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NUMERICAL INVESTIGATION OF A SUPERCRITICAL CO₂ CENTRIFUGAL COMPRESSOR WITH AN IN-HOUSE DENSITY BASED COMPRESSIBLE CFD SOLVER

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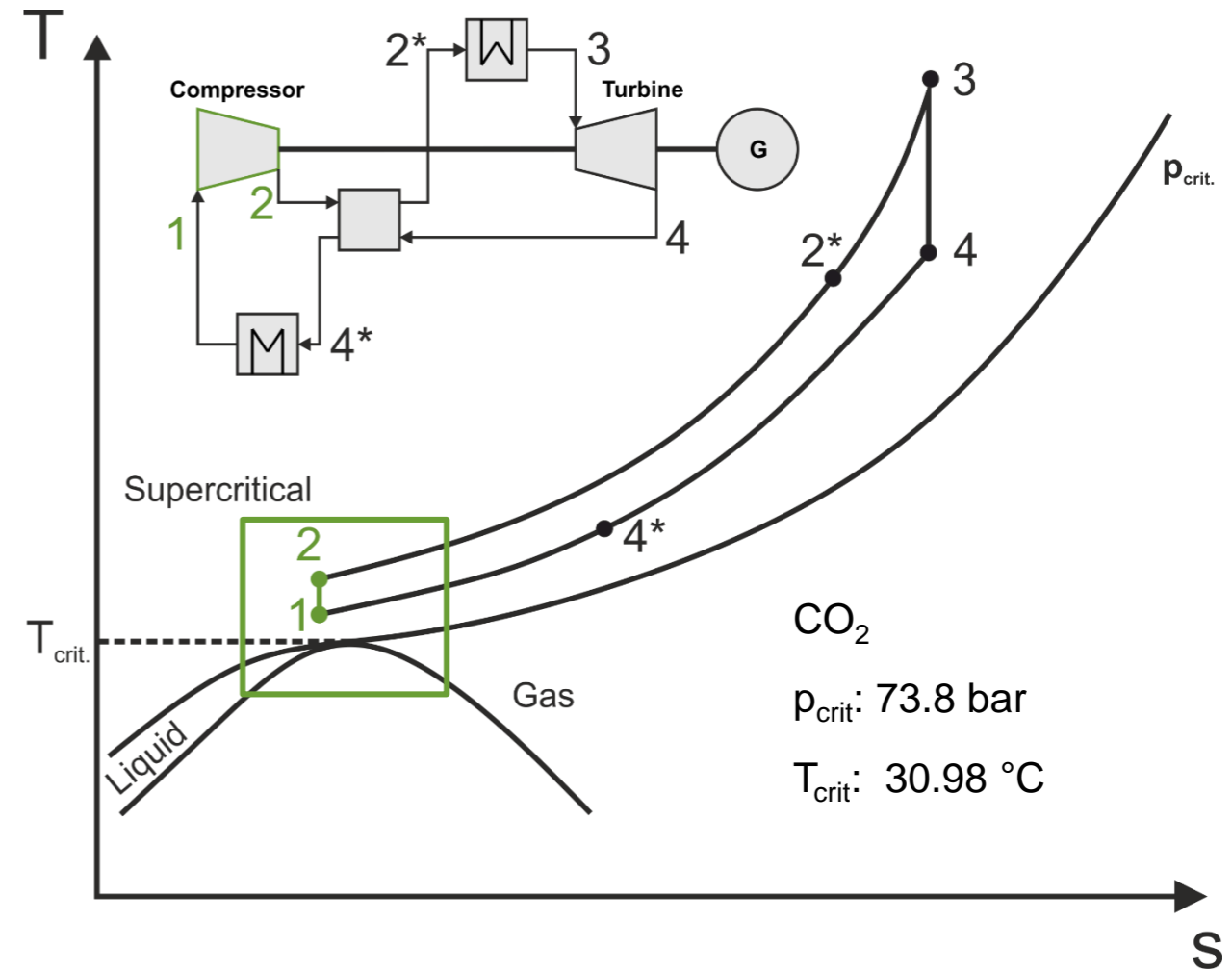
sCO₂-Power Systems

Characteristics

- Low compression work
- Small scale of turbomachinery
- Comparatively high efficiency in the mild turbine inlet temperature range (450 - 600°C)

