

Non-Ideal Effects in Compressible Swirling Flows

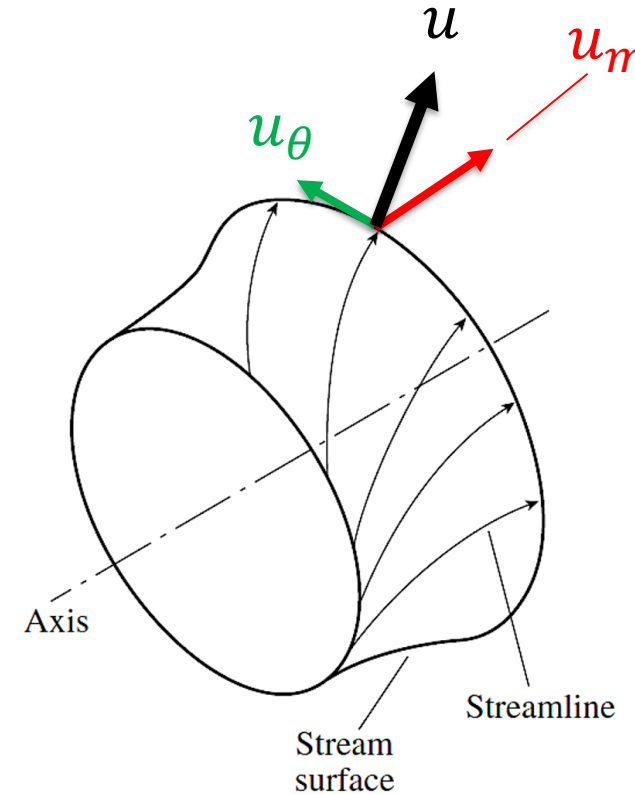
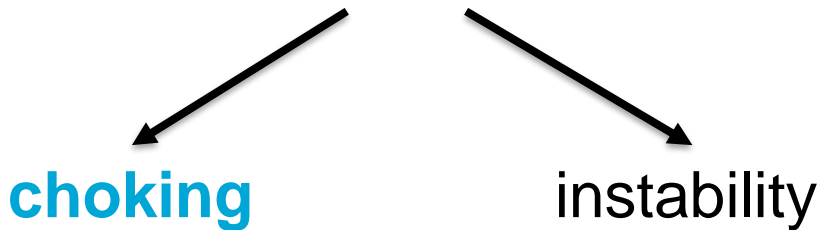
***3rd International Seminar on NICFD
Delft, The Netherlands***

