

# *Positron Annihilation techniques for material defect studies*

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November 26, 2013

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## The positron

Prediction by Dirac (1930)

theory of relativity and quantum mechanics

$$E = \pm (p^2c^2 + m_0^2c^4)^{1/2}$$

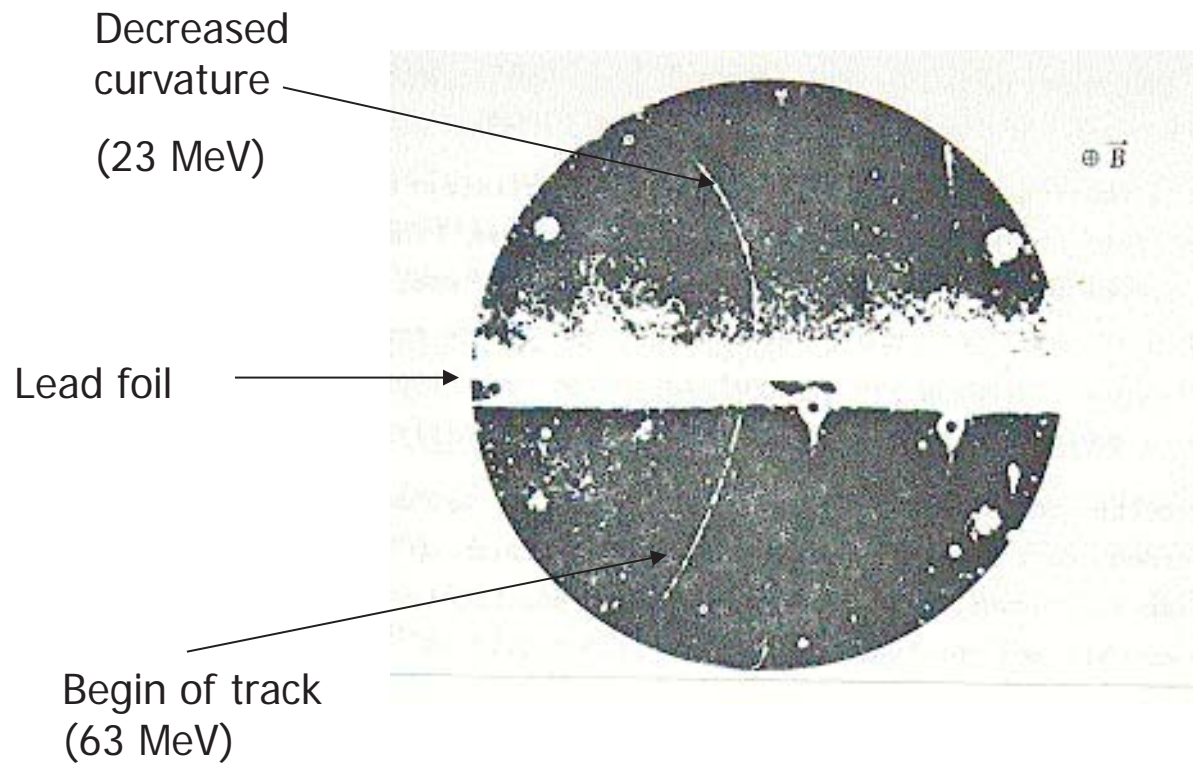


P.A.M.  
Dirac

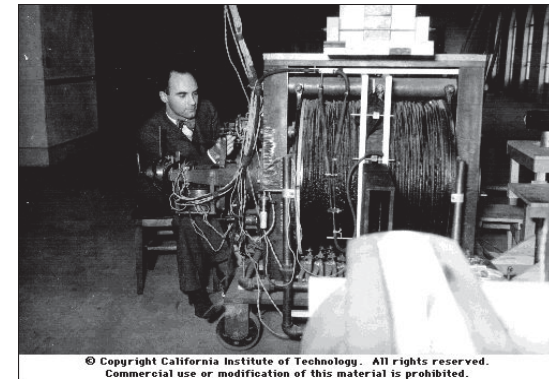
“Hole Theory” these solutions are interpreted as electrons with negative energy

Positron discovery: the first pictures

"Picture" of a positron in the cloud chamber (1932)



C.D. Anderson



## More recent positron-electron tracks

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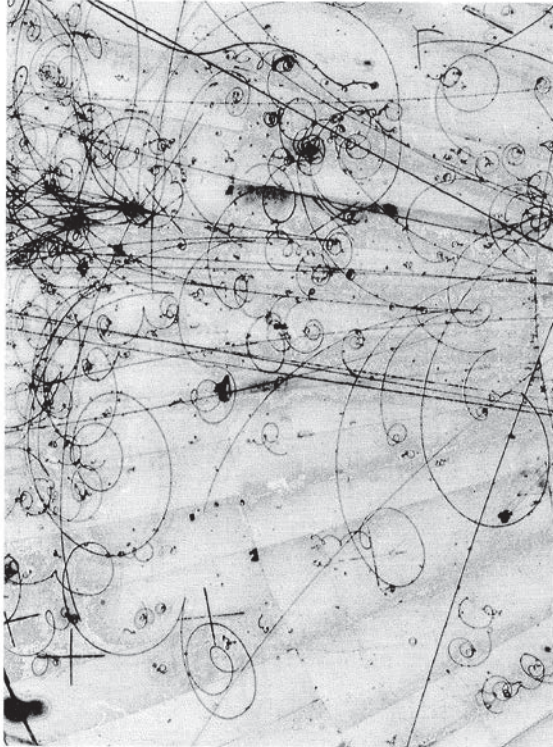
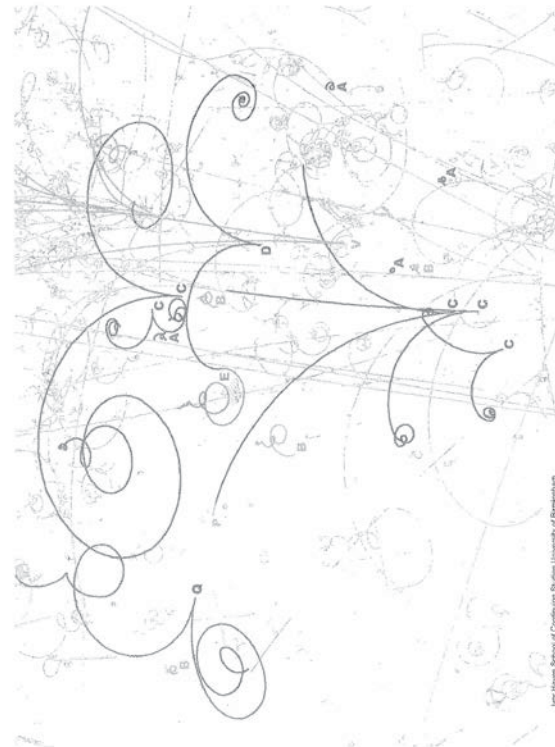


Figure 1. Part of a bubble chamber picture. The dark lines are trails of tiny bubbles created as charged particles force their way through a tank of transparent liquid enclosed in a powerful magnet. At P, the main point of interest, a positron (antielectron) in flight meets an electron and annihilation takes place. One of the photons from the annihilation materializes at Q. At E, a different positron seems to change

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its sign. What has happened is that it has collided head-on with a stationary electron and has transferred all (within errors) its momentum to the electron. This shows that (within errors) the positron has the same mass as the electron. (This picture, from experiment E632 performed at the Fermilab 15 ft (4.6 m) bubble chamber, was found at the University of Birmingham. Graphics by Ivor Hayes.)

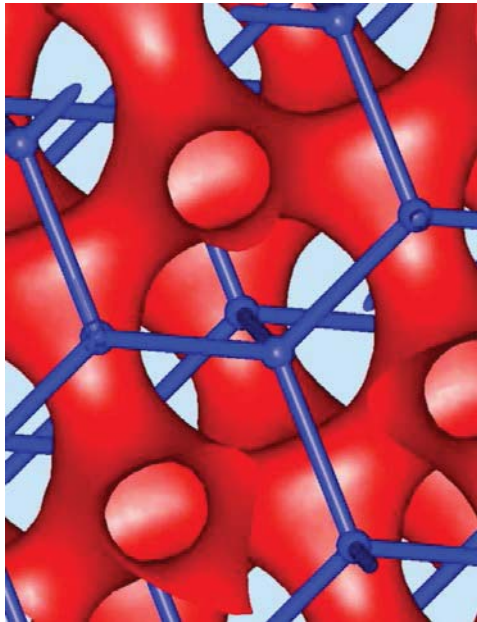
Phys. Educ. 34(5) September 1995 279

From: Phys. Edu 34(5) september 1995, G.T. Jones

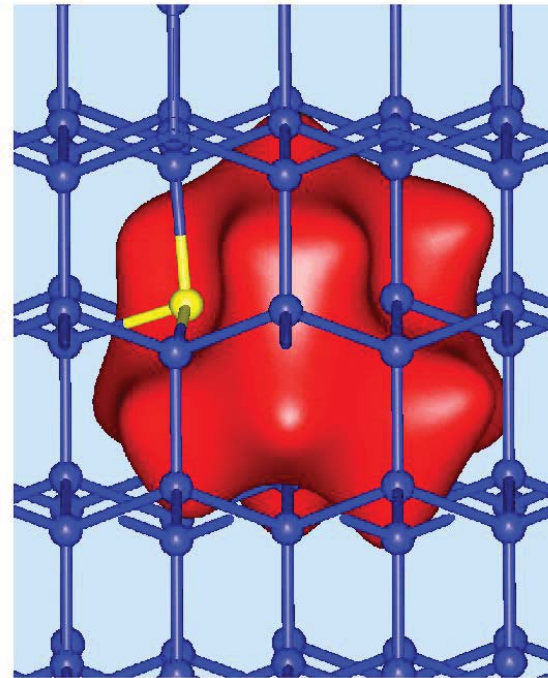
Recent “picture” of a positron as iso-surface of the positron wave function

Seitsonen, Puska and Nieminen (Helsinki University of Technology, 1995)

*Si*



*Si vacancy + Sb neighboring atom*

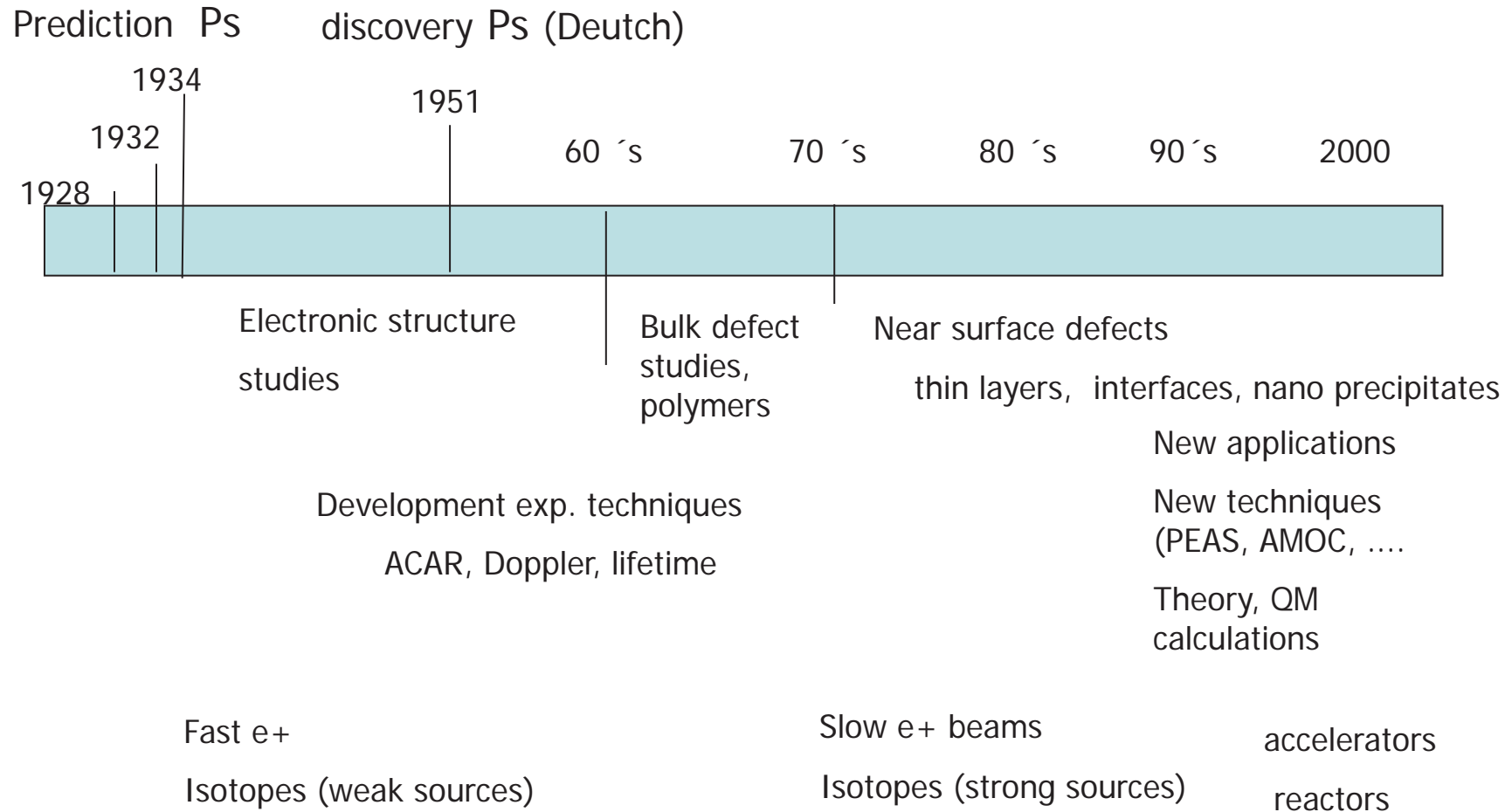


November 26, 2013 *Free positron*

*Trapped positron*

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# Positron annihilation history



## *Positron annihilation (the Science Fiction approach )*



The comic "Barbarella"  
Jean Claude Forest 1964



Positron gun !

