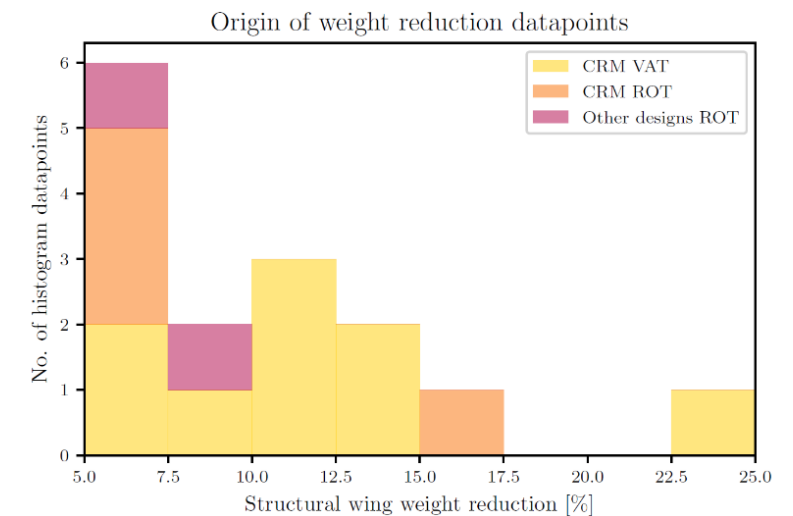
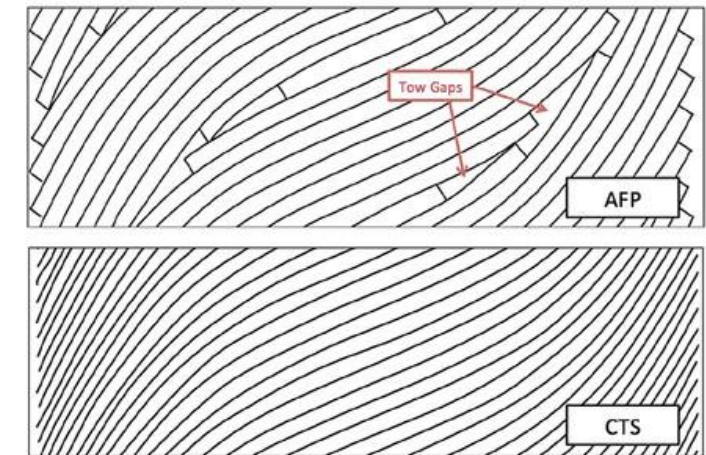
Battery gravimetric density





Structural weight reductions

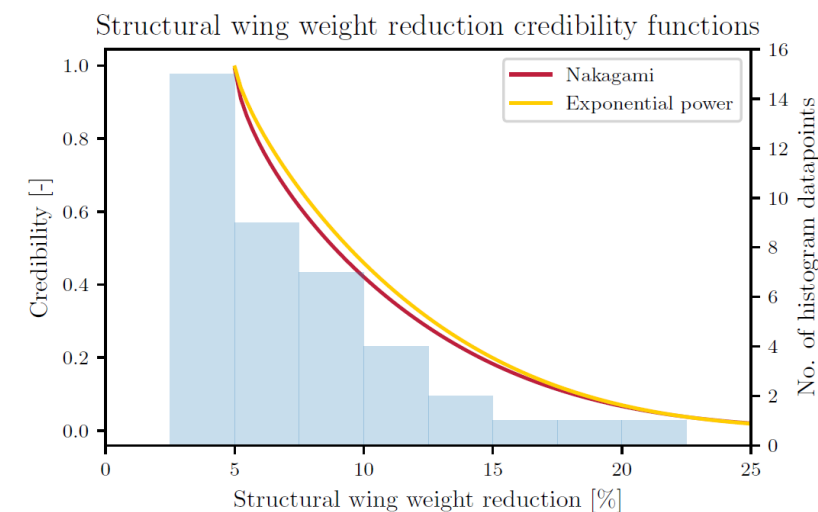
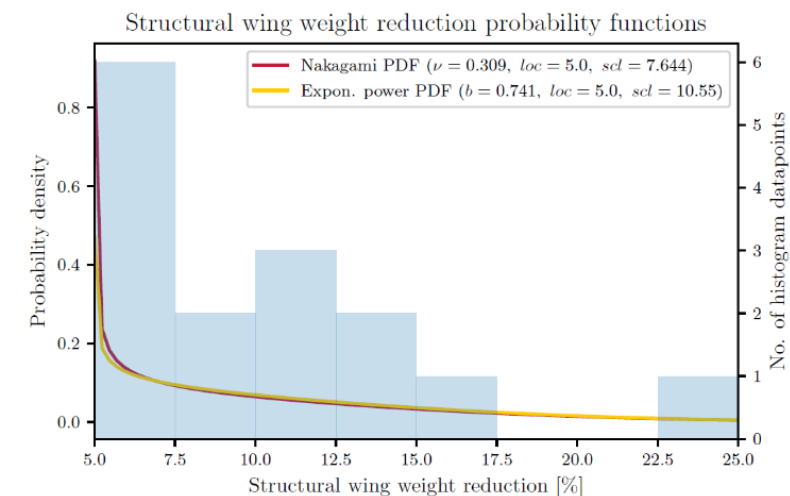
- Future optimisation in CFRP lay-up methods
- Better tailoring to required loads and stiffness
 - Ply rotation
 - Variable angle tow steering (1D & 2D)
- High-fidelity simulations and optimisations
 - NASA CRM wing design (AR-9 and AR-13.5)
 - Other wing applications (FEM)