F. Tosto, A. Giuffre', P. Colonna, M. Pini
Propulsion and Power, Delft University of Technology

Background

Limited knowledge of NICFD effects on turbomachinery

- efficiency
- **operability**

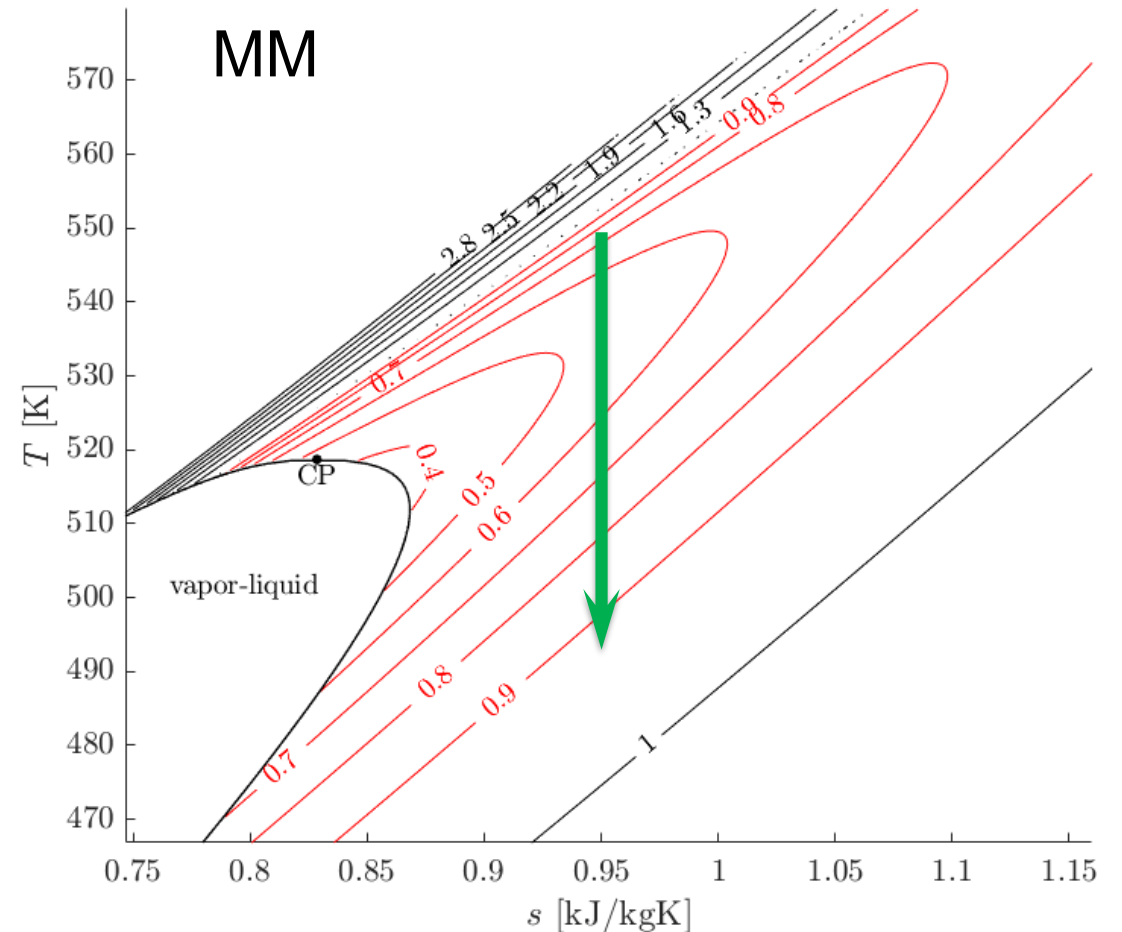


NICFD effects: isentropic exponent γ_{pv}

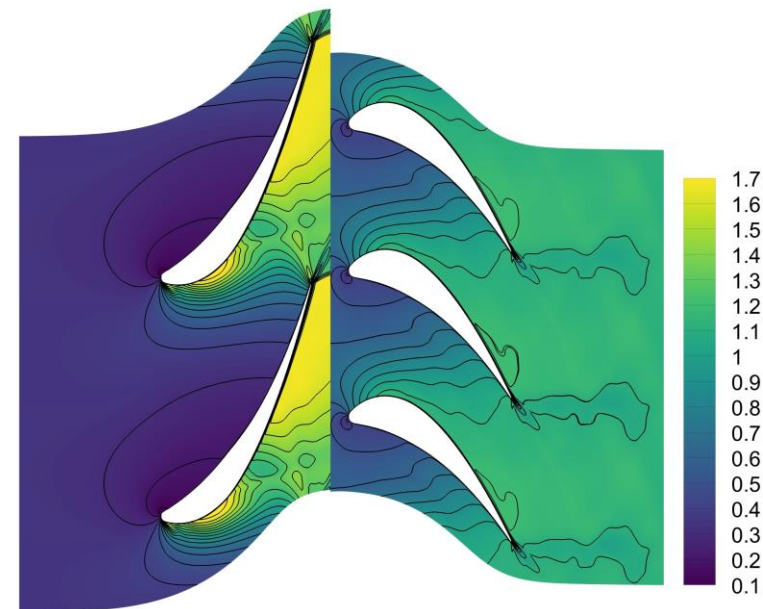
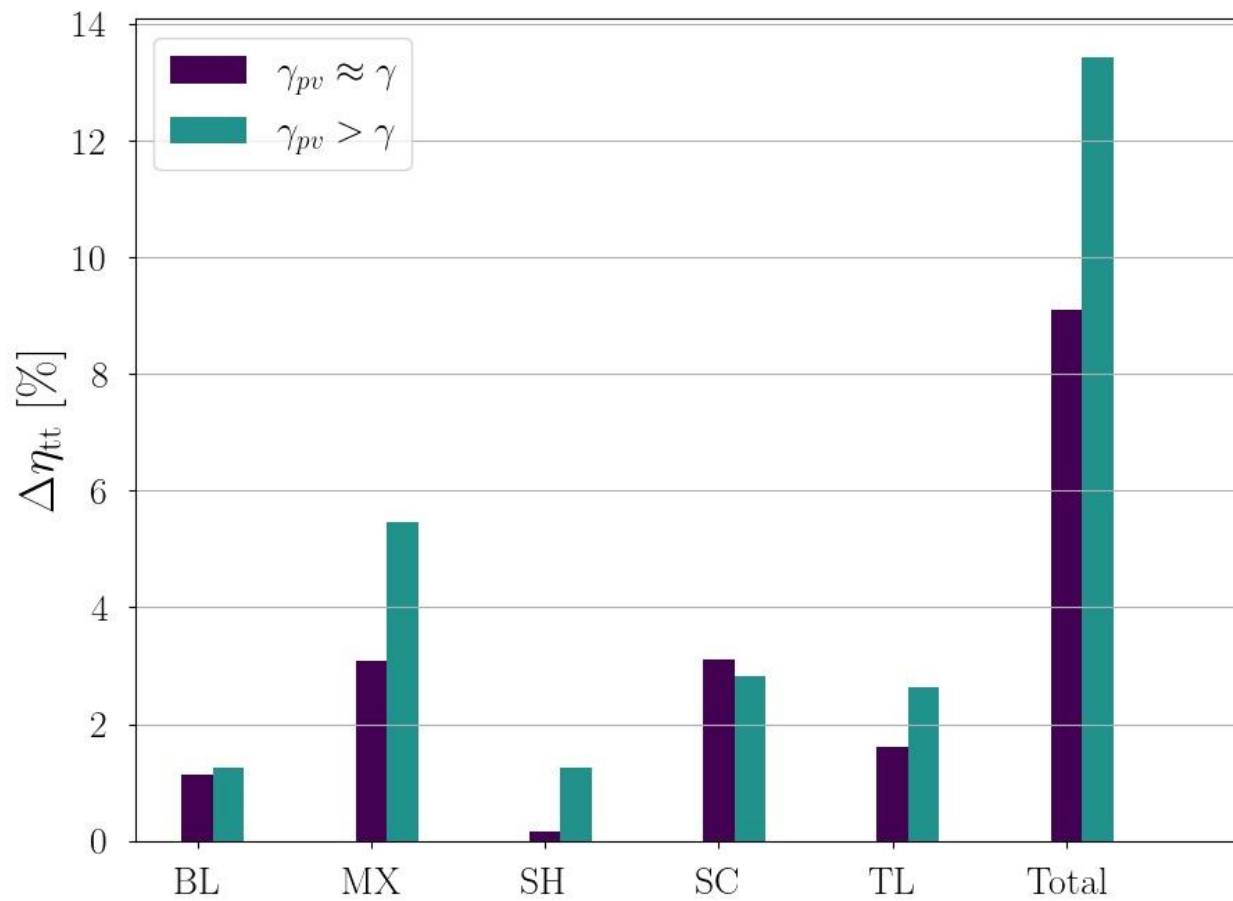
$$\gamma_{pv} = -\frac{v}{p} \left(\frac{\partial p}{\partial v} \right)_s$$

Dilute gas state:

$\gamma_{pv} \rightarrow \gamma$, with $\gamma > 1$



Relevance of NICFD effects on losses



Efficiency can differ of up to $\sim 4\%$

Giuffrè and Pini, "Design guidelines for axial turbines operating with non-ideal compressible flows", JEGTP, 2020, article in press