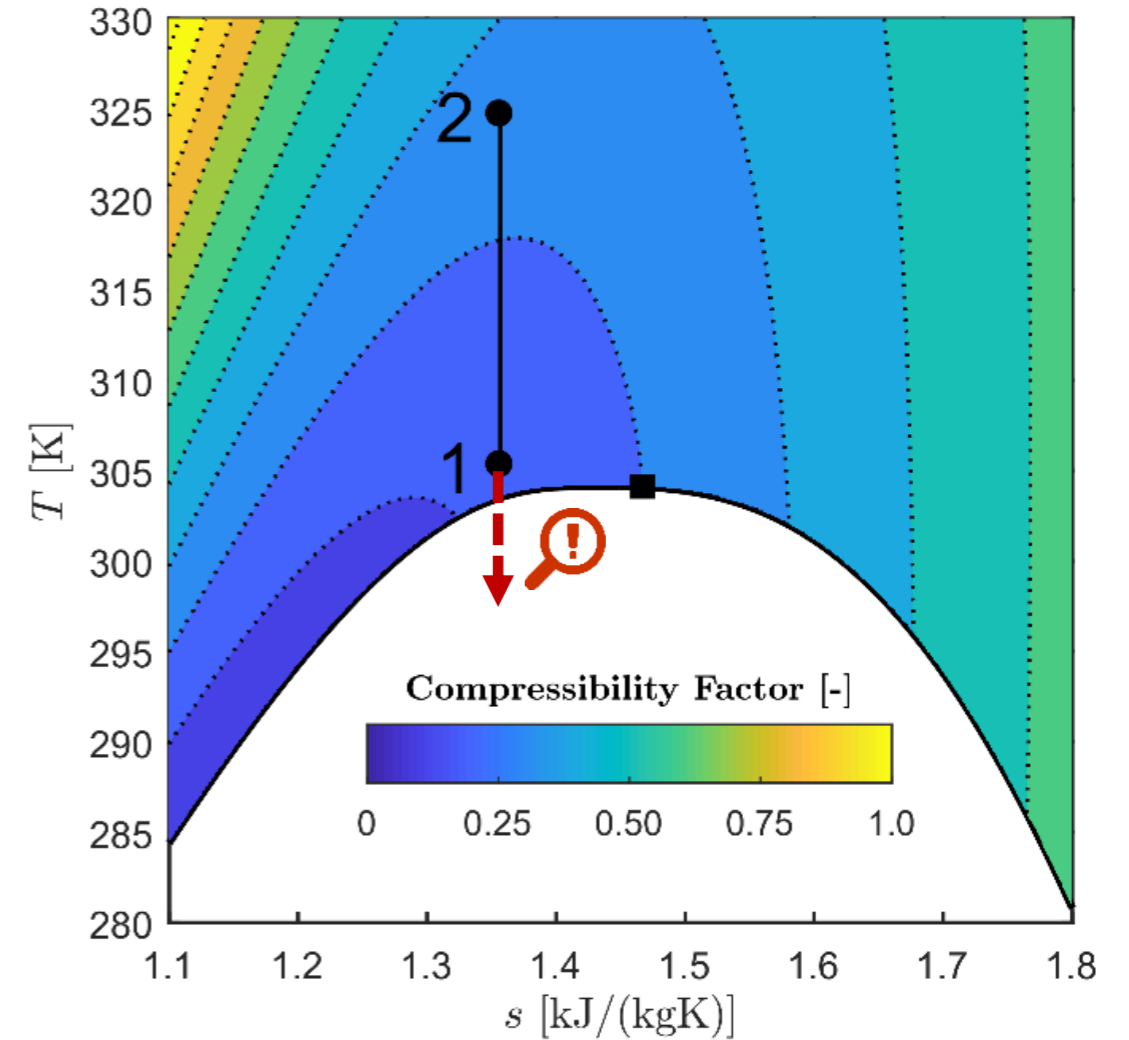
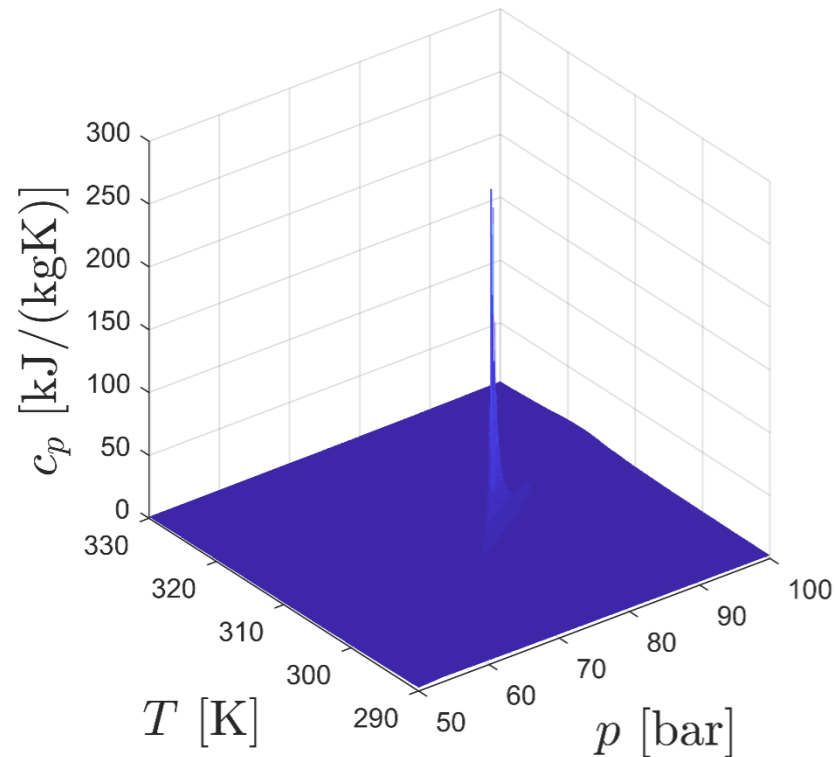
Application Areas