Curve fitting to credibility

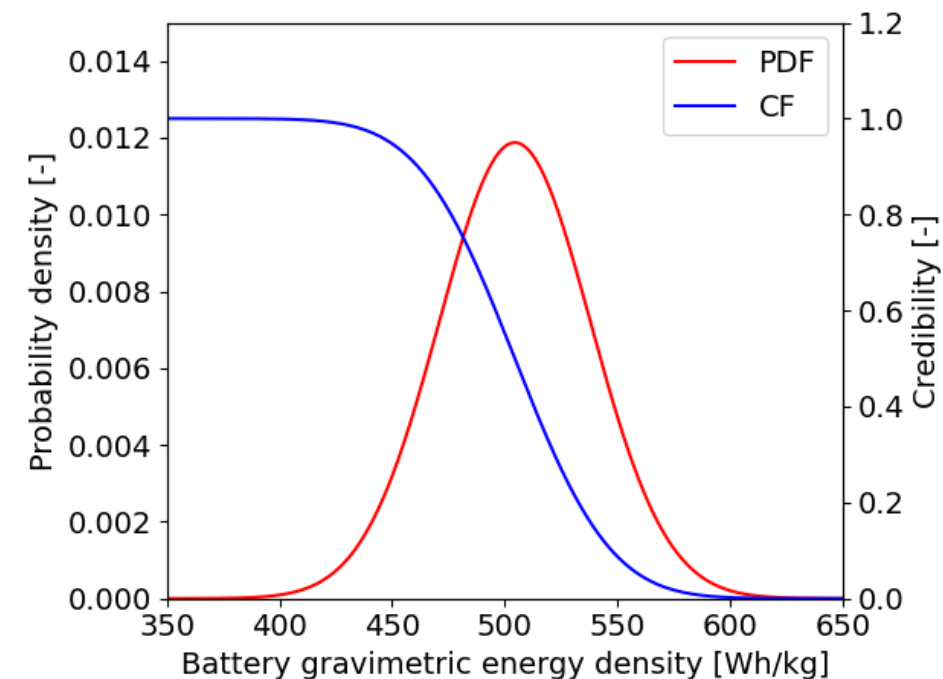
- Fitting of best distribution with Kolmogorov-Smirnov test
 - Suitable due to scarcity of data
- Exponential functions best fit
- Sensible starting point and distribution
 - Small reductions still possible with optimisation of current methods