Problem Statement

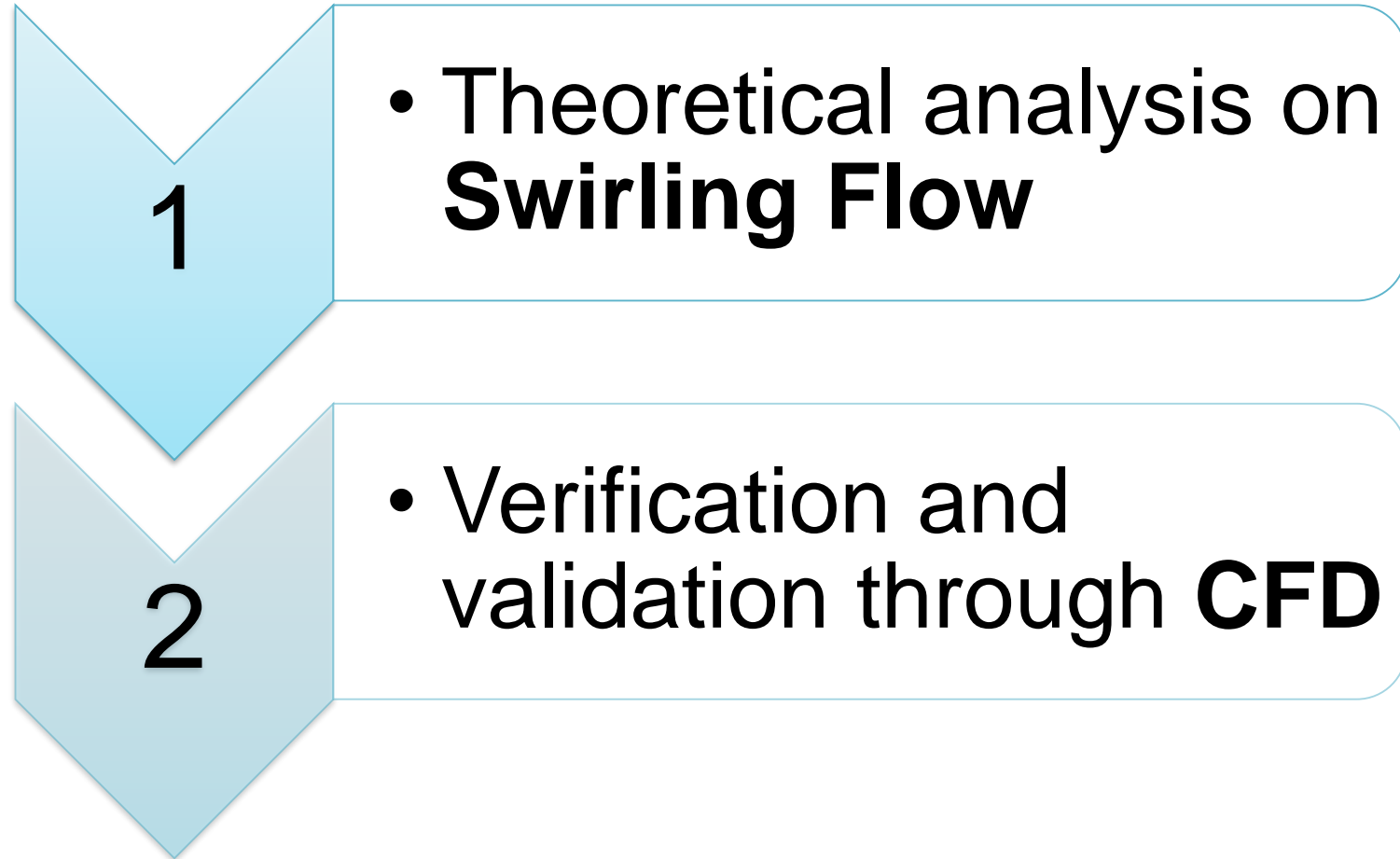
No existing knowledge on quantitative impact of NICFD effects on

- **Choking** conditions
- Flow **deviation** in post and pre-expansion processes

Scope of Research

- Assess variation of flow **deviation** as $f(\gamma_{pv})$
- Assess impact of γ_{pv} on **choking** in turbomachinery

Methodology: 2-steps Approach



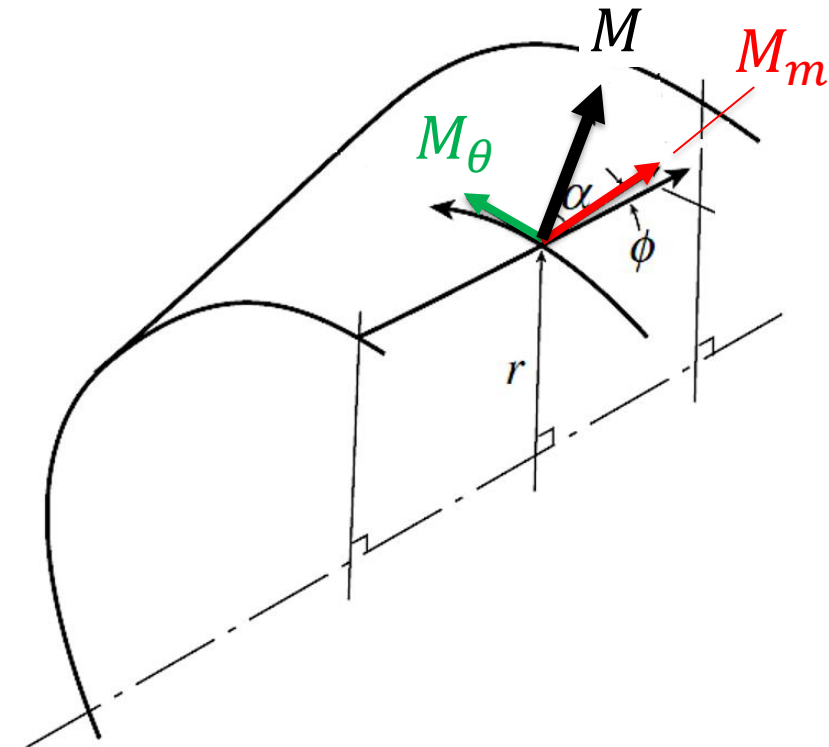
Theoretical Analysis

Corrected mass flow per unit area (1)

$$\dot{m}_{corr} \approx \frac{M_m}{\left(1 + \frac{\gamma_{pv} - 1}{2} M^2\right)^{\frac{\gamma_{pv} + 1}{2(\gamma_{pv} - 1)}}}$$