The movie "Barbarella"  
Jane Fonda; Roger Vadim 1968

Antimatter + Matter → complete destruction



## Characteristics of the positron as the anti-particle of the electron

	<i>positron</i>		<i>electron</i>
<i>Rest Mass</i>		$9.109 \cdot 10^{-31} \text{ kg}$	
<i>Charge</i>	$+$	$1.60219 \cdot 10^{-19} \text{ C}$	$-$
<i>Spin</i>	$\frac{1}{2}$	<i>lepton</i>	$\frac{1}{2}$
<i>Magnetic moment</i>	$+$	$g \cdot q / 2m \cdot S$ ( $g = 2.002319$ )	$-$
<i>Classic radius</i>		$2.81794 \cdot 10^{-15} \text{ m}$	
<i>Lifetime</i>	<i>stable (in vacuum)</i> $t > 2 \times 10^{21} \text{ year}$		<i>stable</i>

$$E = mc^2 \rightarrow \text{rest mass} = 511.0034 \text{ keV} / c^2 \quad (1 \text{ Joule} = 1/q \text{ eV})$$



## Positron Annihilation

*Process of transforming mass into photons*



*General Conservation laws:*

- *energy*
- *linear momentum*
- *electric charge*
- *angular momentum*
- *parity*

*most probable: two photon*

Hence the study of the annihilation quanta will give information about the state of the annihilation positron electron pair *immediately before* the transition !

*Annihilation cross section for two photon annihilation  
in the low velocity limit (free particles)*

$$\sigma_{2\gamma} = \pi r_0^2 c / v$$

*With  $r_0$  the classical Bohr radius of the electron (positron)  
~  $10^{-15}$  m*

*The other annihilation rates (1 , 3 photons ) scale with the fine  
structure constant  $\alpha^4$  and  $\alpha$  , respectively*

$$\alpha = e^2 / \hbar c 4\pi\epsilon_0 = 1/137$$

### Case 1) zero momentum

both particles at rest (in lab system) or observation in the center of mass system

*Before annihilation:*

*After Annihilation*

*Total energy*

$$E = E_{\text{electron}} + E_{\text{positron}} = 2 m_0 c^2 \longrightarrow E_{y1} + E_{y2} \quad (1)$$

*Total momentum*

$$p = 0 \longrightarrow E_{y1} / c + E_{y2} / c \quad (2)$$

*(as components of p vector)*

- two photons emitted in opposite directions
- energy of each photon =  $\underline{m_0 c^2} = 511 \text{ keV}$

Case 2 : electron momentum  $p = p_x$

*Before annihilation:*

*After Annihilation*

Total energy  $E = E_{\text{electron}} + E_{\text{positron}}$   
 $= (m_0^2 c^4 + p_x^2 c^2)^{1/2} + m_0 c^2 \longrightarrow = E_{y1} + E_{y2} \quad (1)$

Total momentum  $p = p_x \longrightarrow = E_{y1}/c + E_{y2}/c$   
 $p_y = p_z = 0 \quad = p_y = p_z \quad (2)$

*in case gamma's emitted in the direction of p*

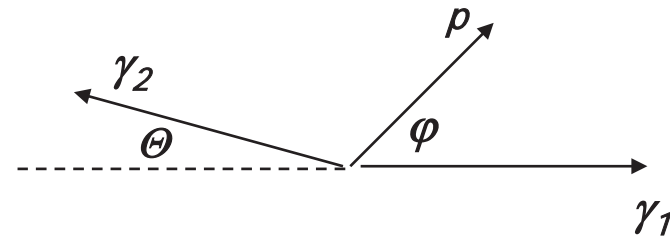
- *two photons emitted in opposite directions*
- *energy of the photons =  $m_0 c^2 \pm c p_x / 2$  (doppler broadening)*

*General solution*

$$\Theta_{\gamma_1-\gamma_2} = \frac{2pc \sin(\phi)}{pc \cos(\phi) + m_0c^2 + \sqrt{m_0^2c^4 + p^2c^2}}$$

$$E_{\gamma_1} = \frac{m_0c^2 + \sqrt{m_0^2c^4 + p^2c^2} + pc \cos(\phi)}{2}$$

$$E_{\gamma_2} = \frac{m_0c^2 + \sqrt{m_0^2c^4 + p^2c^2} - pc \cos(\phi)}{2}$$



*Approximation:*

$$E = m_0 c^2 \pm \frac{1}{2} p_{\parallel} c \text{ keV}$$
$$\Theta_{y-y} = \pi - p_{\perp} / m c \text{ radians}$$

*Some values :*

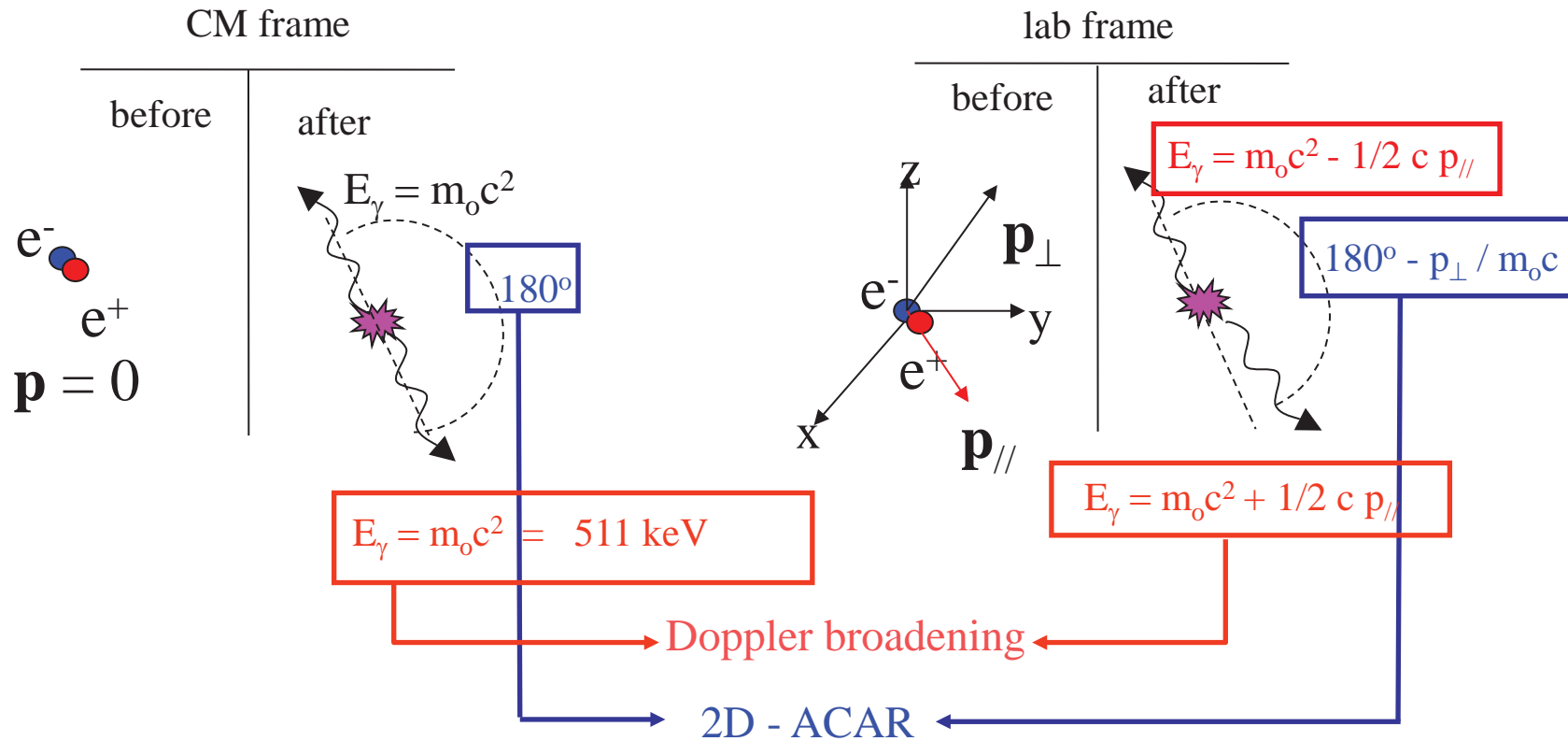
*Energy of electrons (in solids) 10 eV  $\rightarrow \frac{1}{2} p_{\parallel} c = 1.5 \times 10^3 \text{ eV}$   
(compare to  $511 \times 10^3 \text{ eV}$ )*

*p of the order of  $1 \times 10^{-24} \text{ m kg/s}$   $\rightarrow p_{\perp} / mc = 3 \text{ mrad}$  (3 mm at 1 m)*

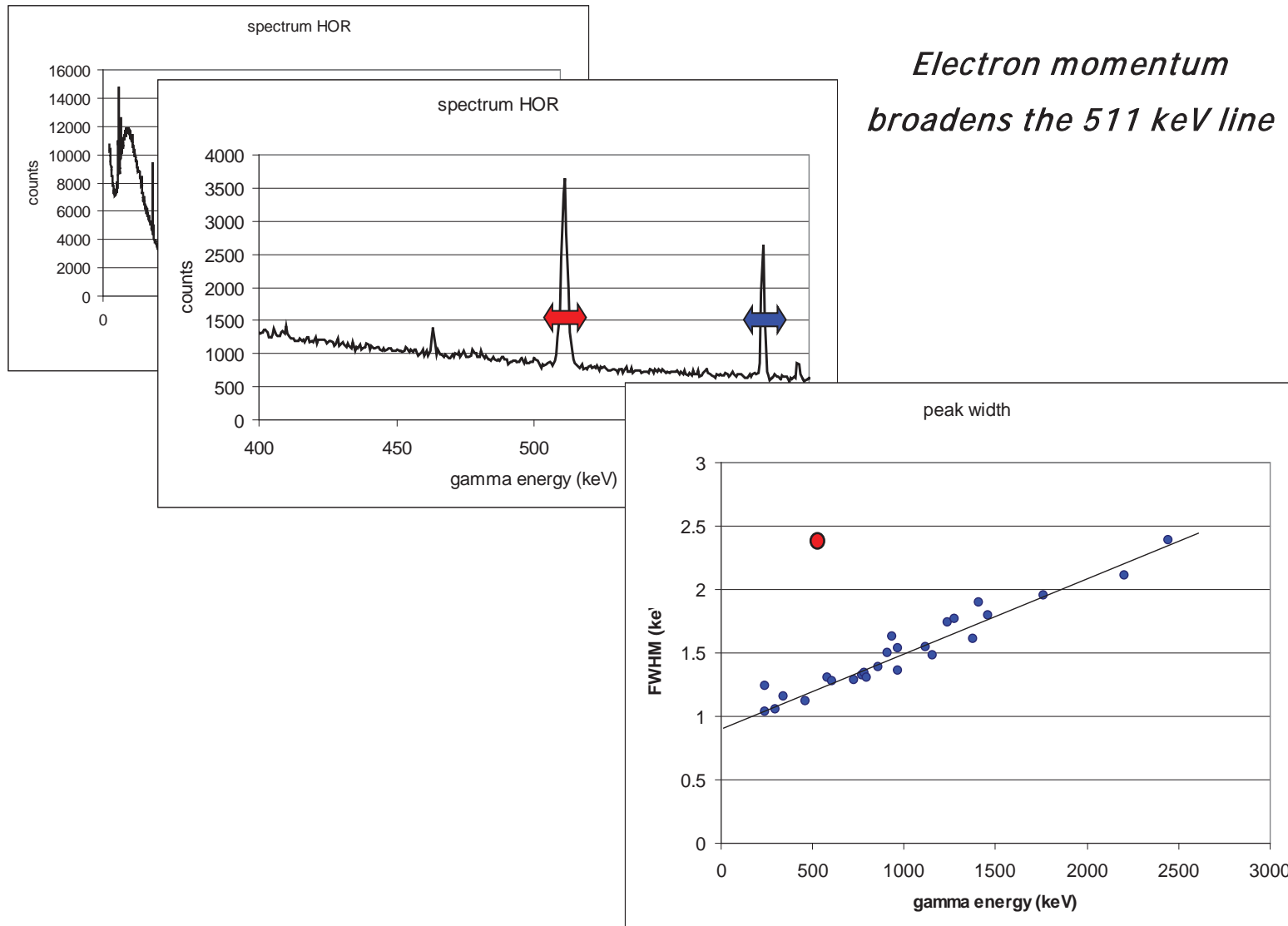
# The effect of conservation of momentum and energy

2  $\gamma$   $e^+ + e^-$  annihilation process :

conservation of energy and momentum



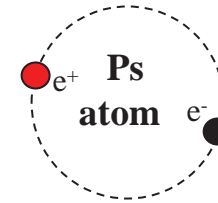
*Electron momentum  
broadens the 511 keV line*





## *Positronium:*

*An electron - positron bound state*



<u><i>H atom</i></u>	<u><i>physical property</i></u>	<u><i>Ps atom</i></u>
1.0080	atomic mass (amu)	0.00110
0.99956	reduced mass	$\frac{1}{2}$
1 $a_0$ (radius)	size	2 $a_0$ (diameter)
13.598 eV	ionization energy	6.803 eV
J = 0 (para)	spin states	S = 0 (para) $\uparrow\downarrow$
J = 1 (ortho)		S = 1 (ortho) $\uparrow\uparrow$
$\infty$	life time	125 ps ( 125 x 10 <sup>-12</sup> s, para) 142 ns (142 x 10 <sup>-9</sup> s , ortho)