Uncertain variables

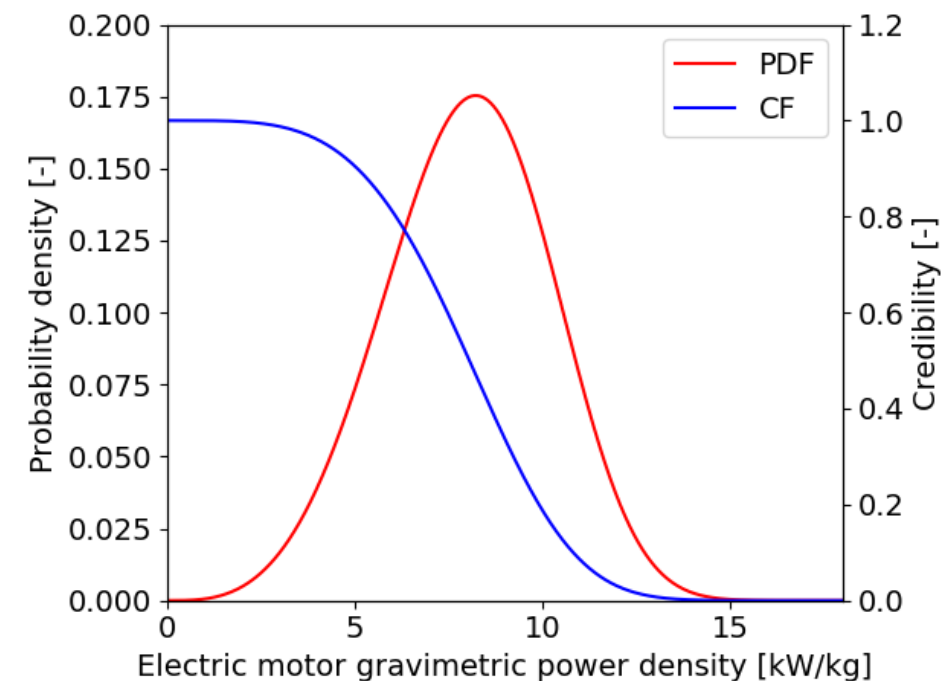
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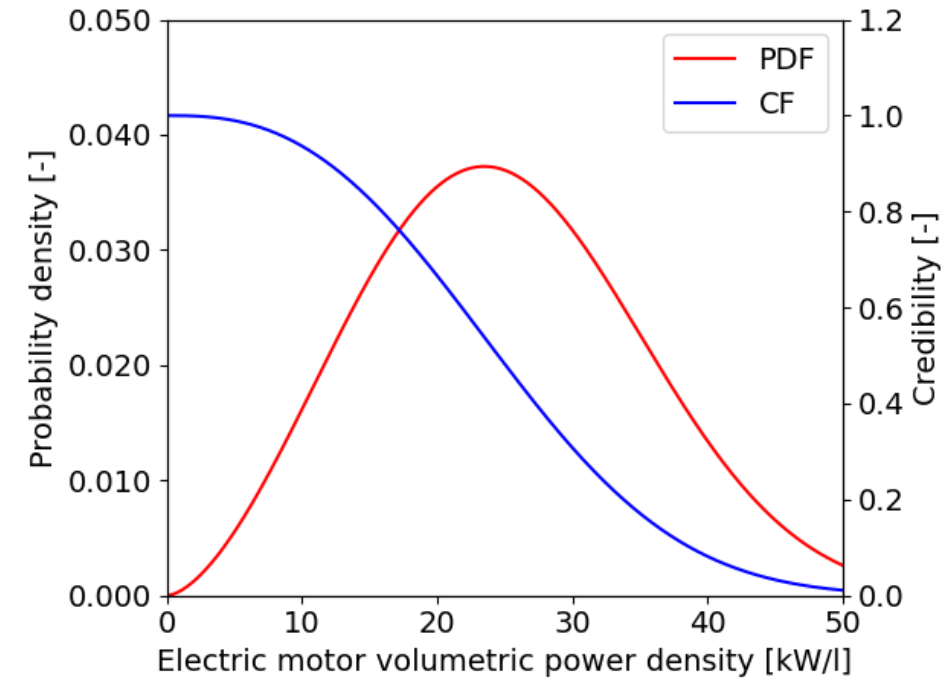
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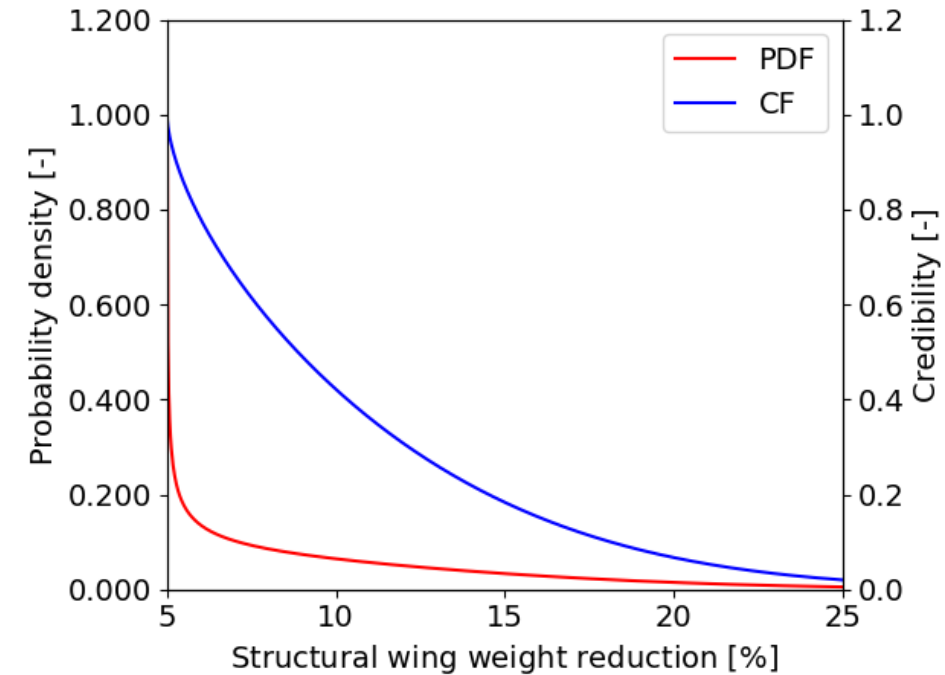
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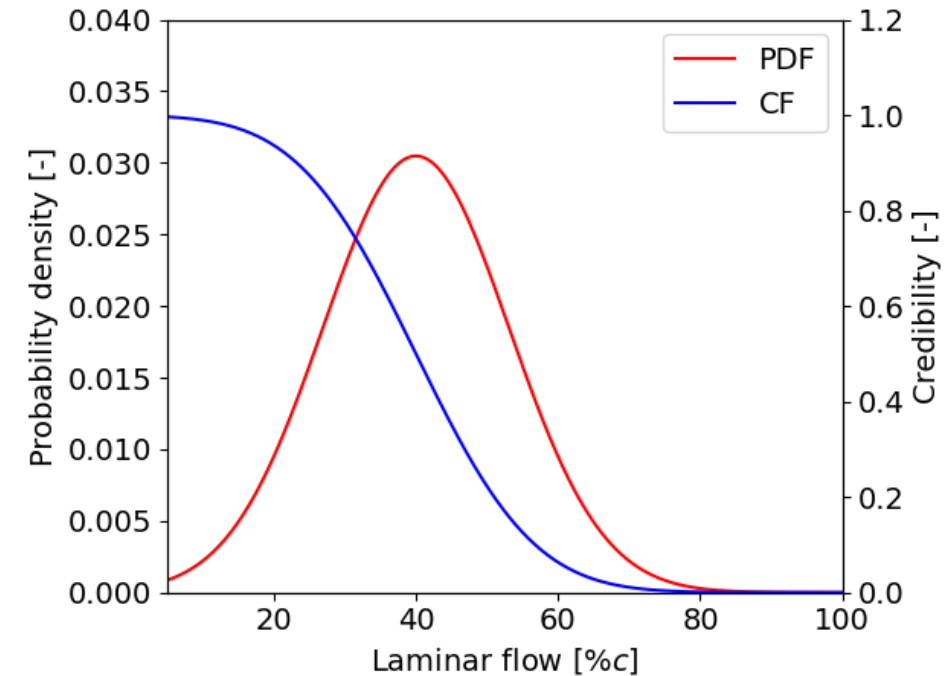