- Nuclear energy
- Topping cycle for fossil fueled power plants
- Bottoming cycle for gas combined cycles
- Exhaust/waste heat recovery
- Renewable energy



Challenges for compressor design and analysis

- Non-ideal thermophysical properties
- Possibility of two-phase flows (locally)
- Rapidly changing fluid properties in the vicinity of the critical point



Scope of work

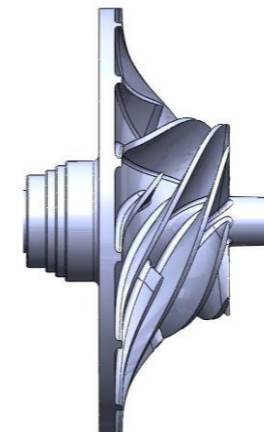
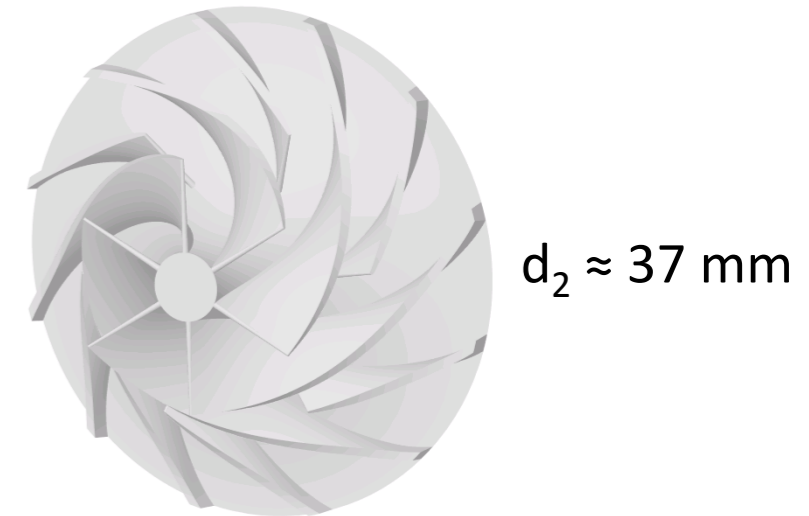
- Extension of the in-house CFD solver to account for thermophysical properties of sCO₂ with high degree of accuracy and numerical stability
 - Span-Wagner multiparameter EOS is too computationally expensive
 - Integration via Spline Based Table Lookup Method [1,2]
- Validation of the CFD framework for sCO₂ compressor performance and flow field assessments
 - Lack of fully documented experimental test cases
 - Investigation of a geometry based on the main dimensions of the SNL main compressor
- Development and validation of a sCO₂ compressor performance meanline analysis tool
 - Further reference for performance assessments
 - Breakdown of individual loss contributions