Positronium annihilation modes:

Para Ps  $\uparrow\downarrow$  "self" annihilates by two-gamma emission (125 ps)

Ortho Ps  $\uparrow\uparrow$  "self" annihilates by three-gamma emission (142 ns)

*or in media:*

o- Ps ( $\uparrow\uparrow$ ) + e<sup>-</sup> ( $\downarrow$ )  $\rightarrow$  p-Ps ( $\uparrow\downarrow$ ) + e<sup>-</sup> ( $\uparrow$ ) (spin exchange)

o- Ps ( $\uparrow\uparrow$ ) + e<sup>-</sup> ( $\downarrow$ )  $\rightarrow$  2 gamma  $\gamma$ 's + e<sup>-</sup> ( $\uparrow$ ) (pick off)

*Para -Ps has zero internal momentum therefore  $E_\gamma \sim 511$  keV  
(only translational momentum of the atom)*

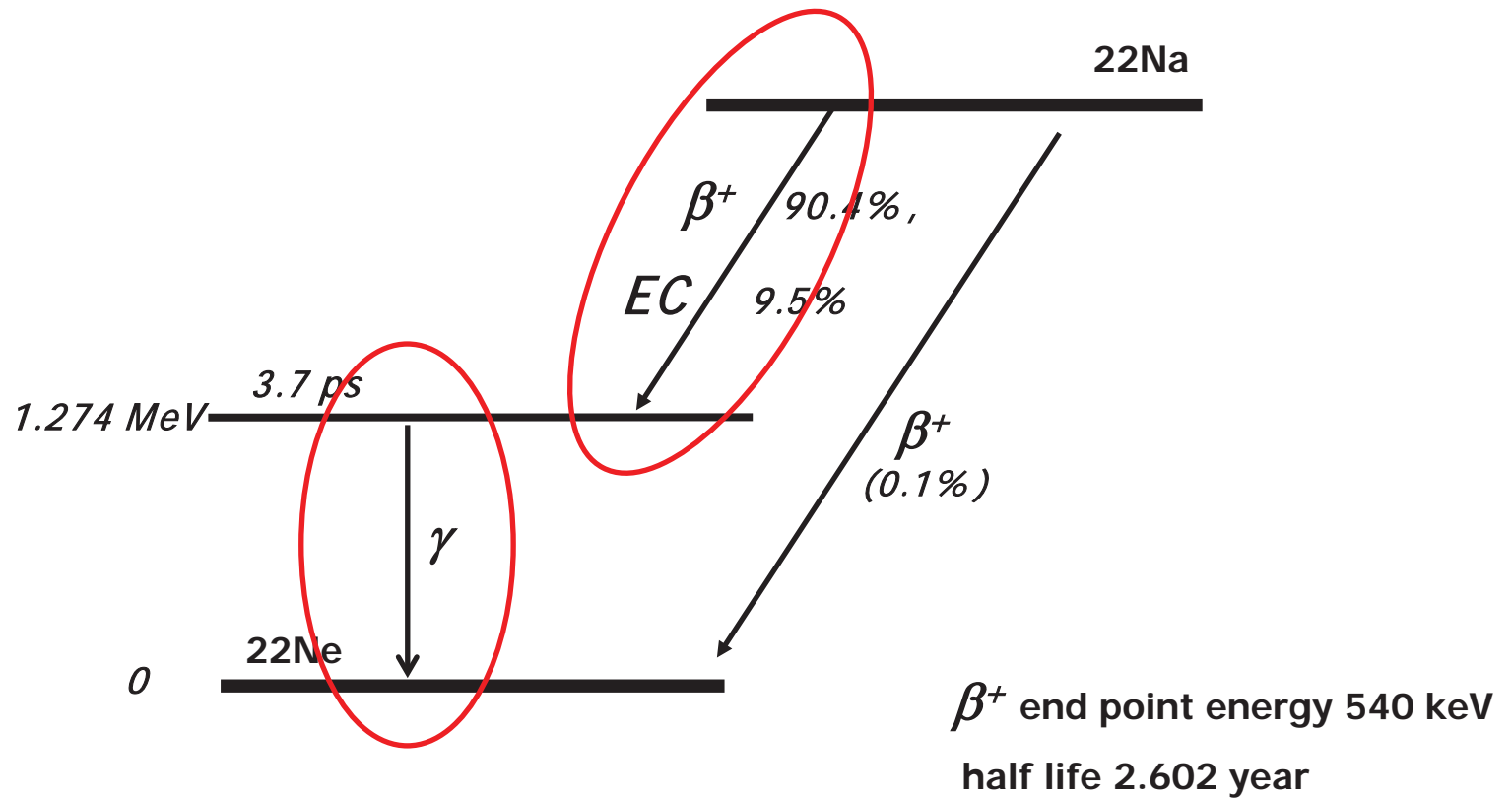
## *Positron sources*

- *Isotopes*
  - *nuclear reactions*
  - *neutron absorption*
- *Pair production*
  - *Electron accelerators*
  - *Fission reactors*
    - *neutron  $\rightarrow$  gamma conversion*
    - *prompt gammas*

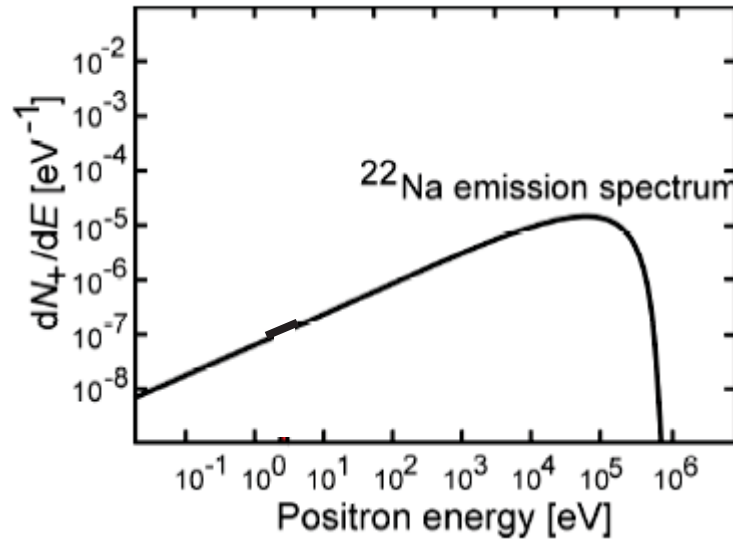
Examples of positron emitters

<i>Isotope</i>	<i>half life</i>	<i>% e+</i>	<i>production</i>	<i>application</i>
$^{11}\text{C}$	20 min	100	$^{11}\text{B}(p,n)^{11}\text{C}$ $^{10}\text{B}(d,n)^{11}\text{C}$ $^{14}\text{N}(p, \alpha)^{11}\text{C}$	medical diagnostics (PET)
$^{13}\text{N}$	10 min	100	$^{12}\text{C}(d,n)^{13}\text{N}$ $^{16}\text{O}(p, \alpha)^{13}\text{N}$	"
$^{15}\text{O}$	2 min	99	$^{14}\text{N}(d,n)^{15}\text{O}$	"
$^{18}\text{F}$	110 min	97	$^{18}\text{O}(p,n)^{18}\text{F}$	"
$^{22}\text{Na}$	2.6 y	90	$^{24}\text{Mg}(d,\alpha)^{22}\text{Na}$	PA accelerators
$^{58}\text{Co}$	71.3 d	15.5	$^{58}\text{Ni}(n,p)^{58}\text{Co}$	" nucl reactors
$^{64}\text{Cu}$	12.9 h	19.3	$^{63}\text{Cu}(n,\gamma)^{64}\text{Cu}$	" nucl reactors

## *<sup>22</sup>Na decay scheme*

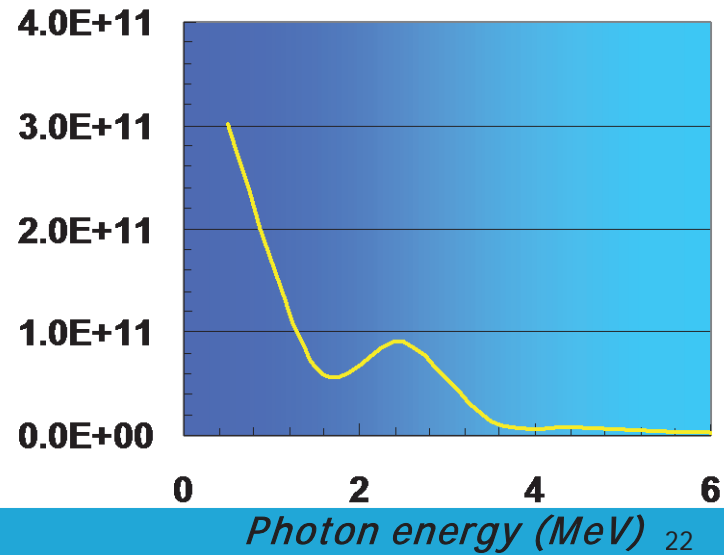


*Positron kinetic energy distribution*



(1274 keV  $^{22}\text{Ne}^*$ )

*HOR gamma flux distribution*



*Pair production:*

*positron kinetic energy depends on the initial energy of the photon*

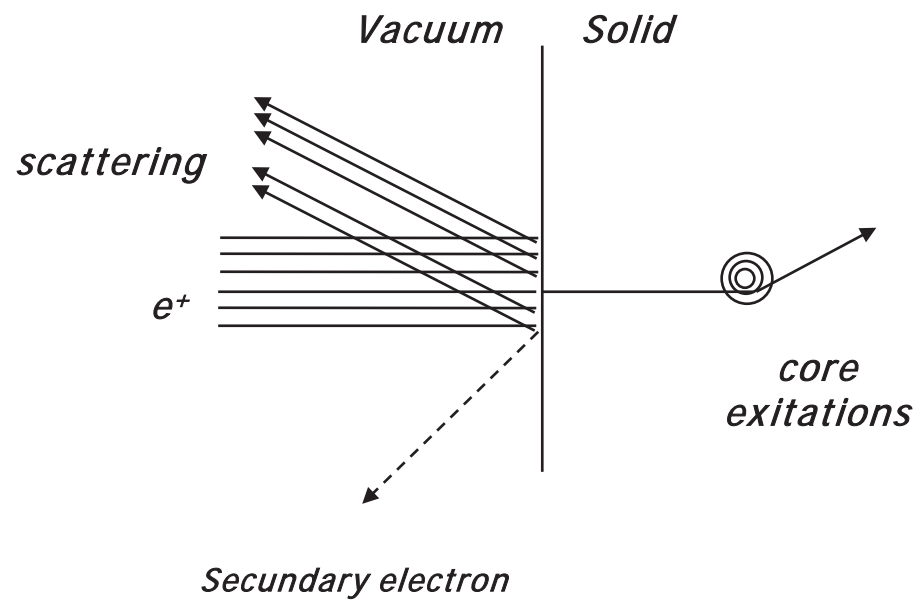
*(Bremsstrahlung or prompt fission gamma energy - 1.022 MeV)*

## Positron - solid interaction

### First encounter

Timescale  $< 10^{-15}$  seconds

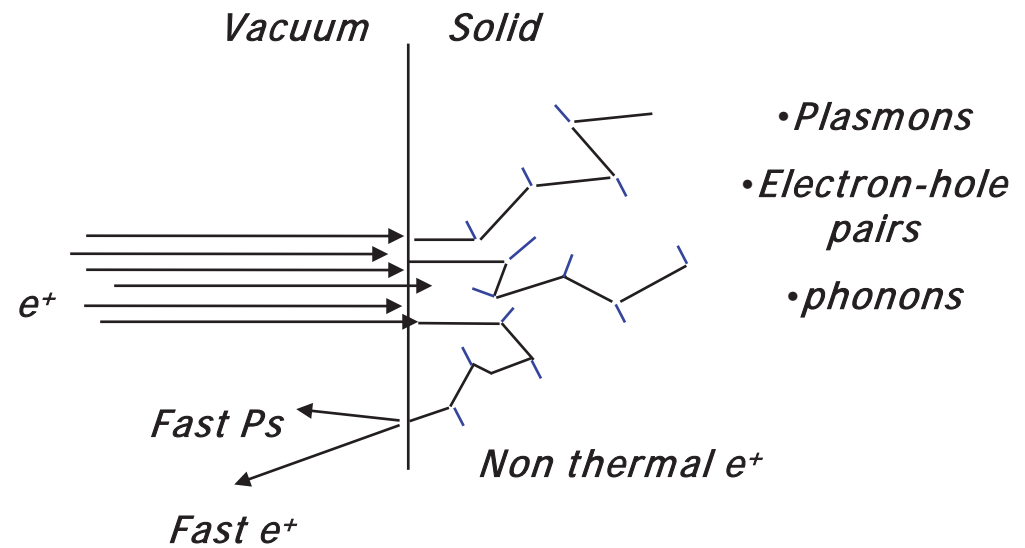
Fast positrons entering a solid lose their kinetic energy by different inelastic energy loss mechanisms