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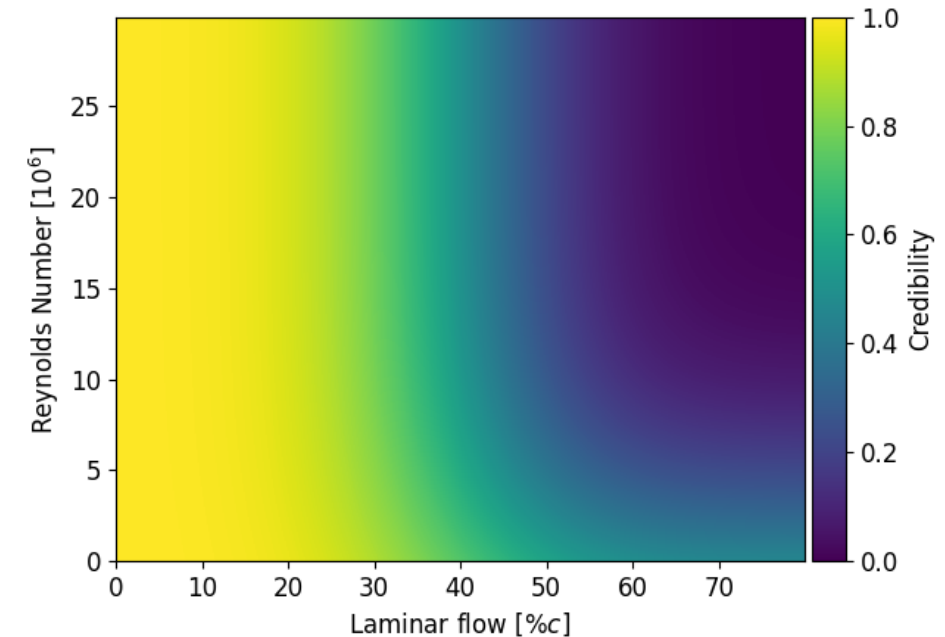
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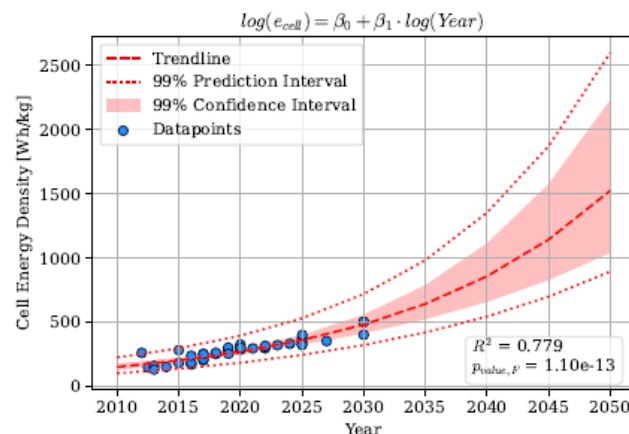
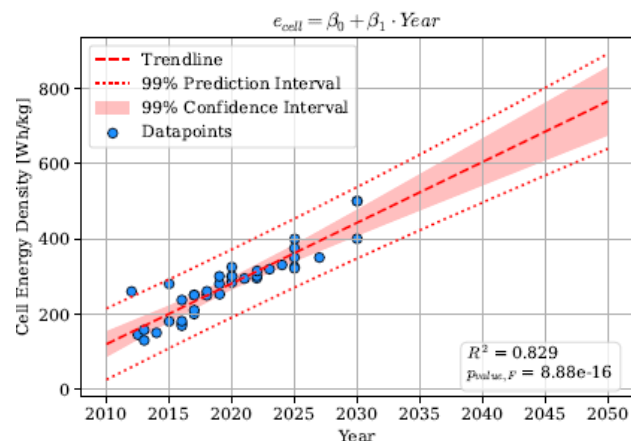
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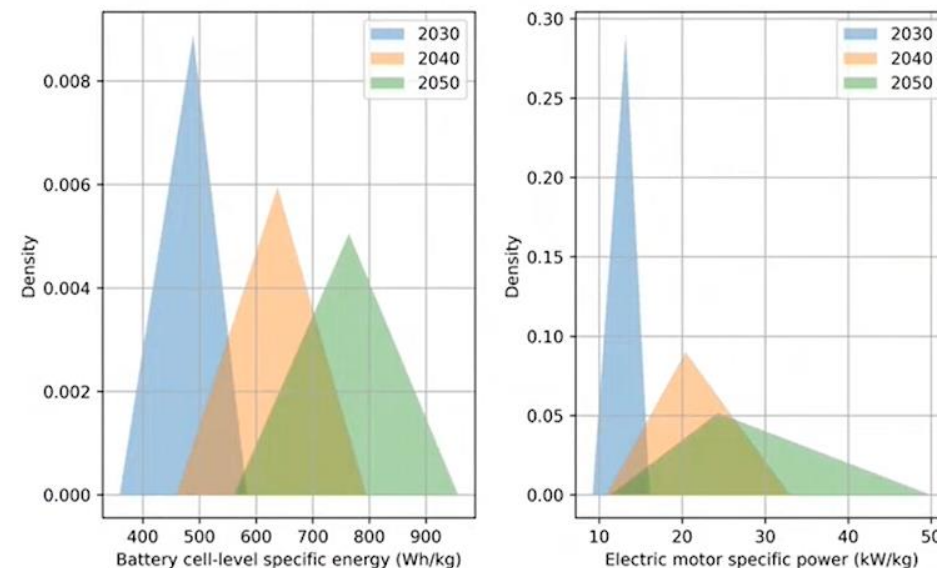