- 1 Motivation
- 2 Test Case Description
- 3 Methodology
- 4 Results
- 5 Conclusion and Future Work

SNL Compressor

- Candidate geometry based on main dimensions of the SNL compression test-loop main compressor
 - Backward swept impeller with splitter blades and a channel diffuser
 - Design specifications:
 $50 \text{ kWe} / 75 \text{ krpm} / 3,54 \text{ kg}\cdot\text{s}^{-1} / \eta_{ts} \approx 66\% / \pi = 1,8$
 $T_{0,in}/T_c \approx 1.004, p_{0,in}/p_c \approx 1.04$
- Restrictions
 - Main dimensions reported partially
 - No blade coordinates accessible
→ Correct reconstruction of blade angle and thickness distribution is not possible
- Simplifications in this preliminary study
 - No tip clearance modeled
 - No diffuser modeled

CAD model of the investigated impeller geometry



Part drawing and photograph of the SNL main compressor [3]

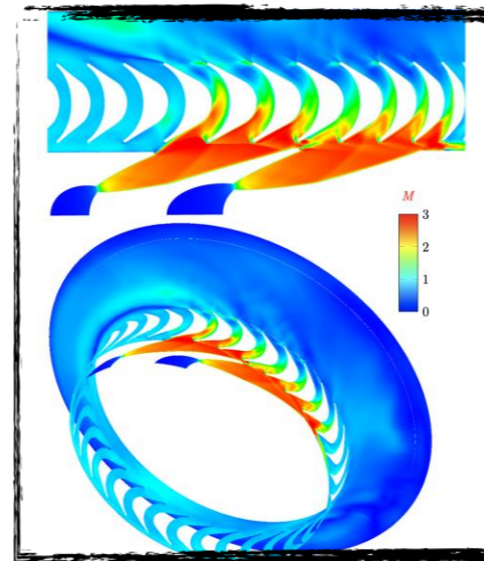
CFD Solver

- In-house density based solver
- Hybrid parallelization
- Complex thermodynamic applications

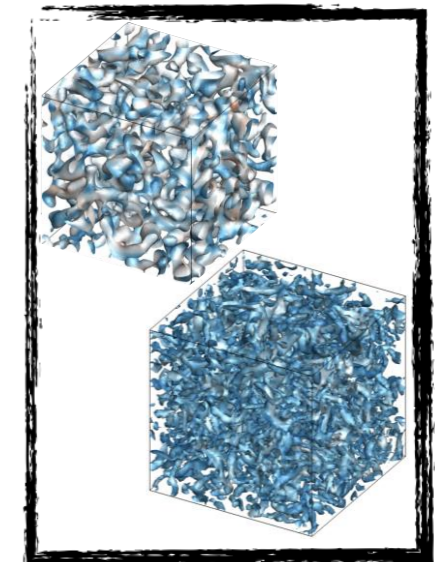
CONDENSING WET STEAM (LES) [5]



ORC [4]