absolute
Mach number

$= M \cos \alpha$
meridional
Mach number



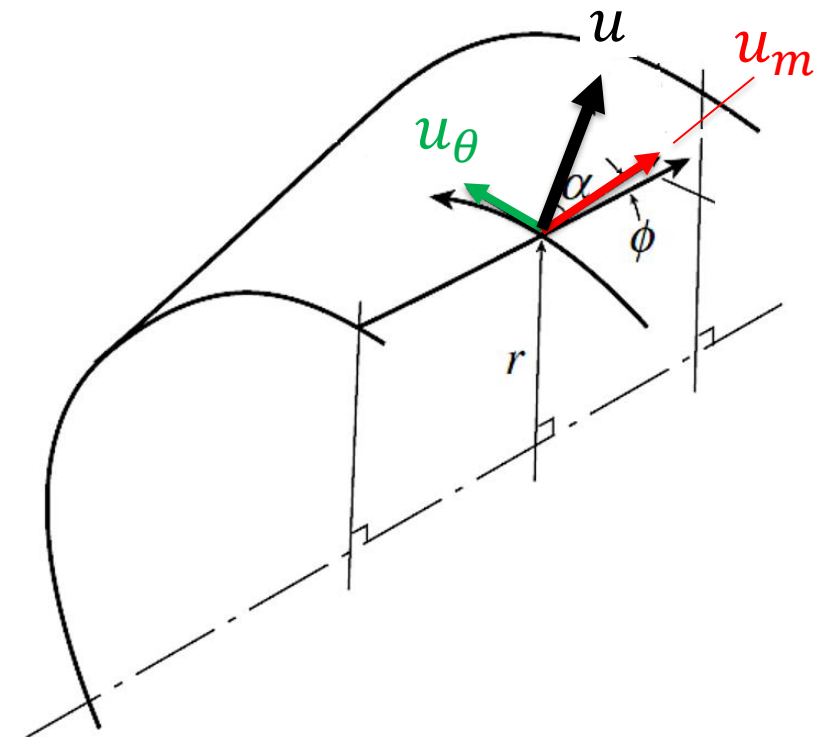
Assumption: $\gamma_{pv} = const$

Corrected mass flow per unit area (2)

$$\dot{m}_{corr} \approx \left(1 + \frac{\gamma_{pv} - 1}{2} M^2 \right) \sqrt{ \frac{M^2}{1 + \frac{\gamma_{pv} - 1}{2} M^2} - \left(\frac{u_\theta}{\sqrt{\gamma_{pv,t} Z_t R T_t}} \right)^2 }$$

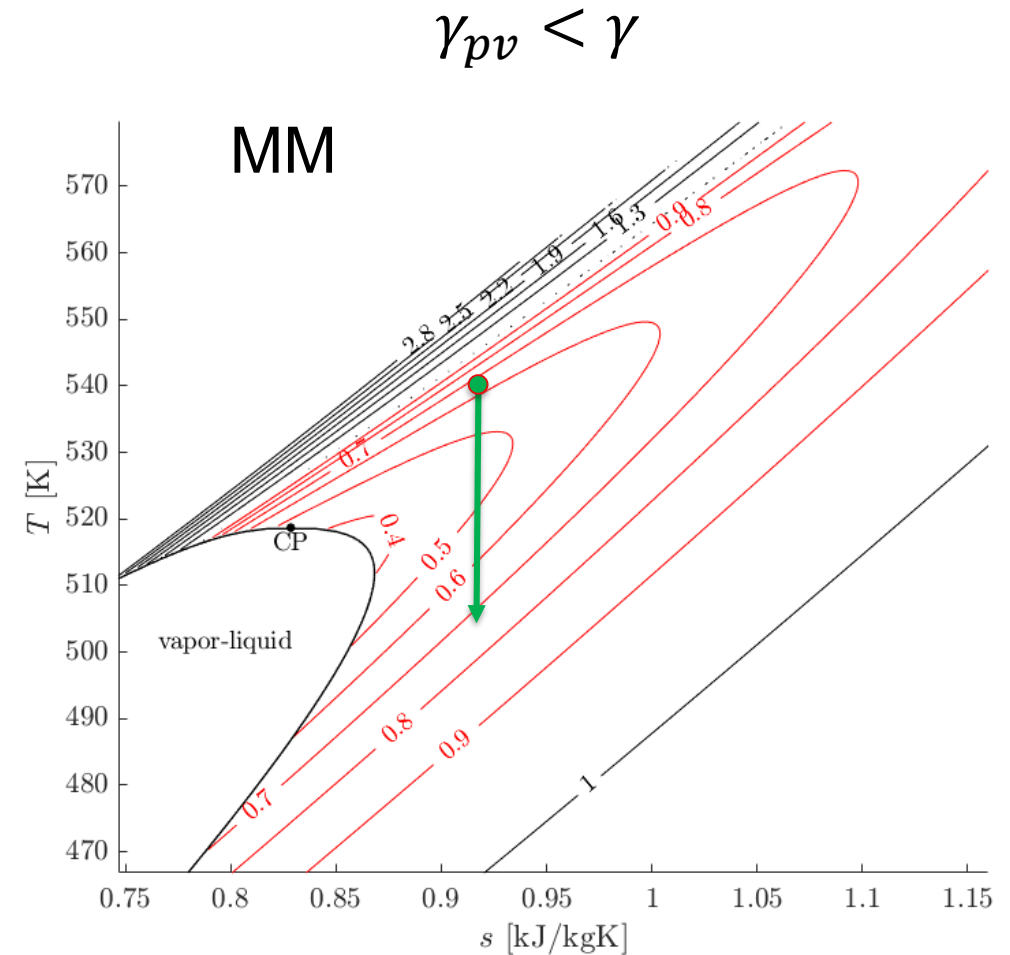
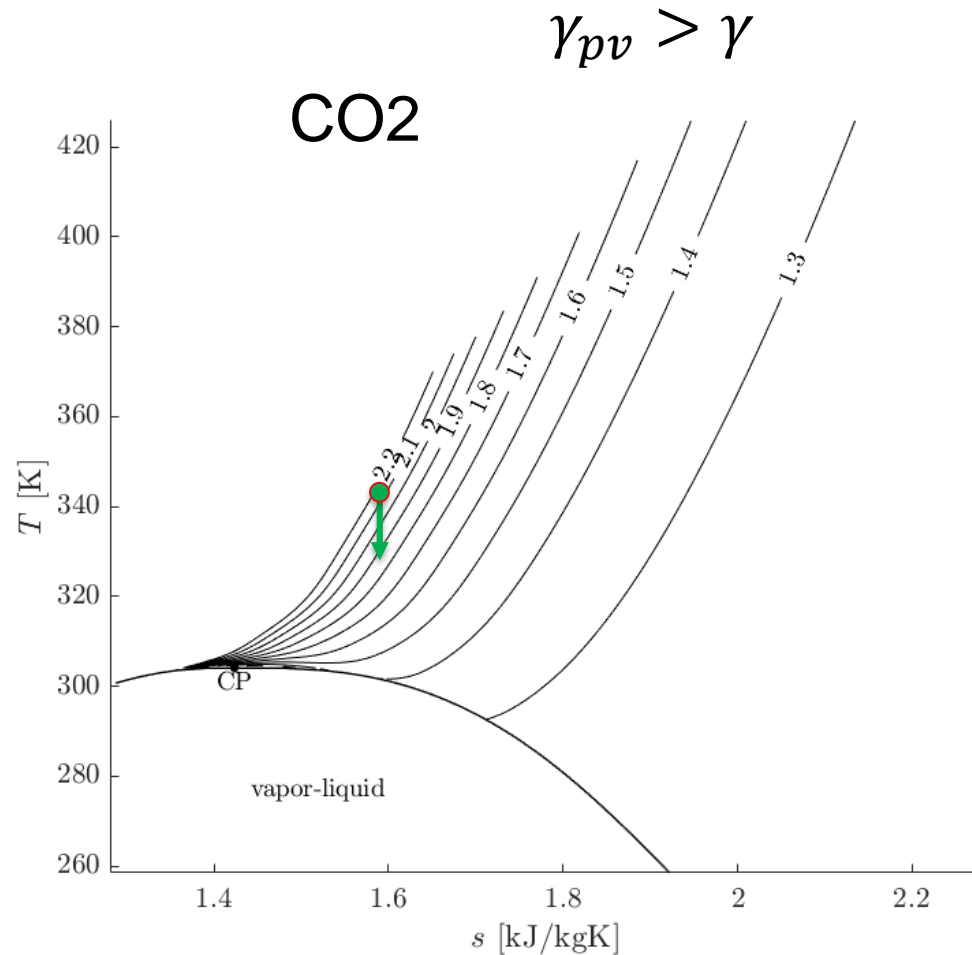
$= \hat{u}_\theta$
 swirl parameter