Verification with other literature

- Expected values 2035
 - Battery: 504 Wh/kg
 - Motor: 10.1 kW/kg



Spinelli, A., Krupa, G. P., & Kipourou, T. (2023). Set-Based Design Space Exploration to Investigate the Effect of Energy Storage Durability on the Energy Management Strategy of a Hybrid-Electric Aircraft. In *AIAA SCITECH 2023 Forum* (p. 0837).



Uzodinma, J., Zaidi, T., Walter, M., Gautier, R., & Mavris, D. N. (2023). Uncertainty Quantification on a Parallel Hybrid-Electric Propulsion EPFD Vehicle. In *AIAA SCITECH 2023 Forum* (p. 0839).



Optimisation procedure

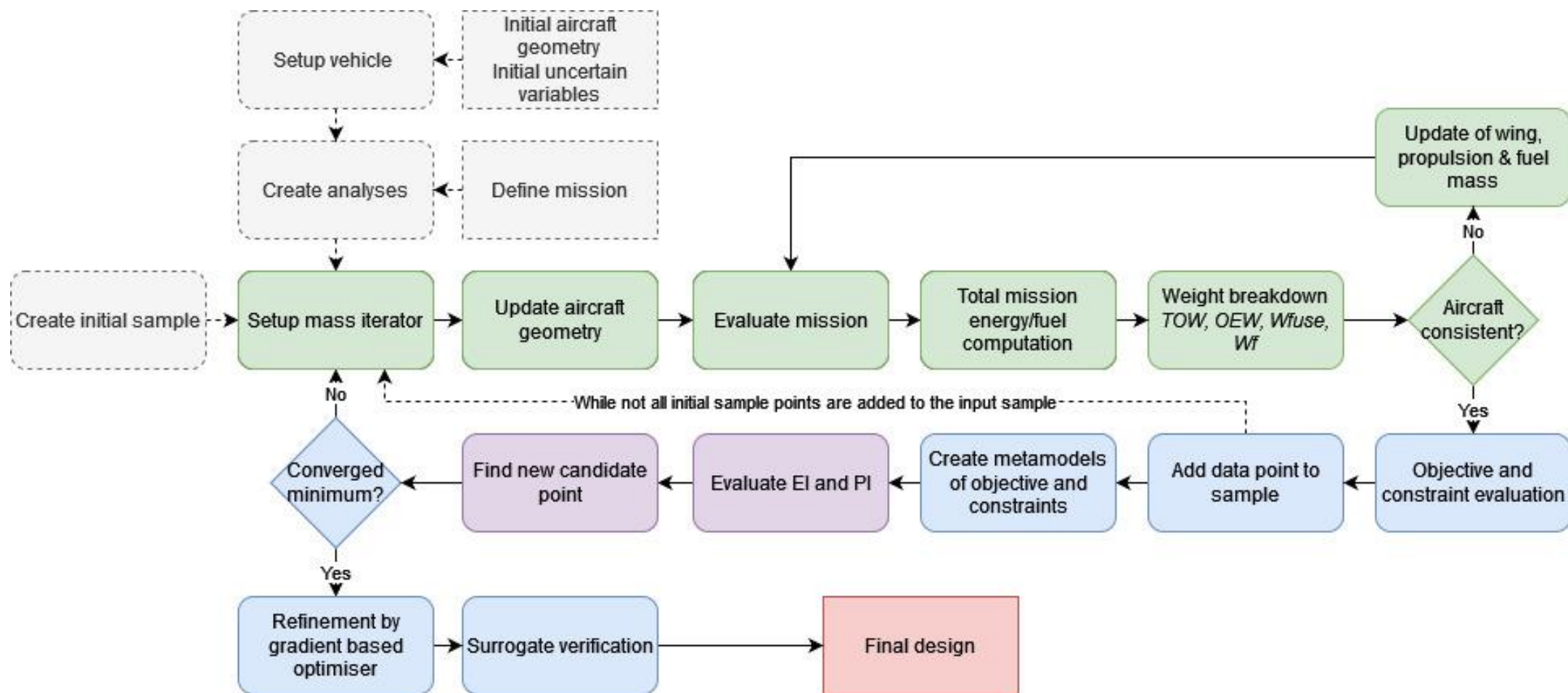


Credibility-based MDO

- In combination with an 'optimised' aircraft
 - Stage 2 of the design process
- Used to further explore potential and scalability vs. acceptable risk
- Sensitivity study for the given aircraft



Optimisation framework





Optimisation formulation

- Maximum mission range
- Uncertain parameter as inputs
- Credibility constraints
 - Per parameter
 - Average
- Fixed design point

$$\begin{array}{ll}
 \min & -R \\
 \text{s.t.} & C_i \geq C_{i,l} \quad \forall i = 1, \dots, n \\
 & \frac{1}{n} \sum C_i \geq \frac{1}{n} \sum C_{i,l} \\
 & \text{or} \\
 & MTOM \leq MTOM_l \\
 & b \leq b_l
 \end{array}$$