DNS/LES



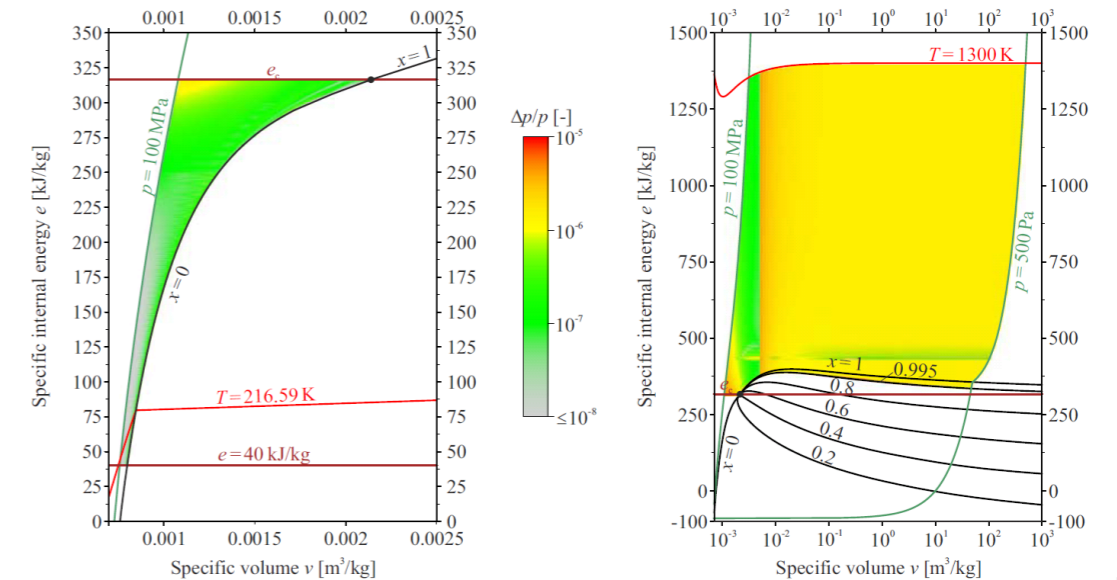
Real Gas Property Tabulation

- Spline Based Table Lookup Method (SBTL) [1,2]
 - Biquadratic polynomial spline interpolation
 - Continuous first derivatives
 - Numerically fast and consistent backward functions
 - Constructed on piecewise equidistant nodes
- Tabulated data is based on the Span-Wagner reference EOS [6] and correlations for viscosity and thermal conductivity [7,8]
- Permissible deviations are within uncertainties of the underlying equations/correlations

[1] M. Kunick. "Fast Calculation of Thermophysical Properties in Extensive Process Simulations with the Spline-Based Table Look-Up Method (SBTL)". Fortschrittberichte VDI, Nr. 618, Reihe 6, Energietechnik, 2018.

[2] M. Kunick et al. "CFD Analysis of Steam Turbines With the IAPWS Standard on the Spline-Based Table Look-Up Method (SBTL) for The Fast Calculation of Real Fluid Properties". Proceedings of ASME Turbo Expo 2015, ASME Paper No. GT2015-43984, 2015.

Permissible deviations of spline-functions (CO₂ application)



[16]

SBTL function	liquid region	gas region
$p(v,e)$	$p \leq 2.5 \text{ MPa}$ $ \Delta p/p < 0.001 \%$ $p > 2.5 \text{ MPa}$ $ \Delta p < 0.5 \text{ kPa}$	$ \Delta p/p < 0.001 \%$
$T(v,e)$	$ \Delta T < 1 \text{ mK}$	$ \Delta T < 1 \text{ mK}$
$s(v,e)$	$ \Delta s < 10^{-6} \text{ kJ/(kg K)}$	$ \Delta s < 10^{-6} \text{ kJ/(kg K)}$
$w(v,e)$	$ \Delta w/w < 0.001 \%$	$ \Delta w/w < 0.001 \%$
$\eta(v,e)$	$ \Delta \eta/\eta < 0.001 \%$	$ \Delta \eta/\eta < 0.001 \%$
$\lambda(v,e)^a$	$ \Delta \lambda/\lambda < 0.001 \%$	$ \Delta \lambda/\lambda < 0.001 \%$

[16]

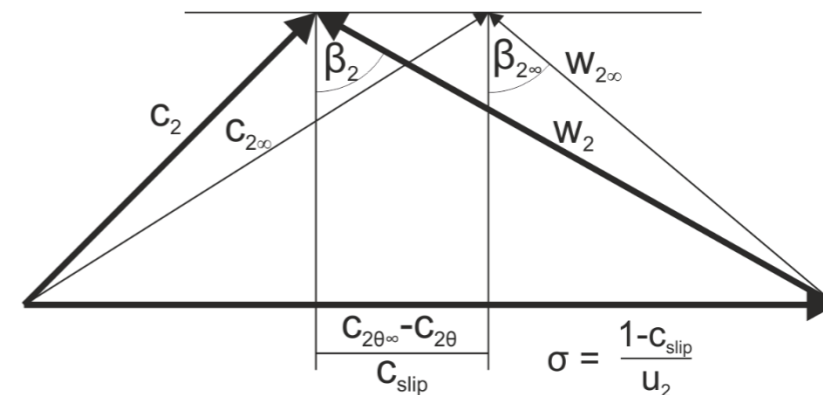
Meanline Analysis Method

- Single-zone modeling approach
- Implemented in PYTHON with direct calls to the CoolProp [9] property library
- Applied loss model set is based on an optimised and validated set of internal and external loss for conventional centrifugal compressors (Oh et al. [10])
- Wiesner slip correlation [11] is applied

$$\sigma = 1 - \frac{\sqrt{\cos \beta_{2,bl}}}{Z_{bl}^{0.7}} \quad (\text{meridional angle system})$$