# Positron - solid interaction

## Thermalisation

Timescale  $< 10^{-12}$  seconds

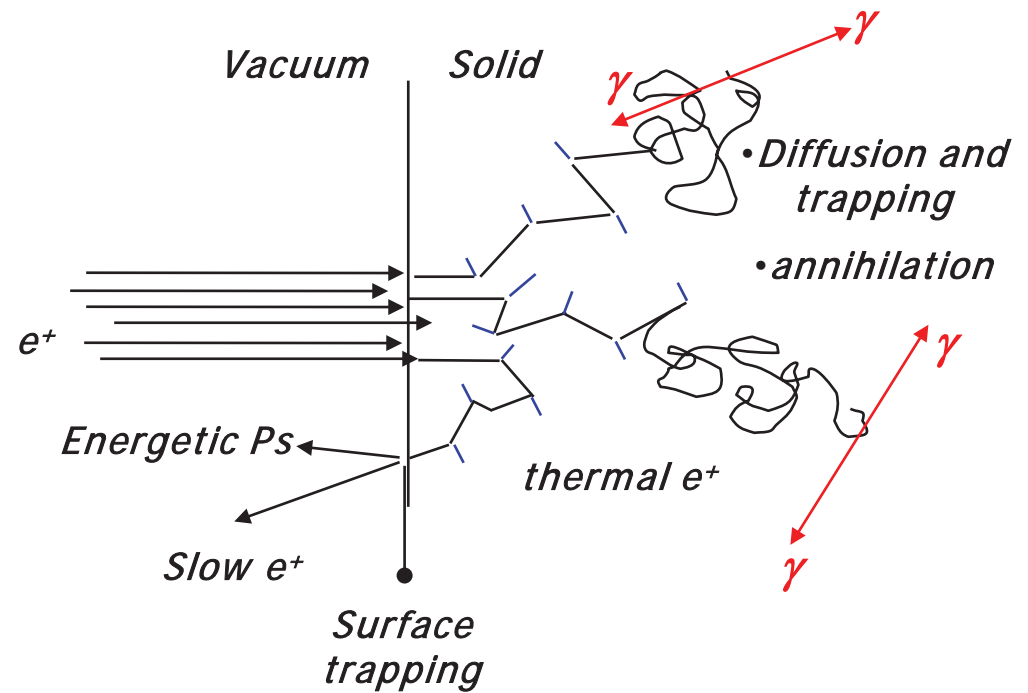




# Positron - solid interaction

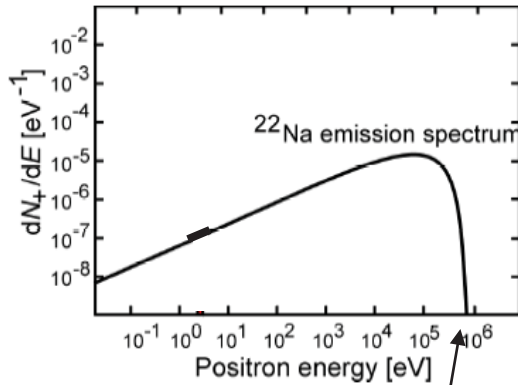
*equilibrium*

*Timescale < 10<sup>-10</sup>  
seconds*



## Positron implantation profile

Fast positrons  
( $\beta^+$  energy distribution)



$$I(x) = I(0) \exp(-a_+ x)$$

$$a_+ = (16 \pm 1) \rho E_m^{-1.43} \text{ (cm}^{-1}\text{)}$$

(E in MeV)

No depth resolution

Implantation  
depth range



Element	density [g/cm <sup>3</sup> ]	a <sub>+</sub> [cm <sup>-1</sup> ]	r (99%) [μm]
Al	2.7	104	442
C	2.25	87	530
Li	.53	20	2250
Mo	10.2	394	117
Si	2.33	90	500
W	19.35	747	62

## Positron implantation profile

with  $m = 2$

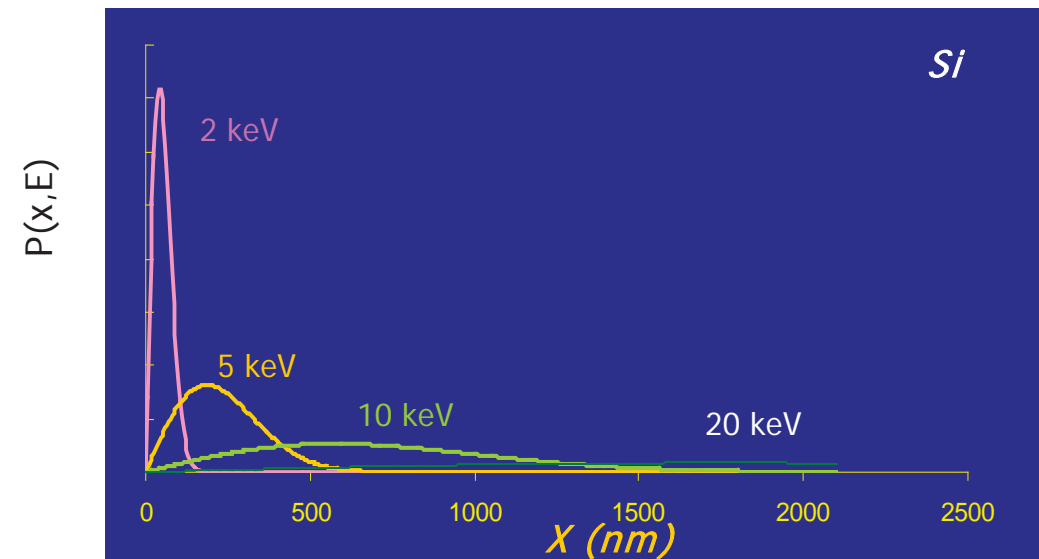
$$P(x, E) = \frac{2x}{x_0^2} \exp - \left[ \frac{x}{x_0} \right]^2$$

$$x_0 = 1.3 \langle x \rangle$$

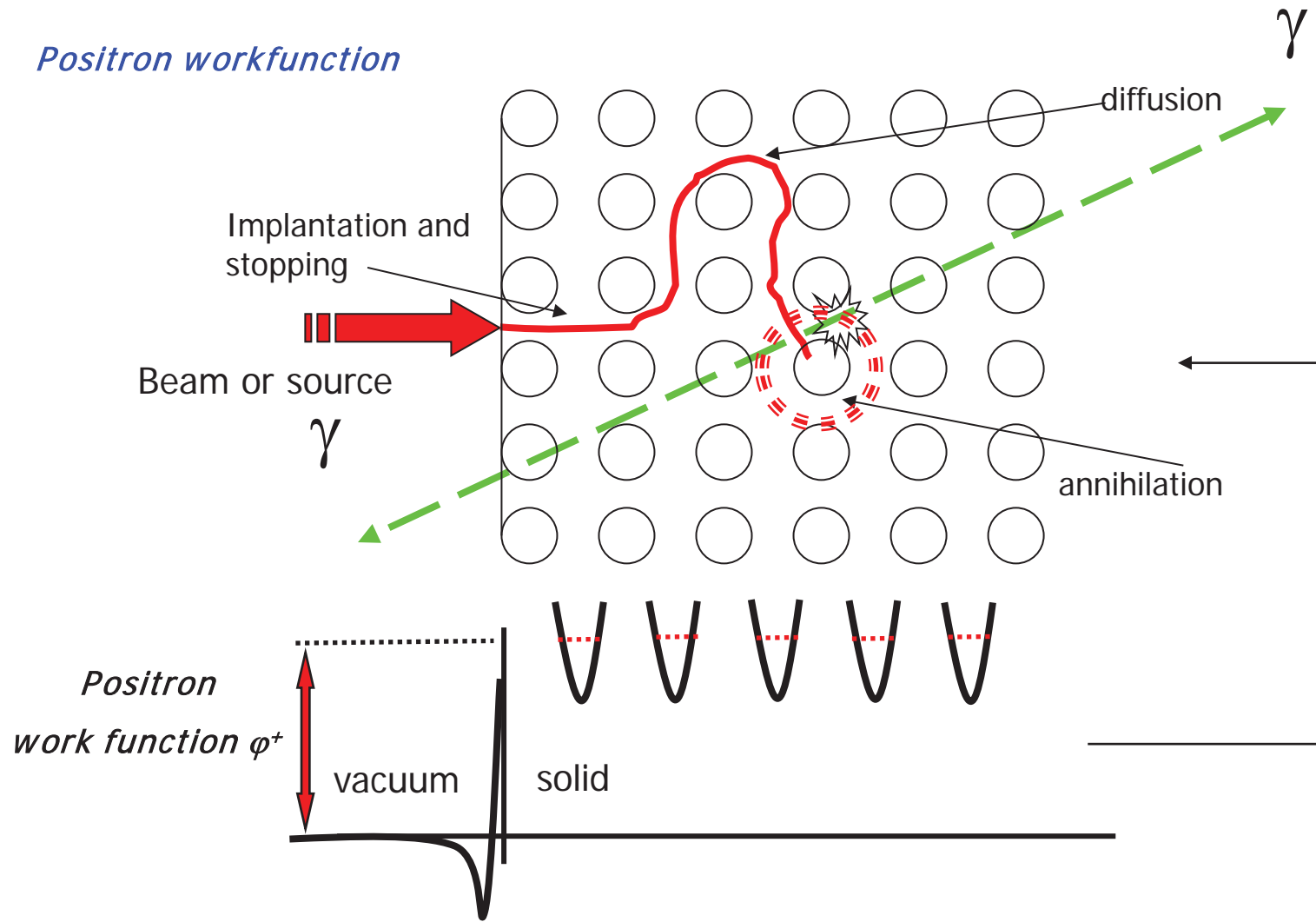
$$\langle x \rangle = (\alpha / \rho) E^n$$

$$n = 1.6 - 1.8, \alpha \sim 4.0$$

"Slow" positrons  
Mono energetic beams  
(~ 0.1 - 25 keV)