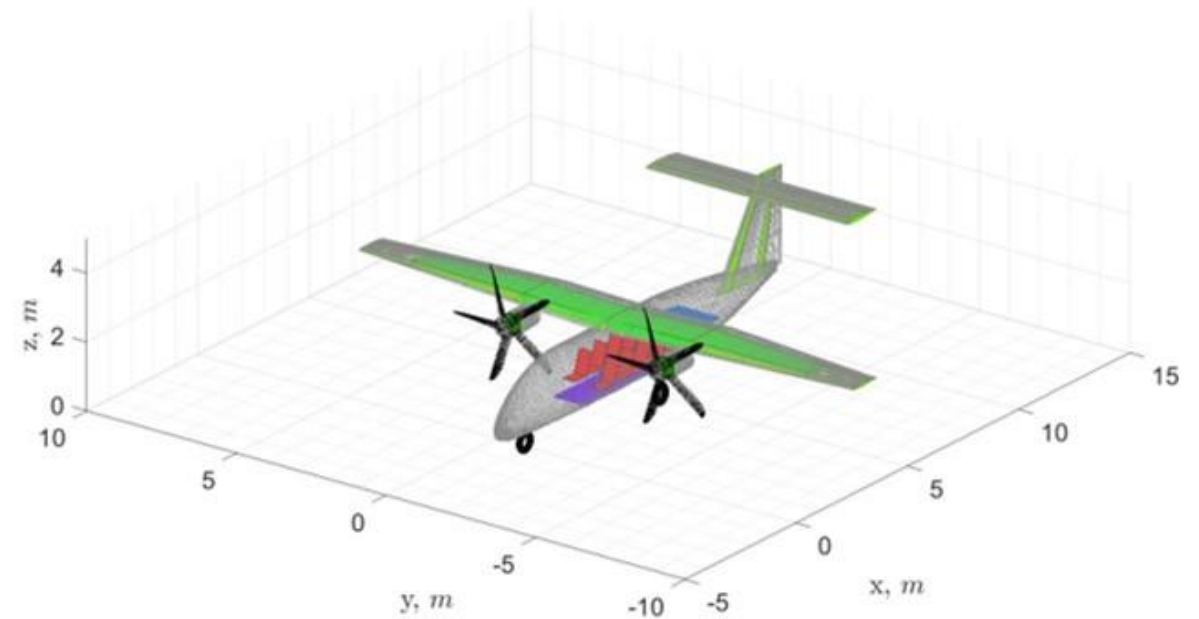


Results



Commuter case

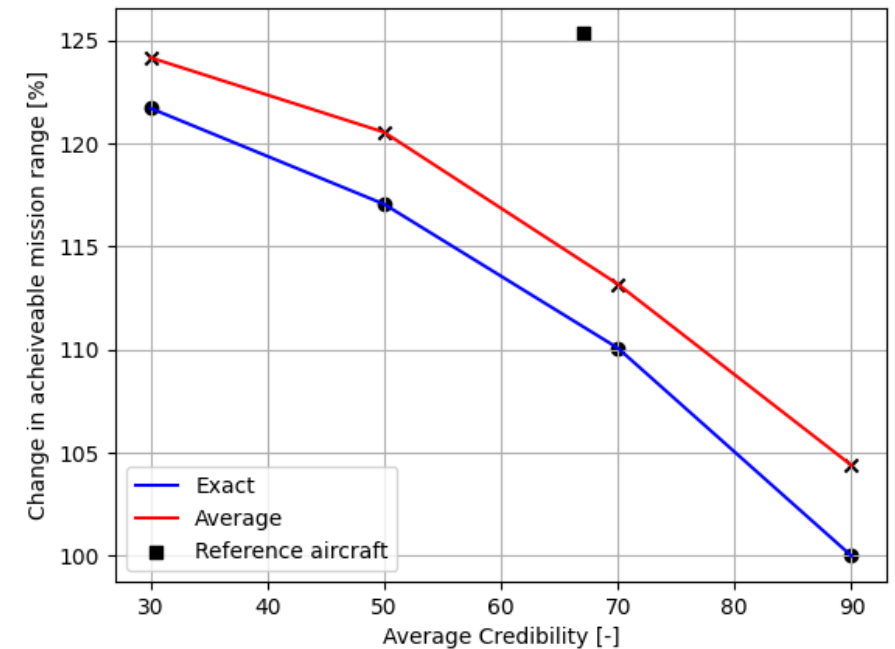
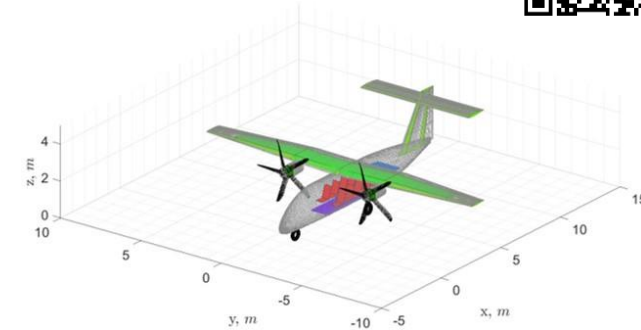
- EASA CS-23 commuter
 - 10 Passengers
 - Fully electric architecture
- Optimised for range
 - MTOM < 8618 kg (19,000lbs)
 - No reserve mission
- 19 Passenger concept in the future





Credibility-based optimisation

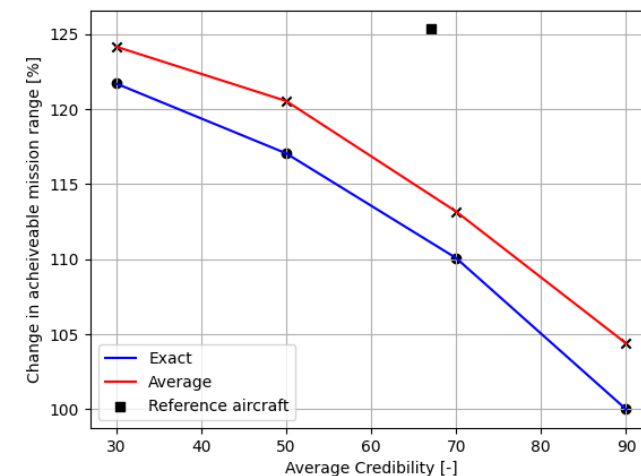
- Exact
 - Defined Credibility level
 - Only range is maximised
- Average
 - Component Credibility up to 10% less
 - Range and parameters optimized