absolute
Mach number

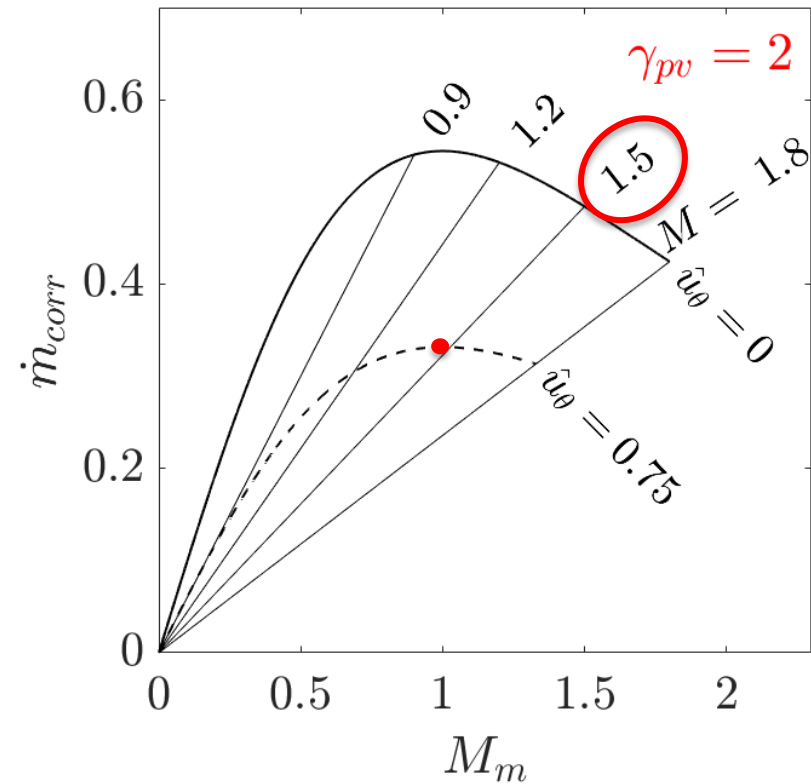


Assumption: $\gamma_{pv} = const$

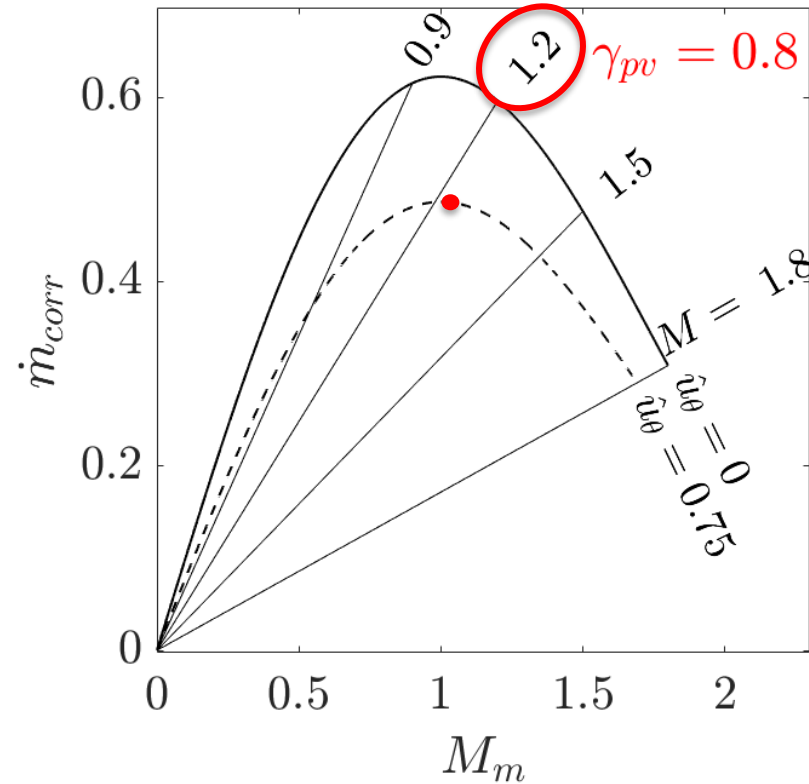
Investigated Processes



Influence of γ_{pv} on Choking



$\gamma_{pv} > \gamma$



$\gamma_{pv} < \gamma$

Choking: $M_m = 1$

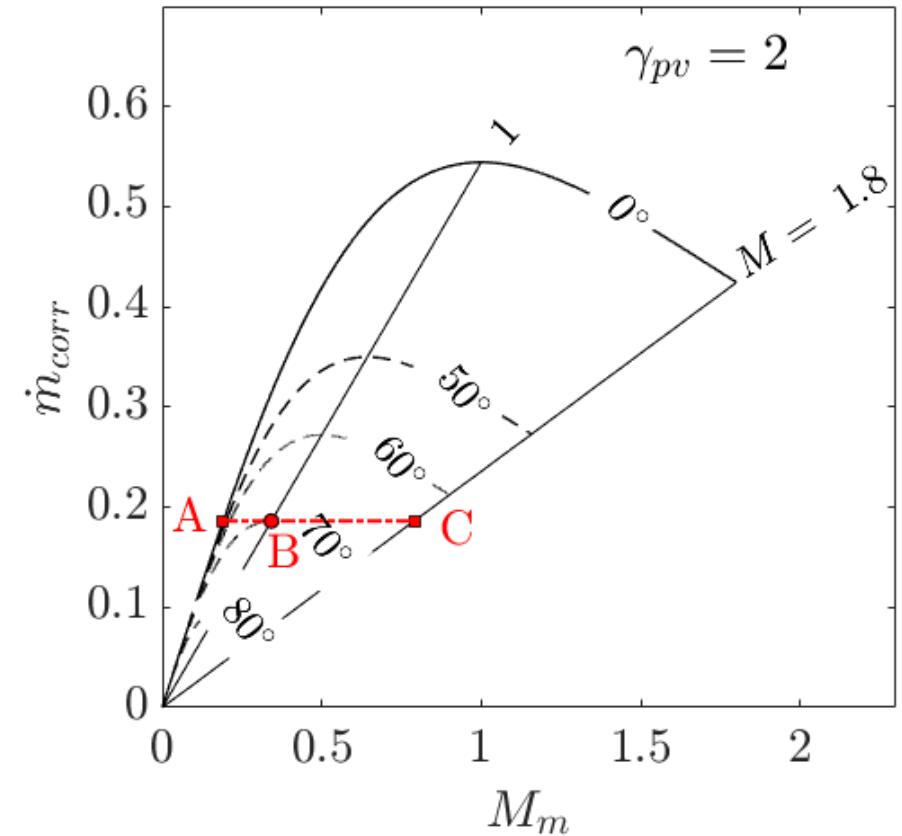
$M \uparrow$

$\gamma_{pv} \uparrow$

Exemplary Post – Expansion in Turbine

Horizontal line at constant \dot{m}_{corr} (A-B-C)

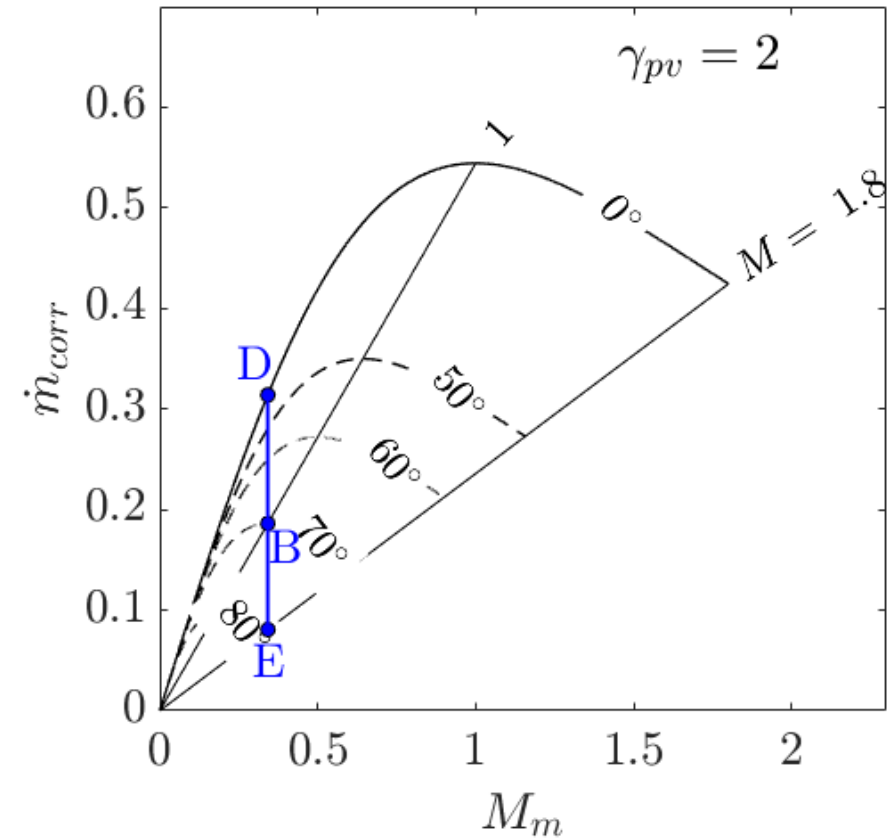
- Point B: sonic throat ($M = 1$)
- Point C: post-expansion final state ($M = 1.8$)
- **Deviation angle increases if γ_{pv} decreases**



Exemplary Expansion in Supersonic Turbine

Vertical line at constant M_m (D-B-E)

- Constant flow coefficient
 - Negligible post-expansion
 - $\Delta \dot{m}_{corr}$ increases if γ_{pv} decreases
- ↓
- Larger area variation to accommodate larger volumetric flow ratio $\alpha = \rho_{t,in}/\rho_{out}$