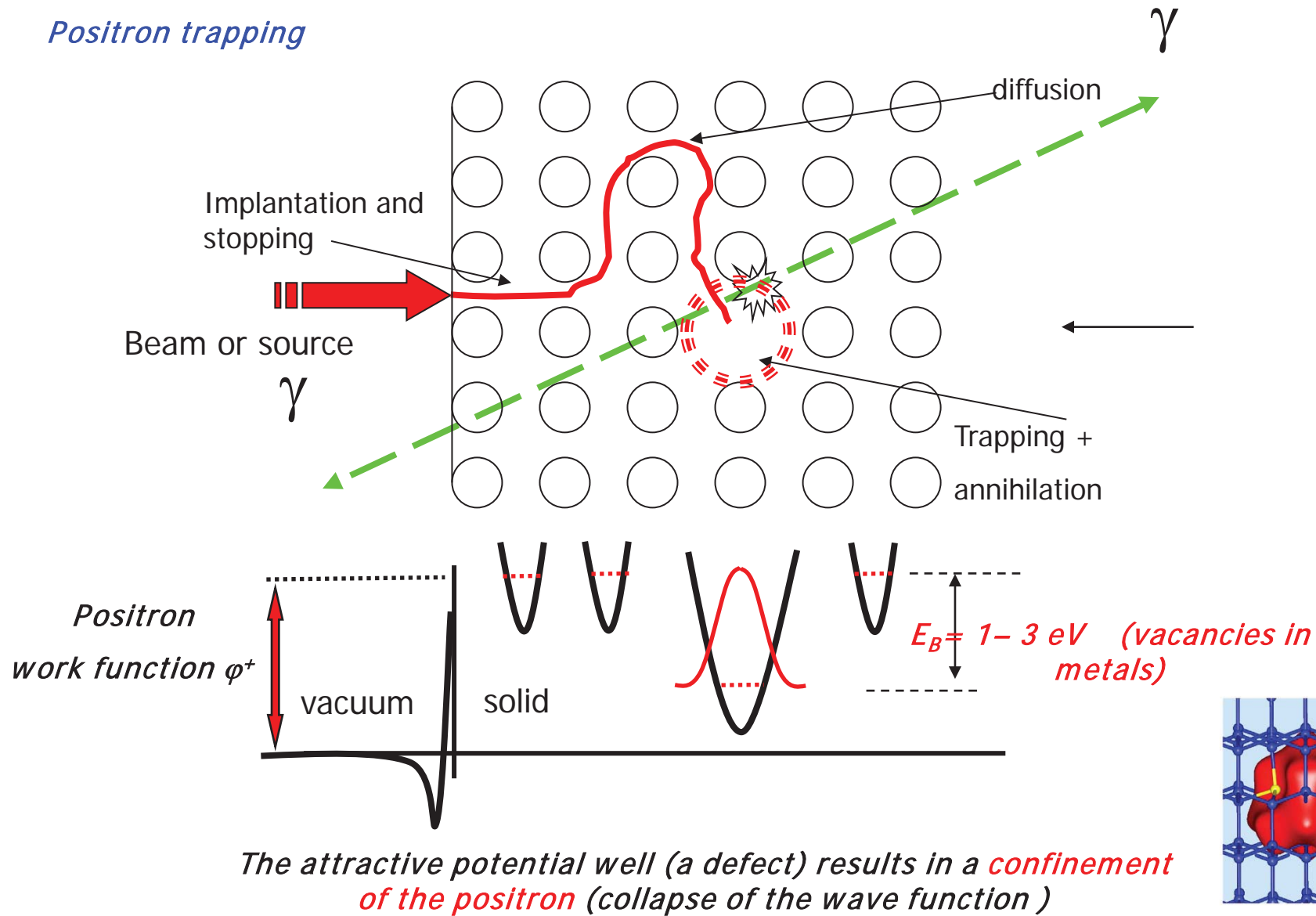


*Positron workfunction*

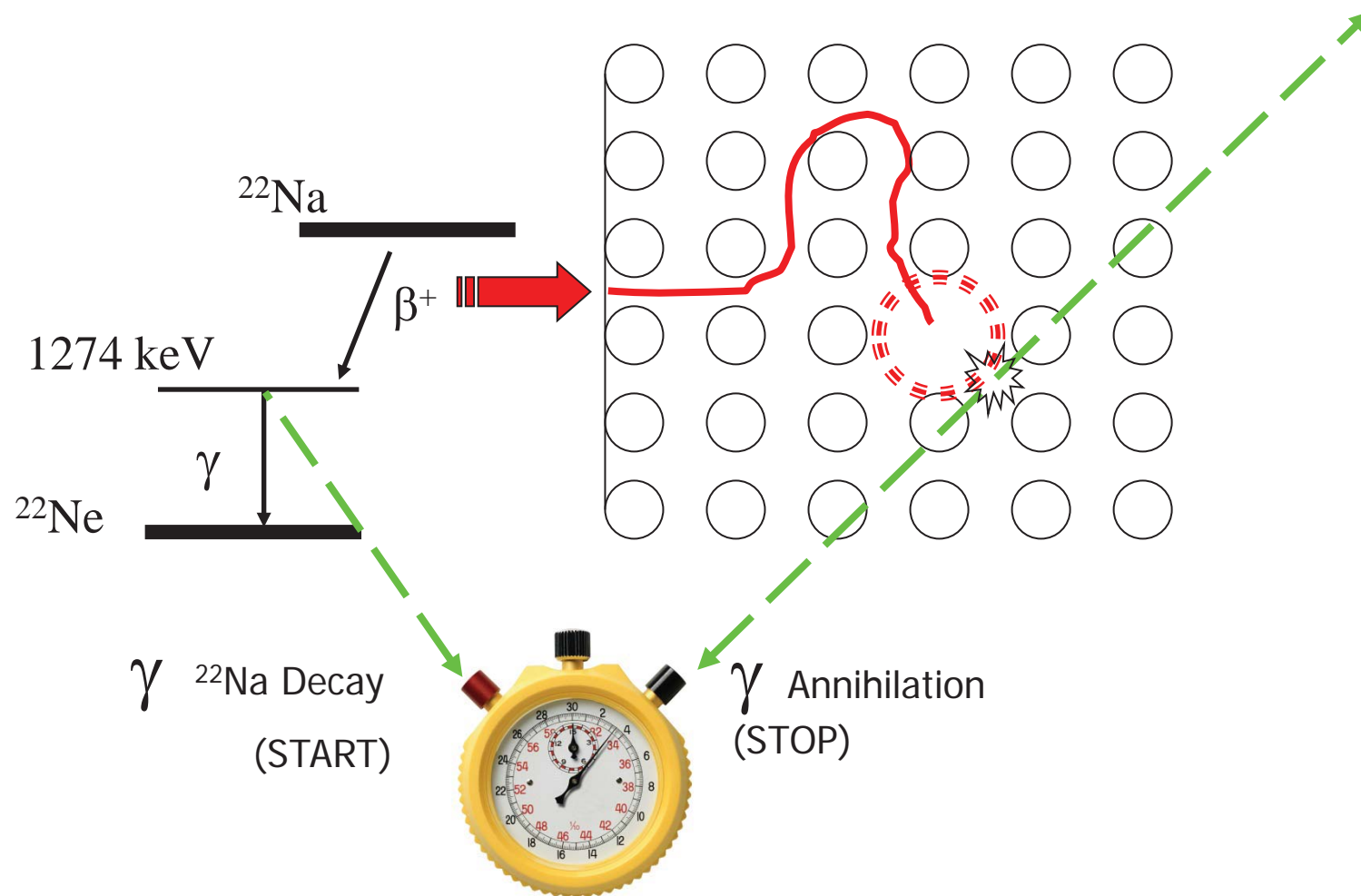


$\phi^+ < 0$  *spontaneous emission from the solid into vacuum (W, Mo, Ni, SiC, . . .)*

# Positron trapping



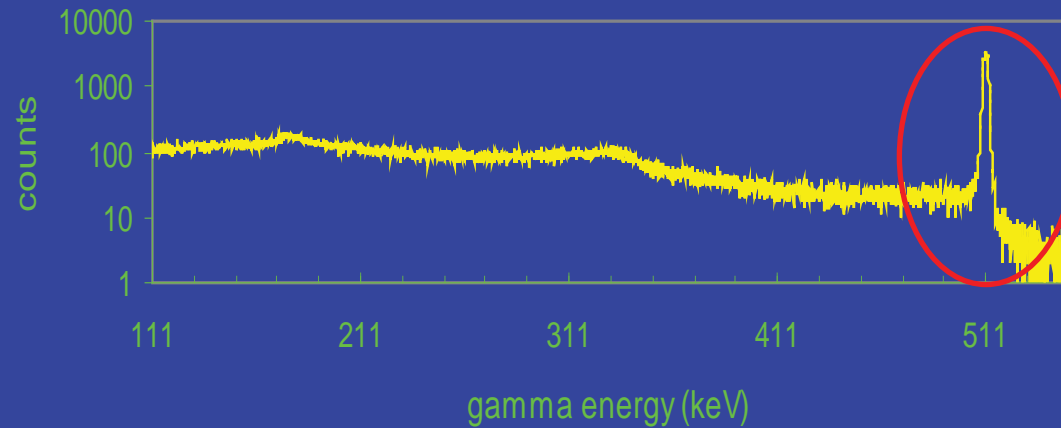
*Probing Local electron density with positrons*



## Observables (1)

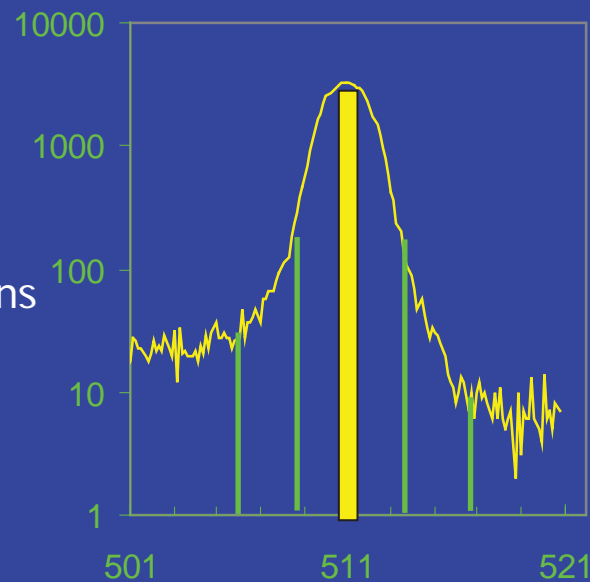
*Doppler broadening*  
*S(hape) and W(ing)*

detecting one 511 keV gamma  
and determining the width of  
the photo peak



- S parameter

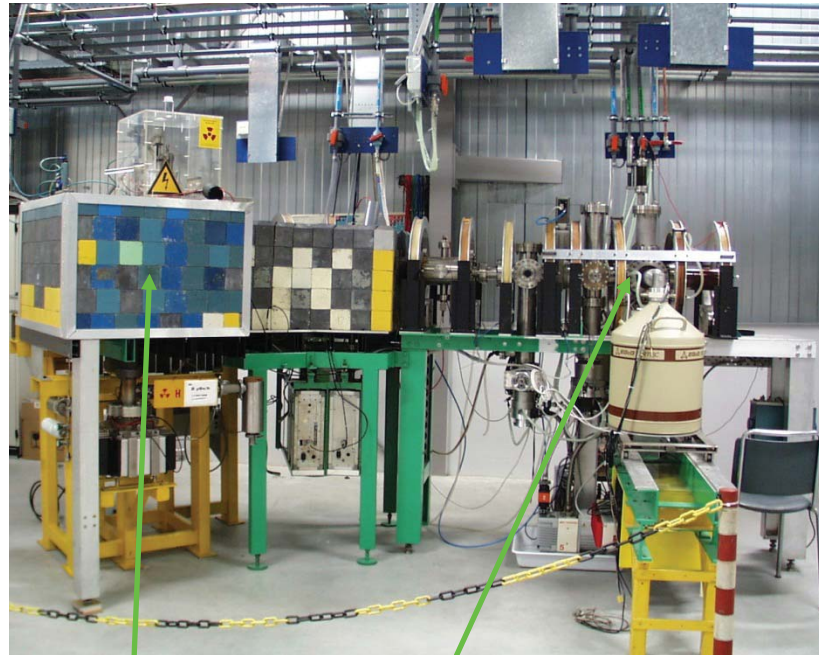
Low momentum  
Valence, conduction electrons  
P(ara) Positronium  
Open volume  
(vacancies, voids ...)



## W parameter

High momentum  
Core electrons  
  
Local chemical surroundnig  
Nano precipitates, sub-lattice  
defects

# Doppler broadening setup

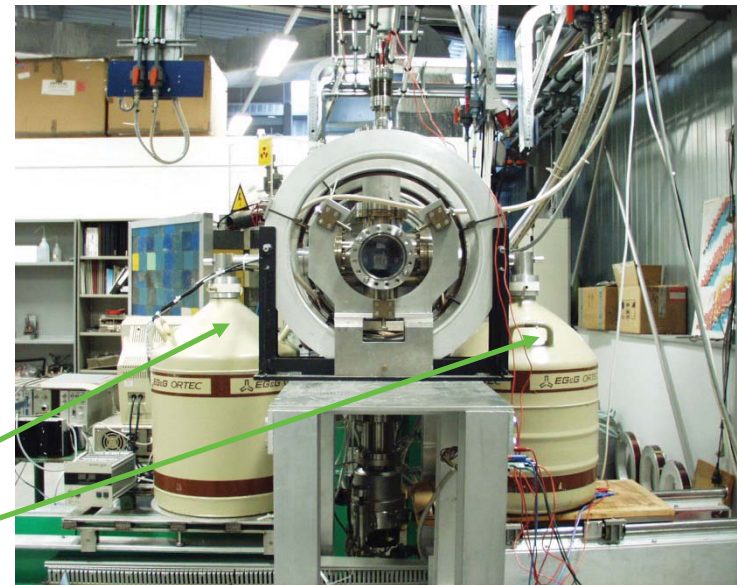


$^{22}\text{Na}$  source

sample chamber

Coincidence setup (2 detectors)

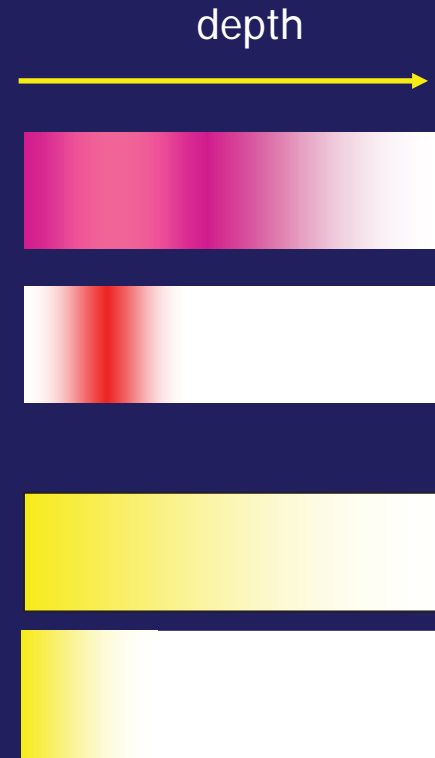
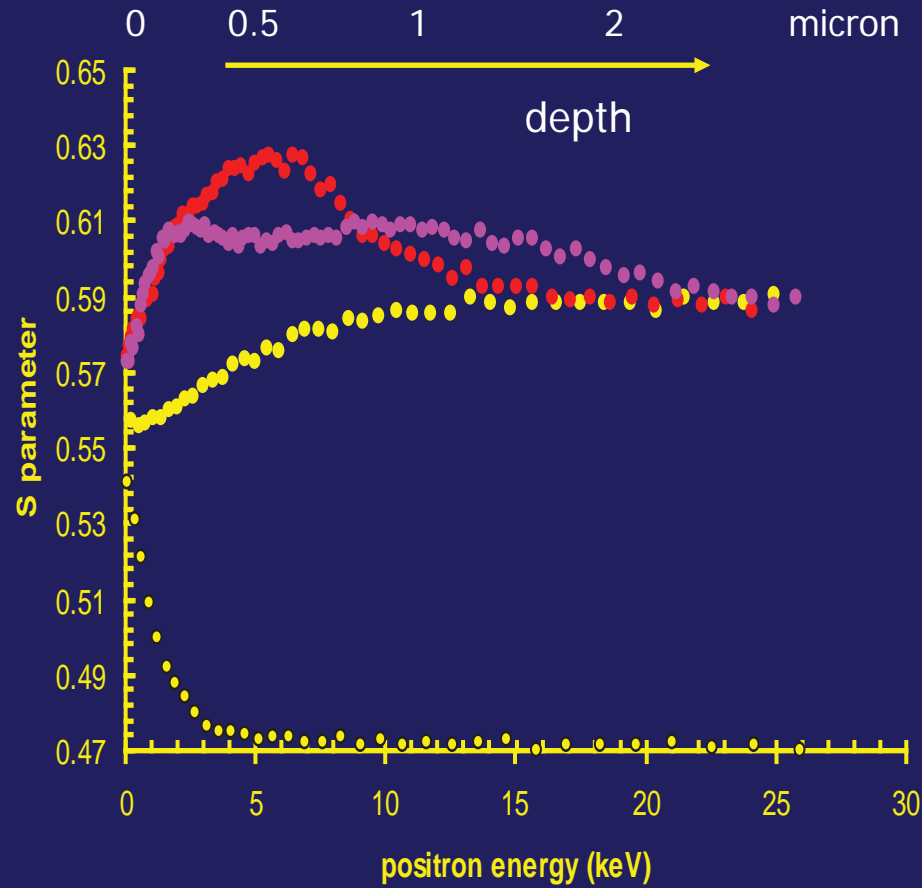
The Variable Energy Positron beam (VEP)