Aircraft comparison – All parameters

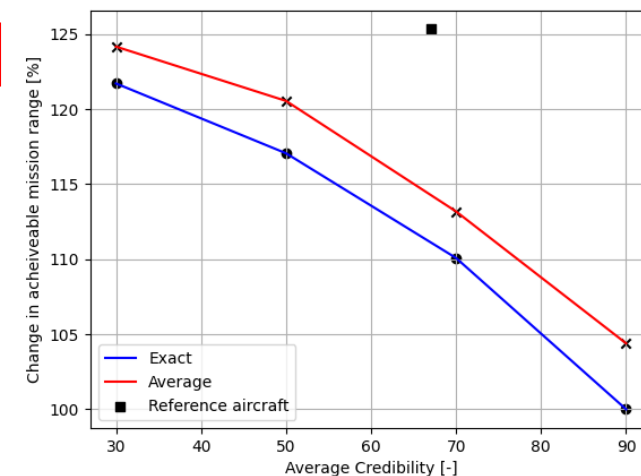
Parameter	Reference	30% Cred	50% Cred	70% Cred	90% Cred
MTOM [kg]	8694	8620	8618	8612	8619
Wing [kg]	1087	722	768	807	826
Motor [kg]	313	117	121	121	131
Battery [kg]	2526	2908	2883	2858	2829
Area of Laminar Flow [%]	0 (100%)	67 (20%)	45 (60%)	31 (84%)	10 (98%)
Structural Wing Weight Red. [%]	0 (100%)	14.5 (20%)	10.4 (40%)	6.8 (68%)	5.1 (94%)
Battery Grav. Energy Density [Wh/kg]	643.5 (0.0017%)	530 (22%)	513 (40%)	496 (60%)	476 (80%)
Motor Grav. Power Density [kW/kg]	3.4 (99.7%)	9.0 (68%)	8.7 (72%)	8.7 (72%)	8.0 (80%)
Motor Vol. Power Density [kW/l]	4.4 (99.8%)	35.6 (20%)	32.5 (40%)	23.9 (70%)	10.6 (97%)