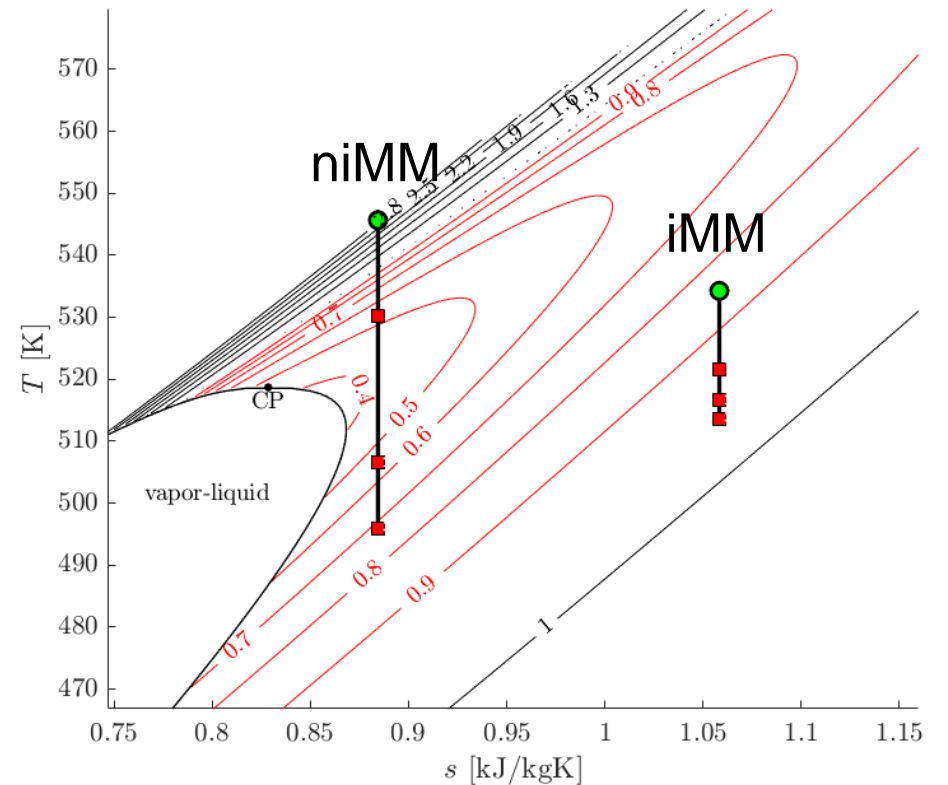


CFD Verification

Test Cases & Numerical Setting

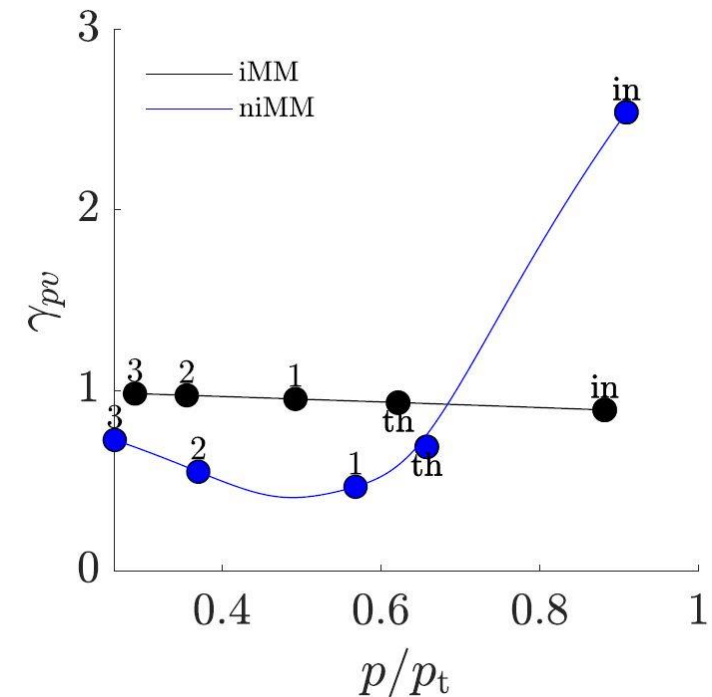
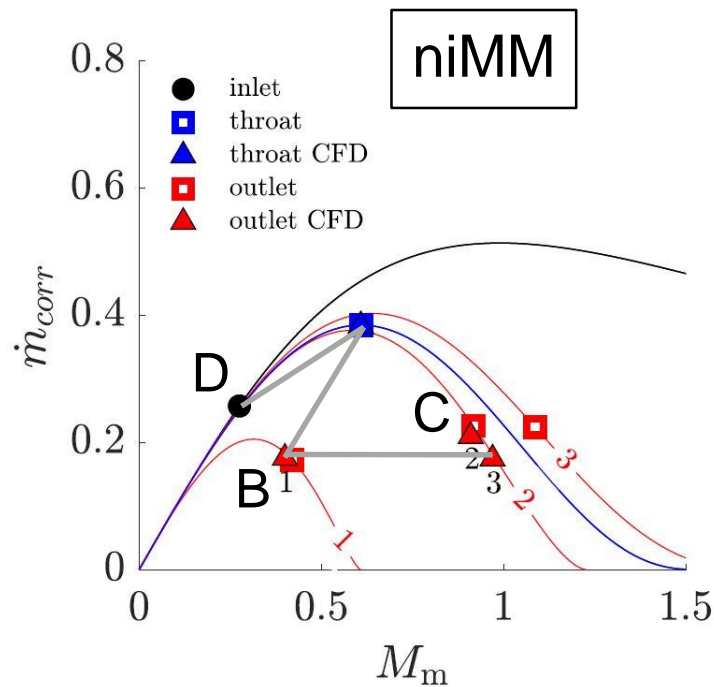
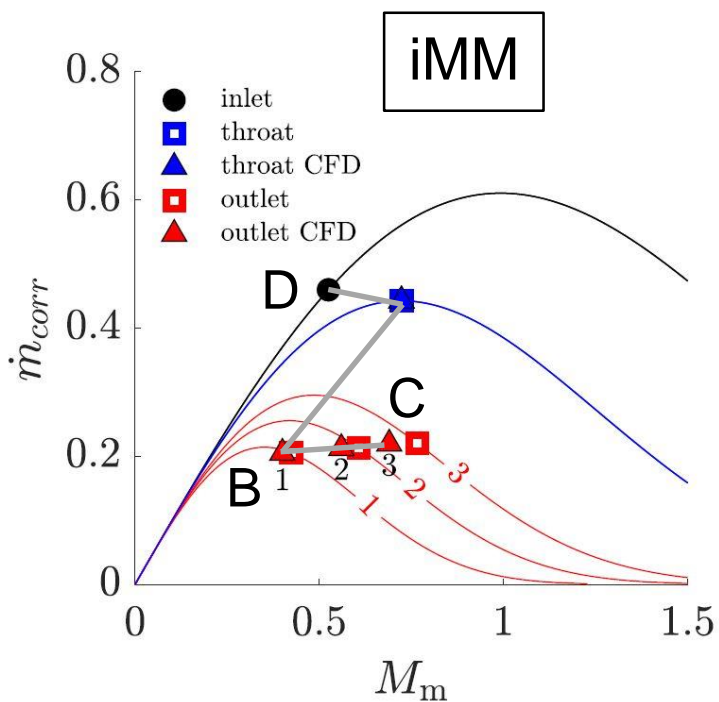
3D transonic stator vanes