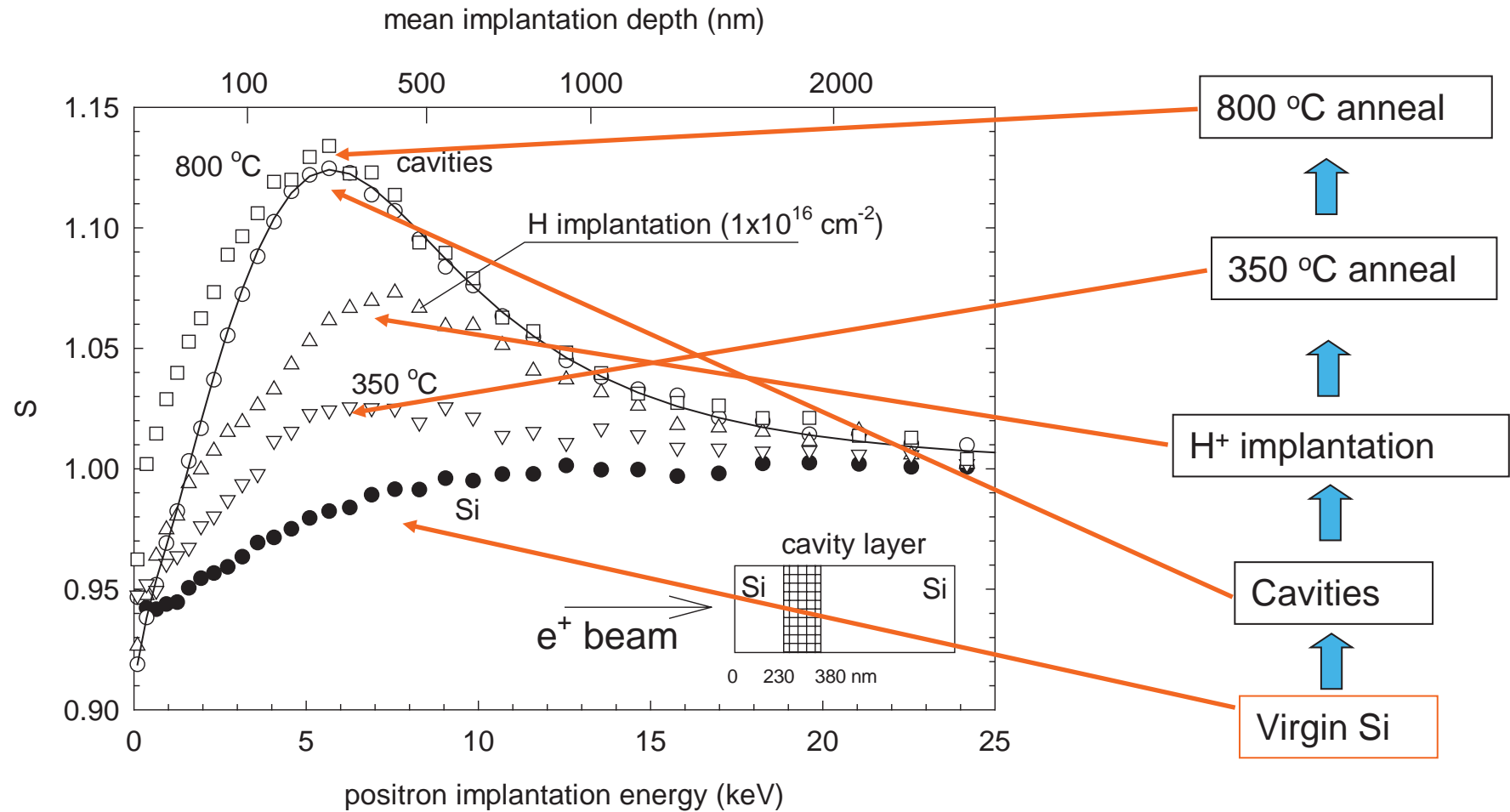


# Some examples (beam exp<sup>t</sup>)

? Model ?

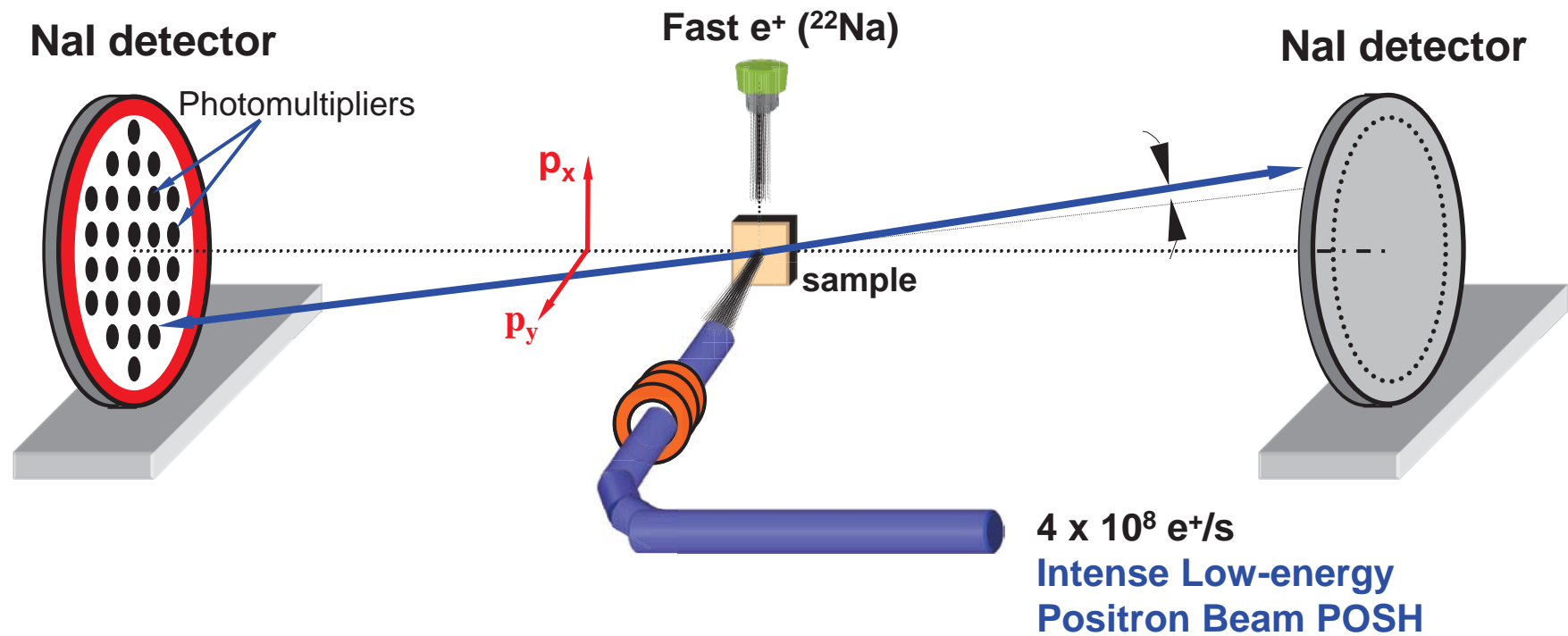


$1 \times 10^{16} \text{ H}^+ \text{ cm}^{-2}$

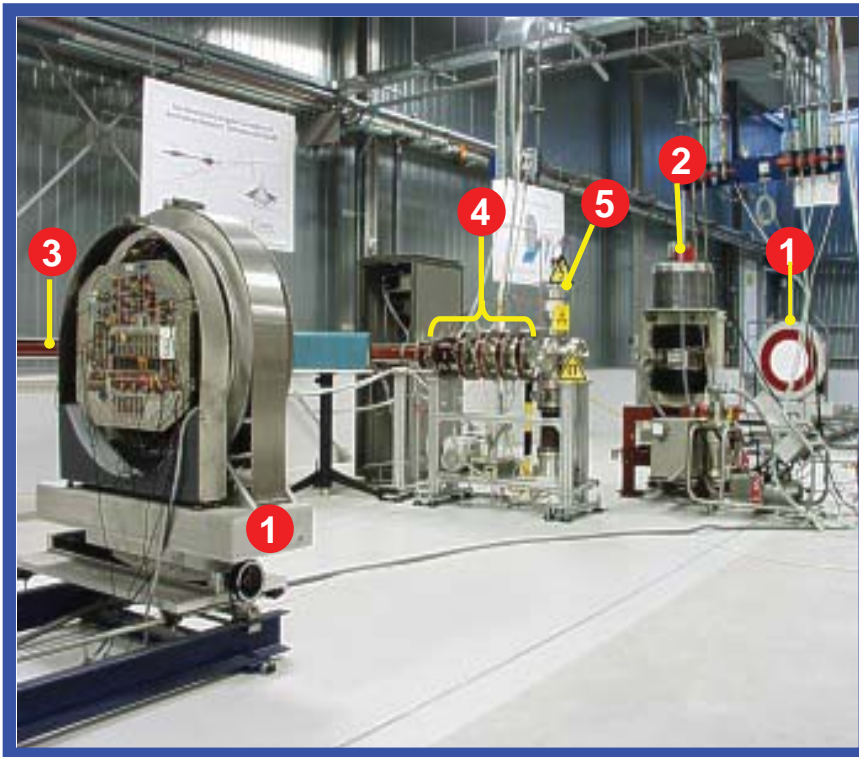


## Observables (2)

*Angular Correlation* measurement of the angle between the two 511 keV gammas



*The Delft POSH 2D-ACAR setup*



- ① Anger cameras
- ② source ( $^{22}\text{Na}$ ) chamber
- ③ POSH  $e^+$  beam line
- ④ Accelerator
- ⑤ Target chamber

*Example of 1-D ACAR*

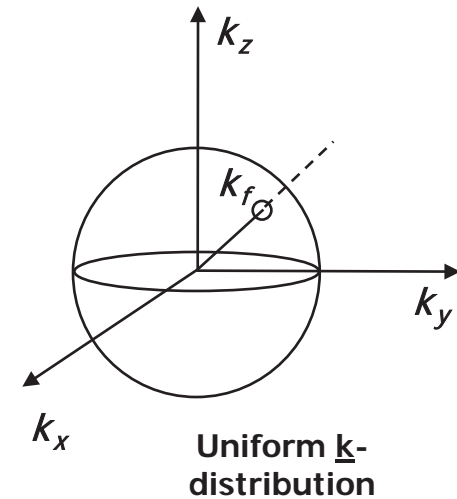
*Measurement of the Fermi level of electrons in Al*