Aircraft comparison – All parameters

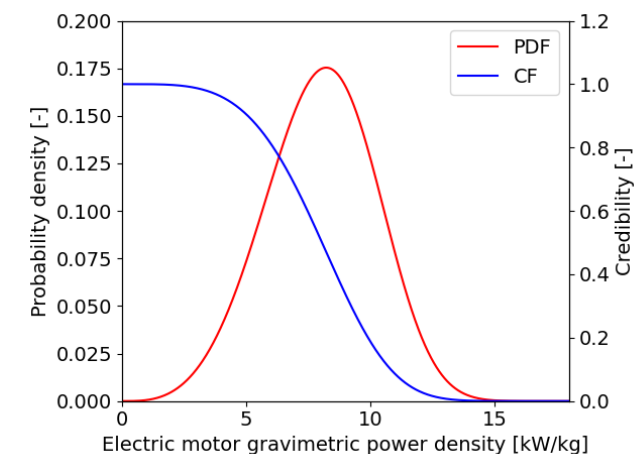
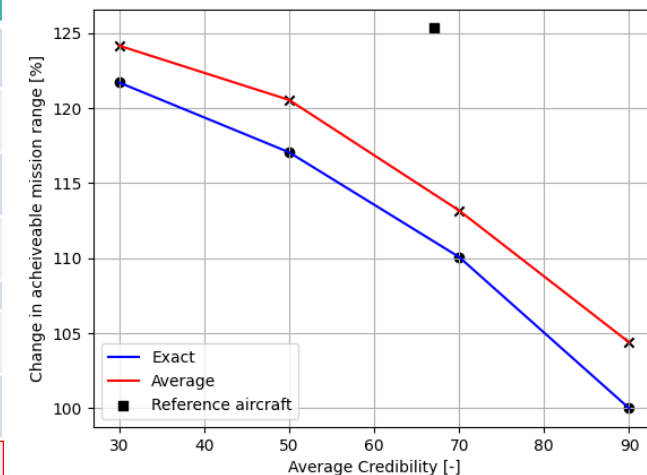
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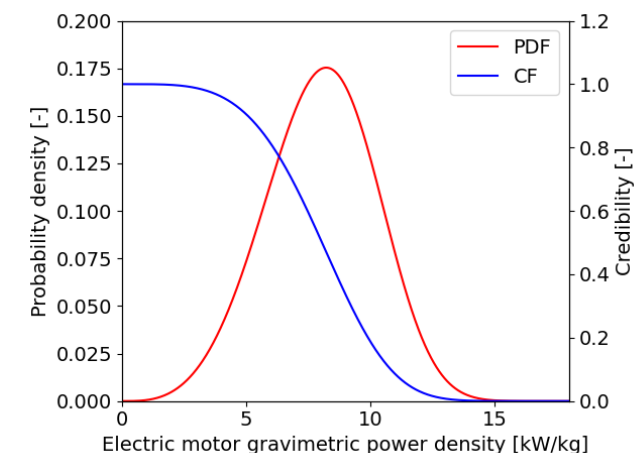
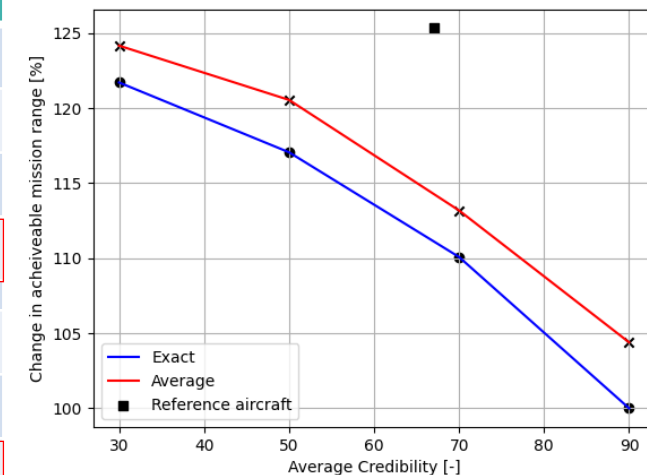
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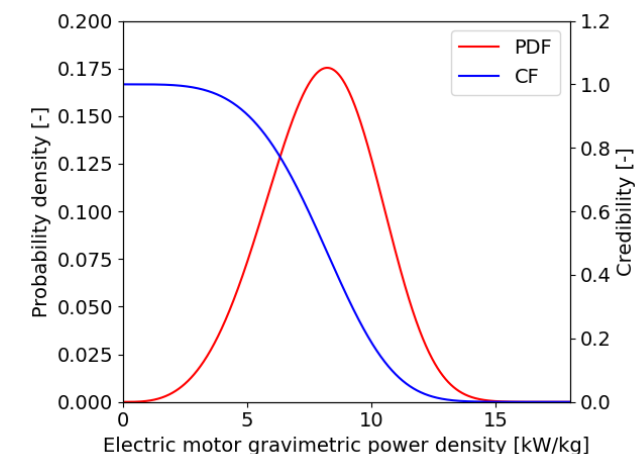
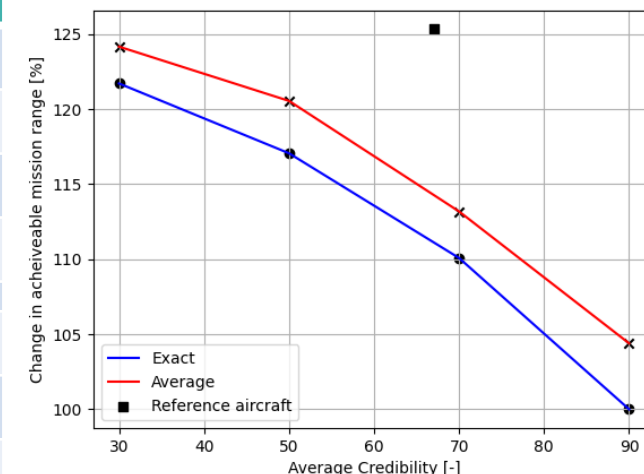
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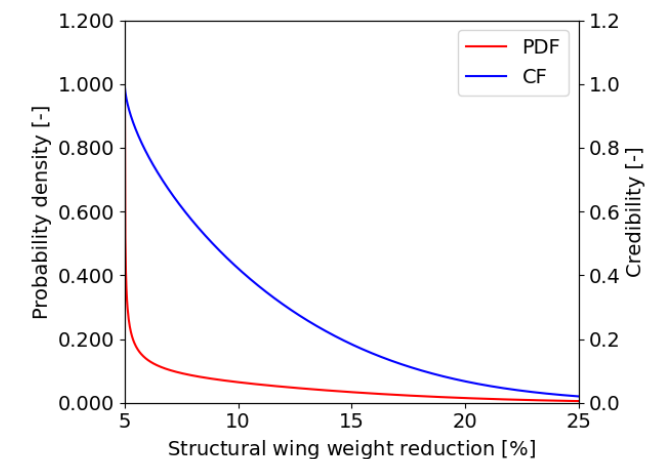
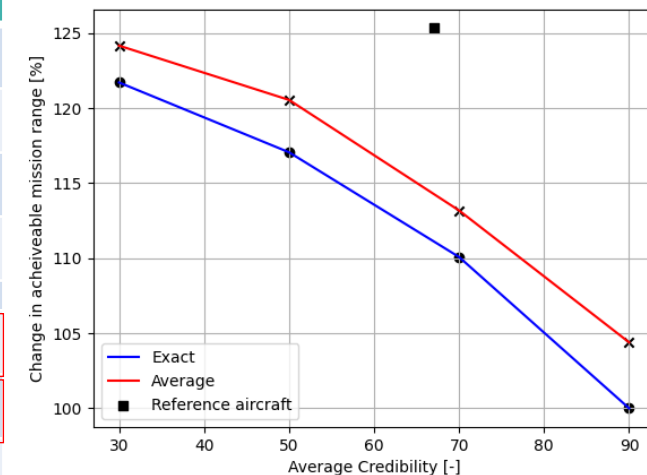
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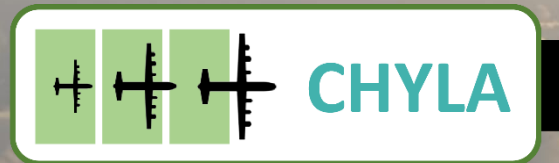
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Thank you for your attention

CREDIBILITY-BASED MDO RESULTS



CREDIBLE HYBRID ELECTRIC AIRCRAFT