- iMM: $\beta_{ts} = 2.0 - 2.8 - 3.4$
 - niMM: $\beta_{ts} = 1.8 - 2.7 - 3.8$
-
- Spatial discretization: 2nd order
 - Turbulence: $k - \omega$ SST ($y^+ \leq 1$)
 - Fluid mesh: 5M points
 - Look-up table: 2.5M (iMM) - 4M (niMM) points



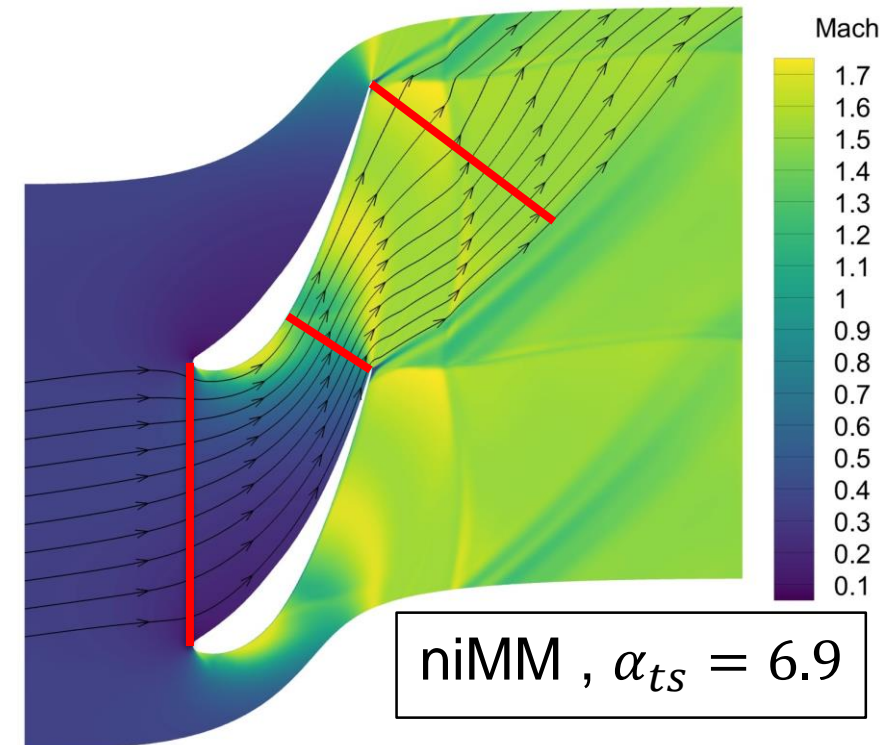
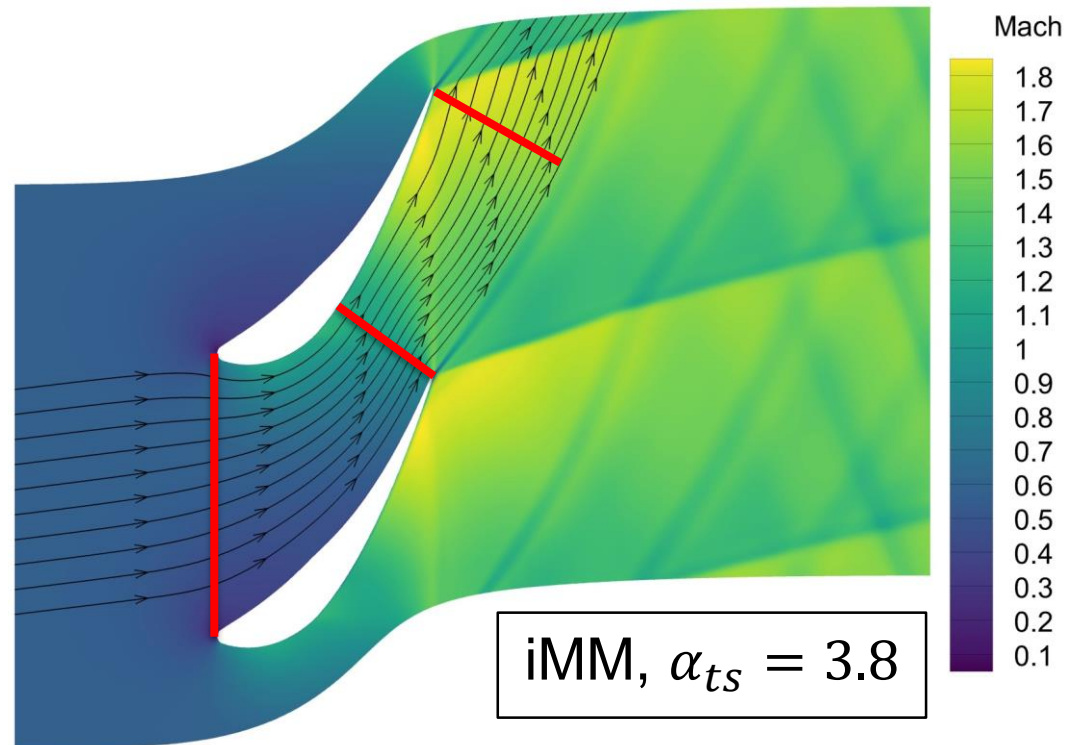
Results

- 1D model qualitatively in line with CFD if sufficiently far from choking
- Large deviation in volumetric flow ratio
 - iMM: $\alpha_{ts} = 2.2 - 3.1 - 3.8$
 - niMM: $\alpha_{ts} = 1.6 - 4.0 - 6.9$



Physical Insights

- $\gamma_{pv} < \gamma \rightarrow$ larger area variation to accommodate larger α at given β
- $\gamma_{pv} < \gamma \rightarrow$ larger flow deviation in convergent blade channels



Take-Away Messages

- Expansions characterized by $\gamma_{pv} < \gamma$ lead to **earlier choking** and **larger flow deviation** when fixing β_{ts}
- Turbines operating with flow $\gamma_{pv} < \gamma$ (ORC) more susceptible to reach **complete choking** → operability/efficiency issues
- **Research hypothesis:**
choice of **convergent-divergent** nozzle driven by ability to control flow deviation and extend operating range

Ongoing & Future Work

- Verify hypothesis by
 - Investigate expansion in convergent-divergent nozzles
- Pre-expansion at compressor inlet
- Analysis of compression processes

Further info upon request @
m.pini@tudelft.nl & co-workers!

Thank you