*free electron gas model*

*Highest energy level occupied  $E_f$*

*→ Maximum momentum  $p_f = (2 m E_f)^{1/2}$*

*→ Maximum angle angular correlation ( $\alpha_f$ )*

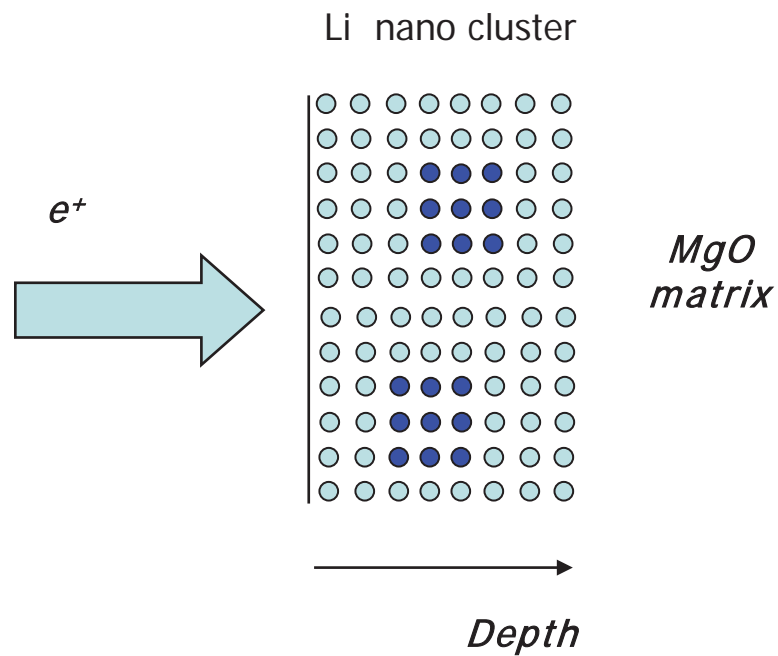


*show*



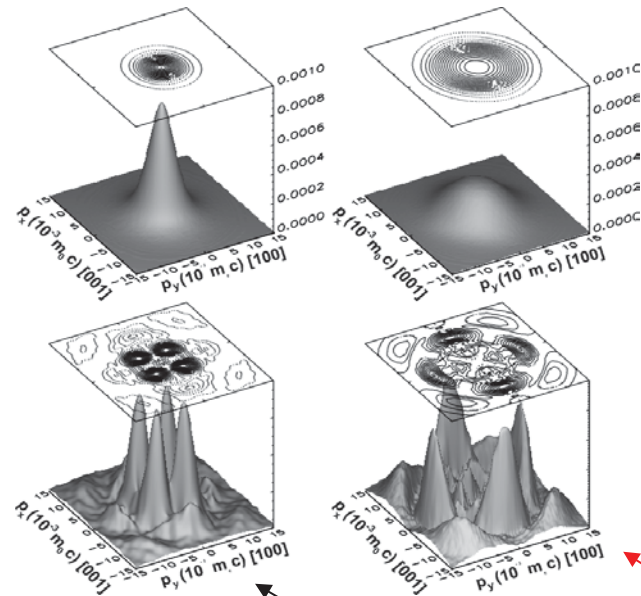
*Example of a 2D – ACAR application*

**Li nanoclusters are *FCC* and in simple epitaxy with the MgO host matrix.**



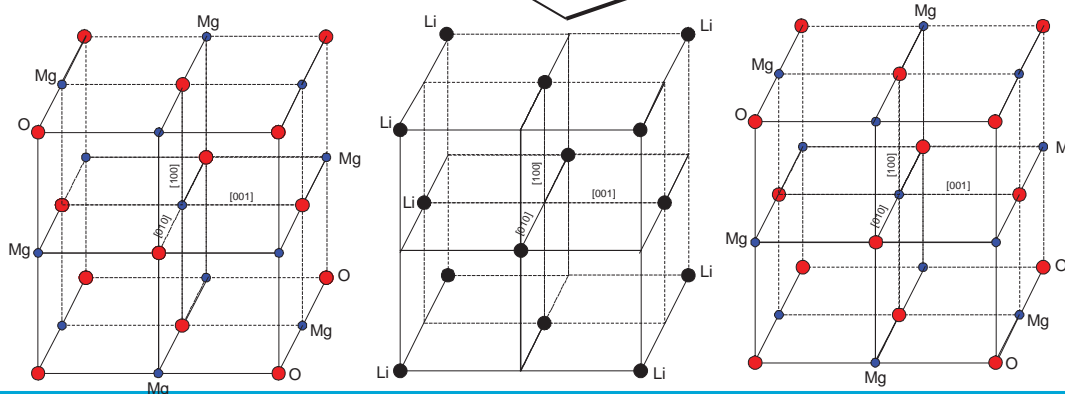
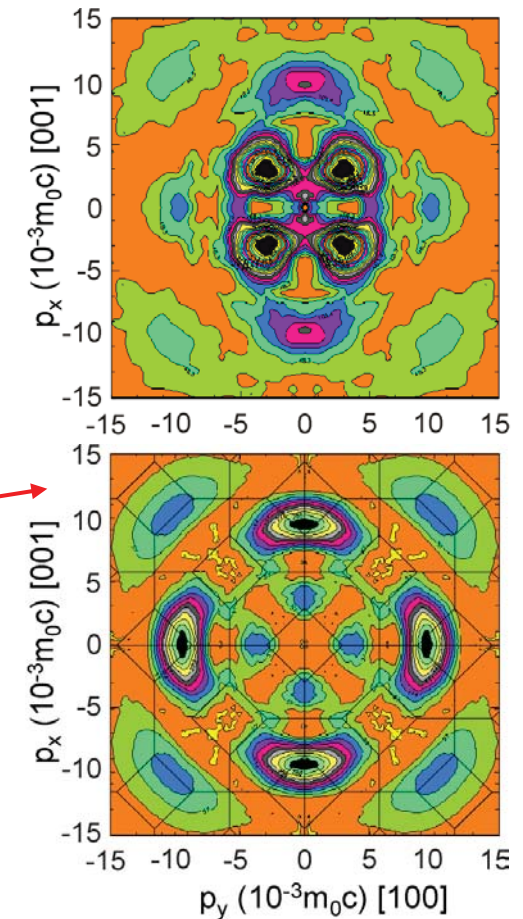
# Li nanoclusters are FCC and in simple epitaxy with the MgO host matrix.

MgO(100):Li  
POSH (4 keV)



MgO(100)  
fast e<sup>+</sup> (<sup>22</sup>Na)

MgO(100):Li  
nanocrystals

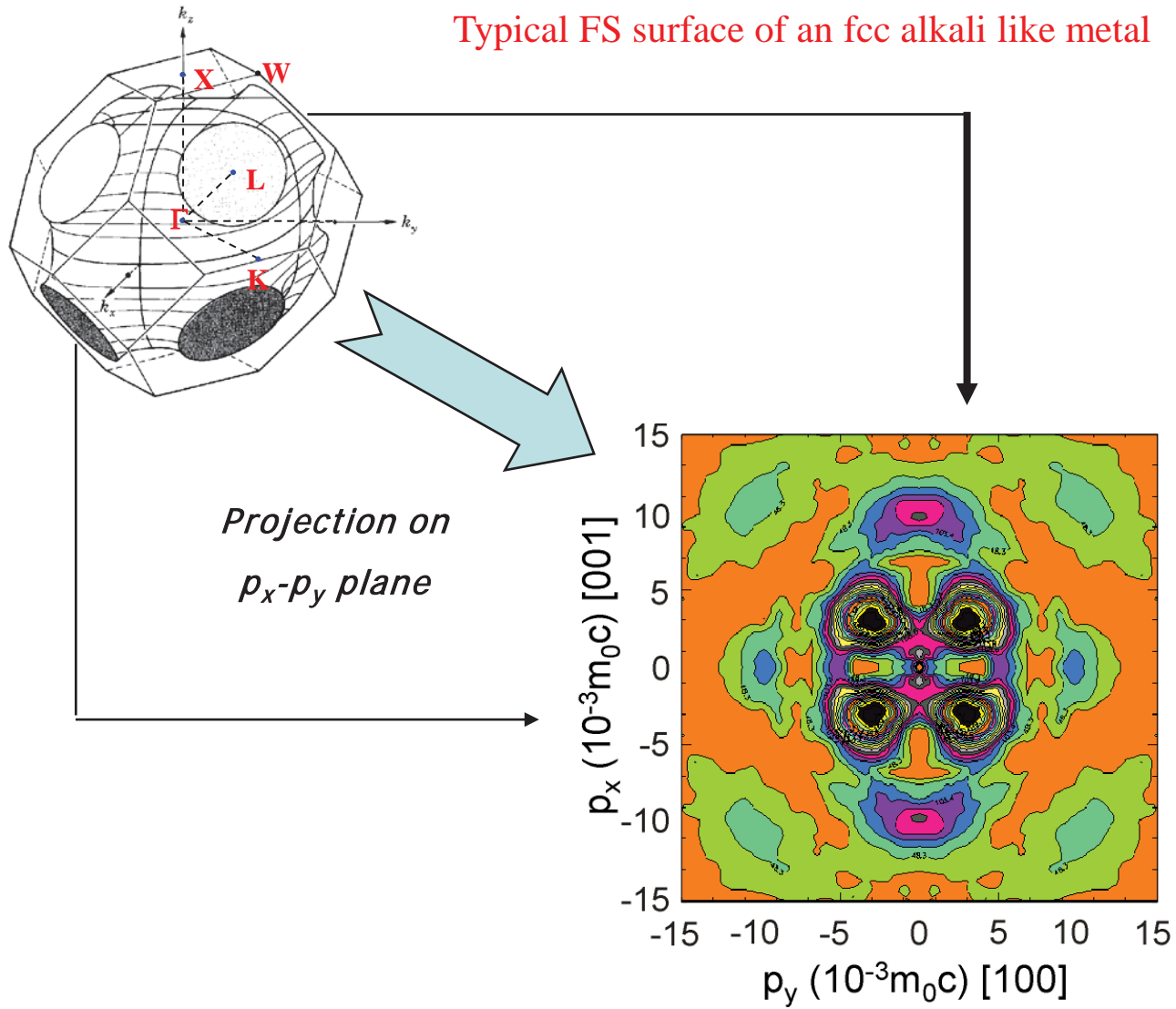


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MgO(100)

*In MgO Li nano clusters have FCC structure !*

Typical FS surface of an fcc alkali like metal

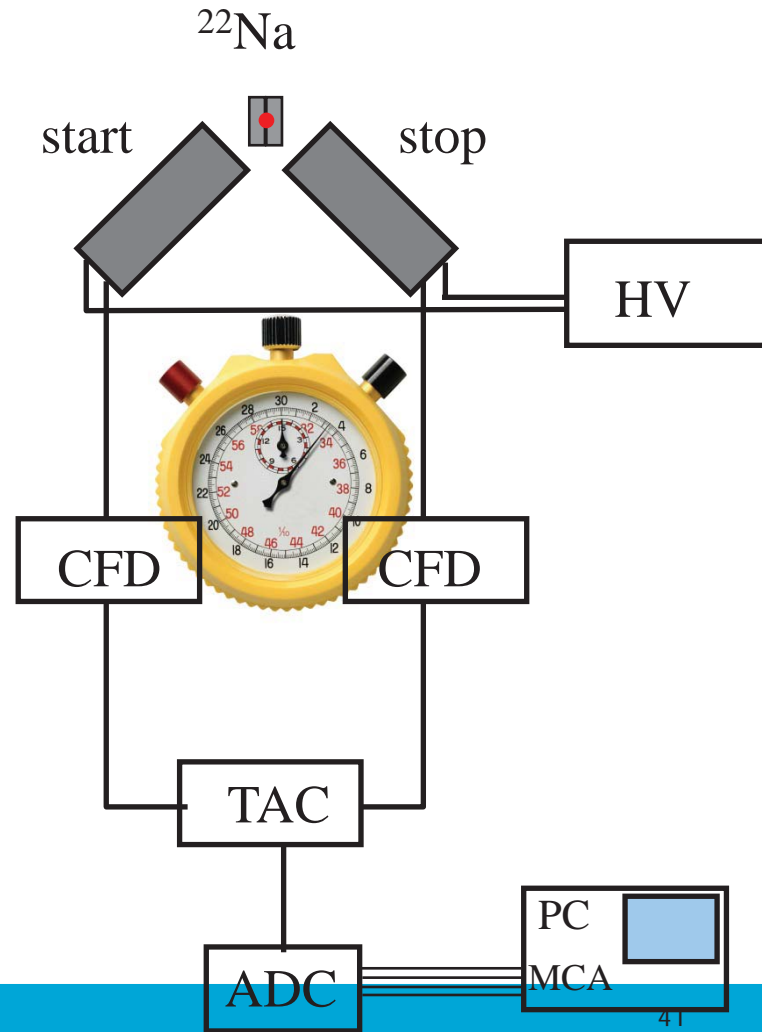




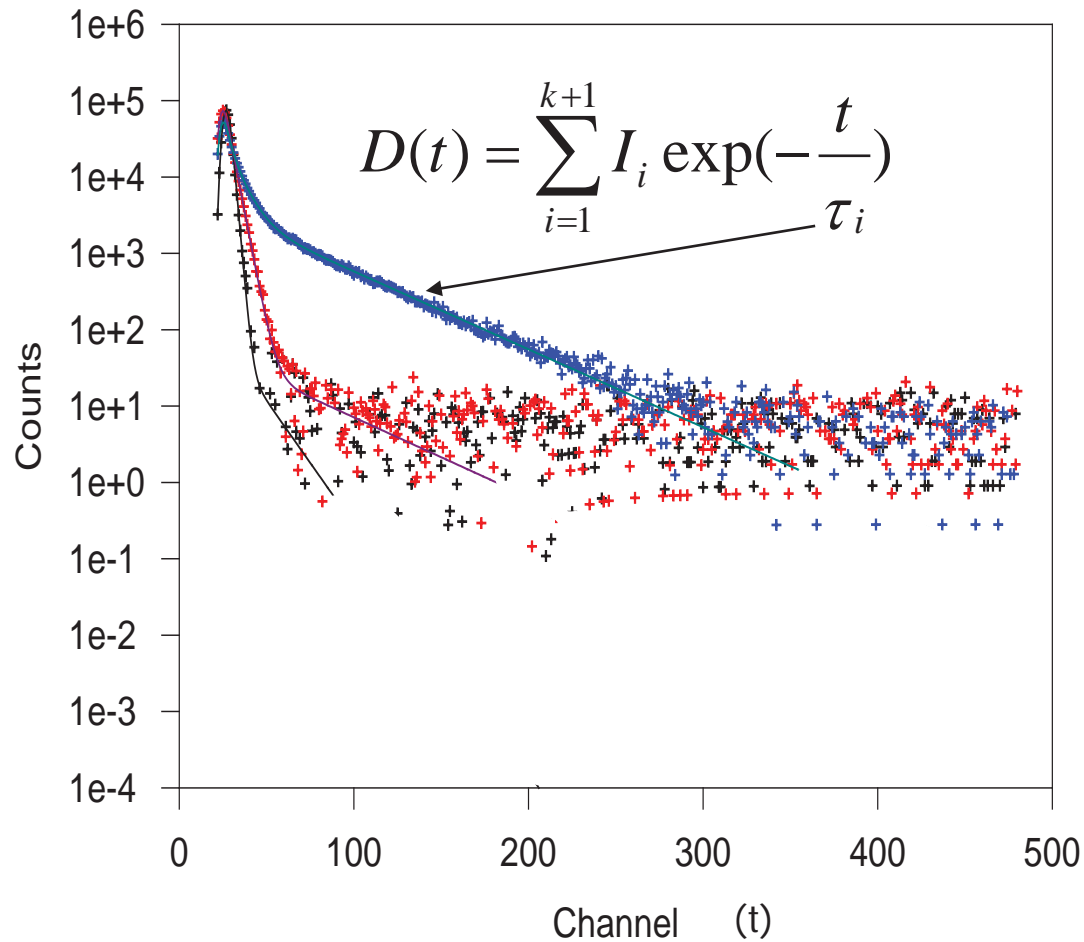
# Observables (3)

*positron lifetime (PALS)*  
measurement of the time elapsed between  
positron injection and annihilation

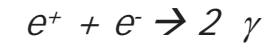
resolution 260 ps



### Typical PALS spectra



Positron Lifetimes in dense solids  
(metals and semiconductors)



- Tungsten (100 ps)
- Silicon (220 ps)

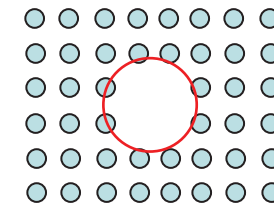
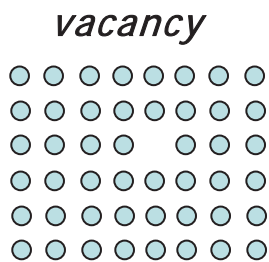
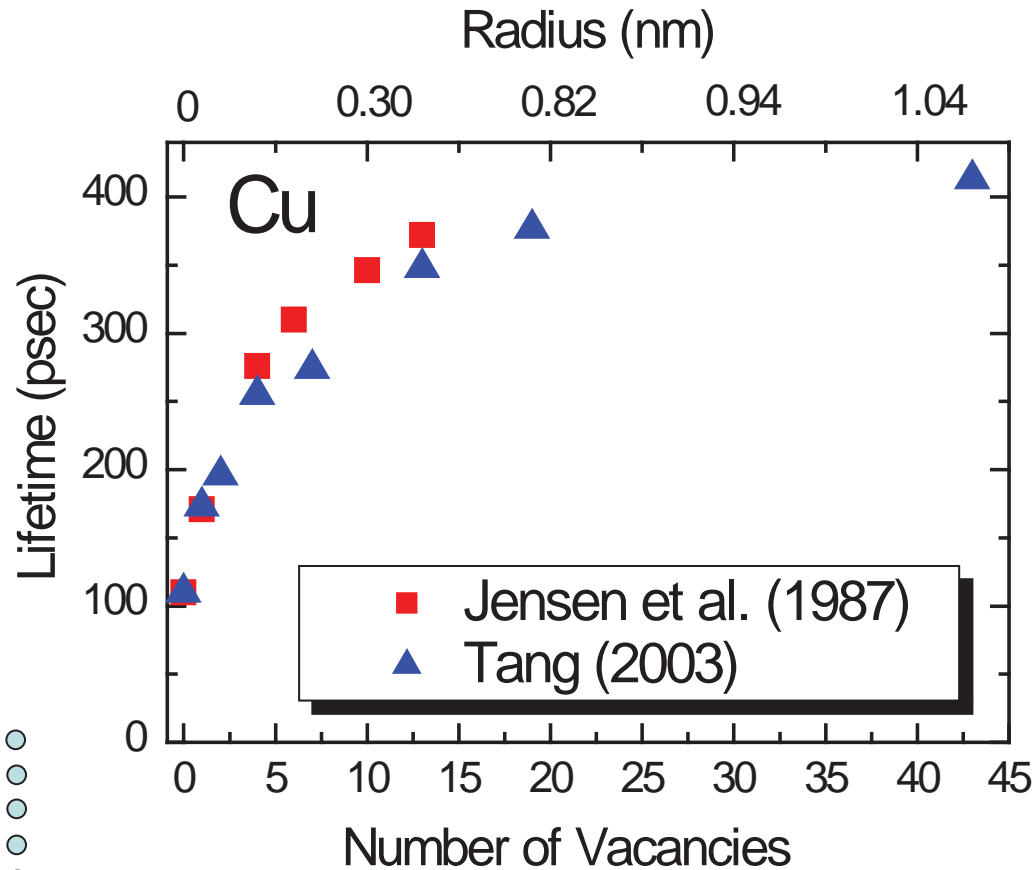
Positron lifetimes in polymer

*ortho* - Ps formation (140 ns)

- PolyEthyleen (PE) (2-3 ns)

# Calculated positron lifetimes in vacancy clusters

$$\lambda_0(n_e) = \pi r_o^2 c n_e$$



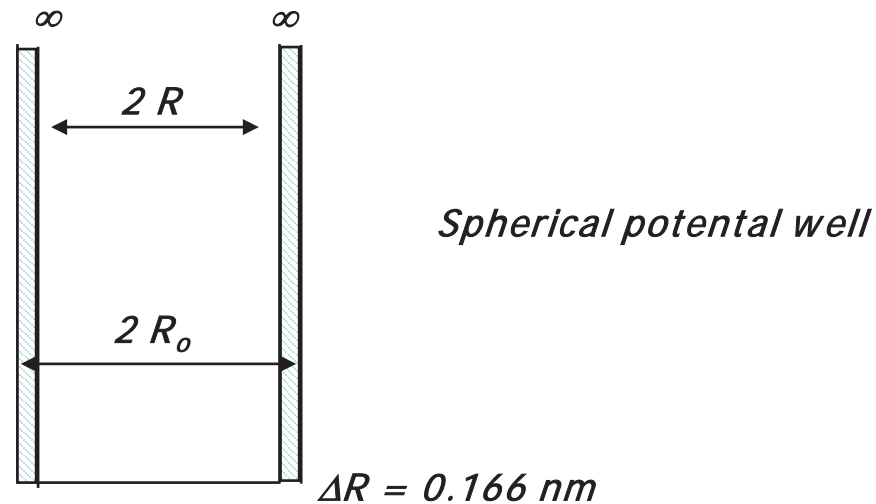
*Vacancy cluster*

### *Positron lifetimes in polymers*

*Semi empirical relation between volume size (R) and o-Ps decay rate*

*Usually the third long lifetime component*

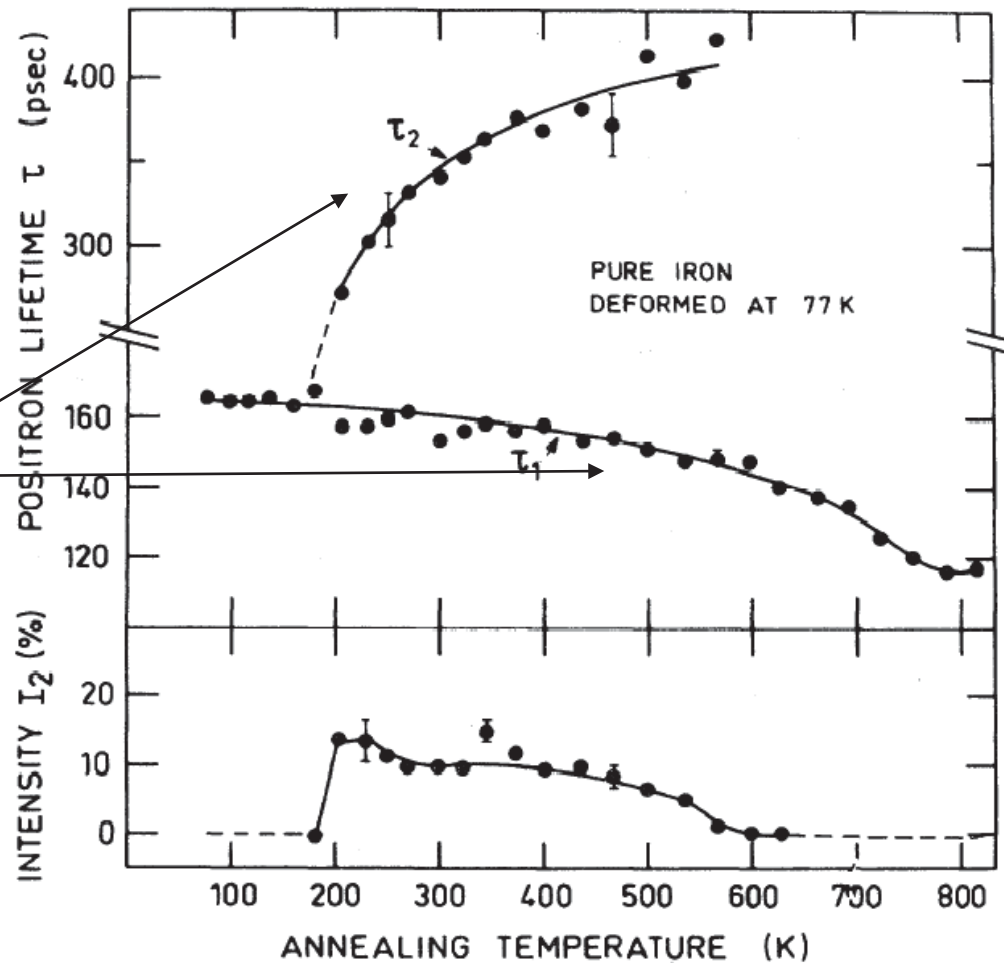
$$\tau_3 = \left[ 2 \left( 1 - \frac{R}{R_0} + \frac{1}{2\pi} \sin(2\pi R / R_0) \right) \right]^{-1}$$



# Annealing of Fe deformed at low temperature

$$D(t) = \sum_{i=1}^{k+1} I_i \exp\left(-\frac{t}{\tau_i}\right)$$

Vacancies migrate and cluster above ~200 K



## sensitivity range for measuring defect concentration (Al and Mo)

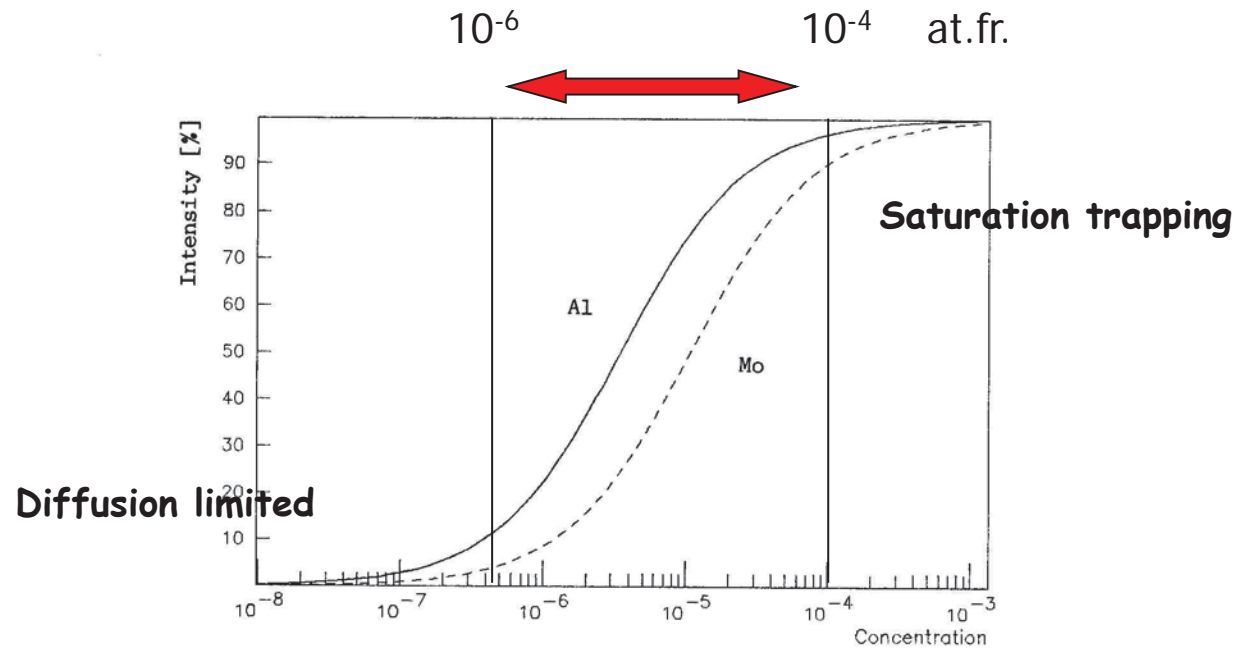
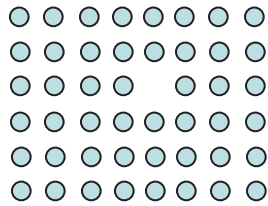


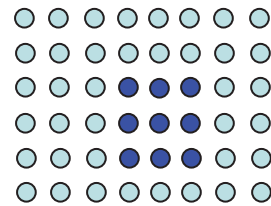
Fig. 1.2 Intensity of the defect lifetime for monovacancies in Al and Mo as a function of the defect concentration (in defects per atom)

*examples of systems studied with positrons*

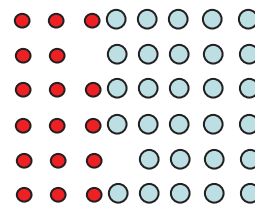
Vacancies



nano precipitates



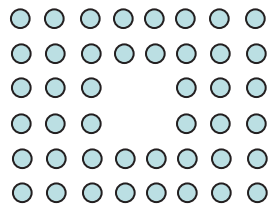
interfaces



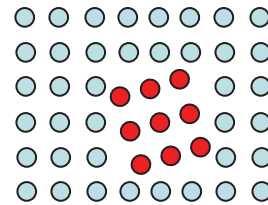
polymers (free volume)



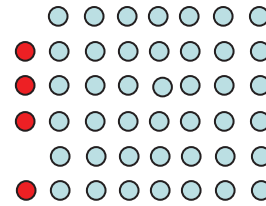
Voids



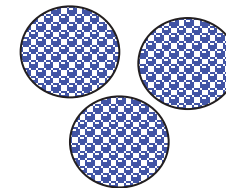
nano precipitates



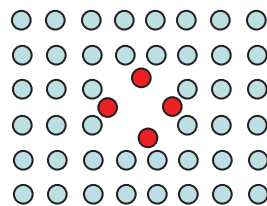
surfaces



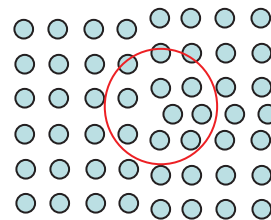
nano-colloids



internally decorated voids



dislocations



Metals, Alloys

Semiconductors (Si, GaAs, ...)

Polymers

Colloids, Ceramics, Metaloxides

.....