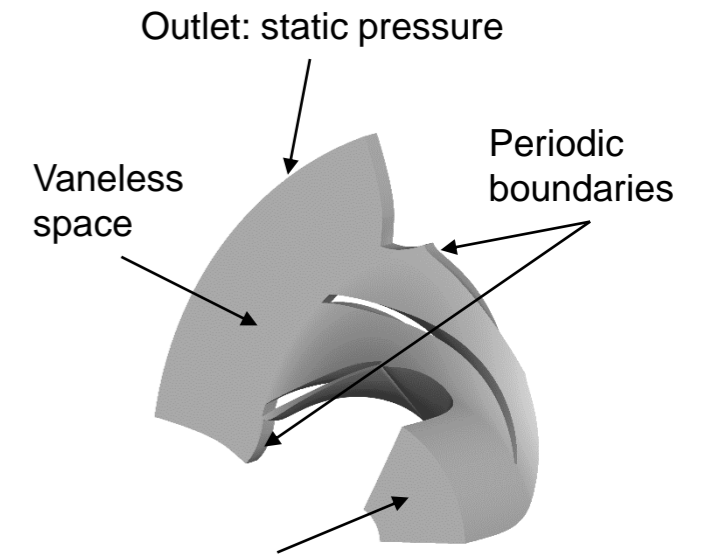
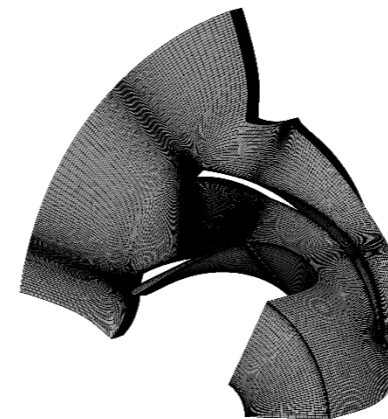
$$W_{Euler} = u_2 c_{2\theta} - u_1 c_{1\theta} = u_2 (\sigma u_2 + c_{2m} \tan \beta_{2,bl})$$

Loss mechanism	Loss model	Reference	
internal	Incidence	$\Delta h_{inc} = \sigma \cdot \frac{\sin^2(\beta_1 - \beta_{1,bl}) w_1^2}{2}$	Conrad et al. [9]
	Blade loading	$\Delta h_{bl} = 0.05 \cdot D_f^2 \cdot u_2^2$	Coppage et al. [10]
	Skin friction	$\Delta h_{sf} = 2 c_f \frac{L_{fl}}{d_{hb}} \bar{w}^2$	Jansen [15]
	Clearance	$\Delta h_{cl} = u_2^2 0.6 \frac{\delta \cdot c_{2\theta}}{b_2 u_2} \times \sqrt{\frac{4\pi}{b_2 Z_{bl}} \left[\frac{r_{1l}^2 - r_{1h}^2}{(r_2 - r_{1l})(1 + \rho_2/\rho_1)} \right] \frac{c_{2\theta} c_{1m}}{u_2 u_2}}$	Jansen [15]
Mixing	$\Delta h_{mix} = \frac{1}{2} \frac{c_2^2}{1 + (c_{2\theta}/c_{2m})^2} \cdot \left[\frac{1 - \epsilon - B}{1 - \epsilon} \right]$	Johnston & Dean [17]	
external	Disk friction	$W_{df} = f_{df} \frac{\bar{\rho} r_2^2 u_2^3}{4\dot{m}}$	Daily & Nece [11] as quoted by Oh et al. [23]
	Recirculation	$W_{rc} = 8 \cdot 10^{-5} \sinh(3.5 \alpha_2^3) D_f^2 u_2^2$	Oh et al. [23]
	Leakage	$W_{lk} = \frac{\dot{m}_{cl} u_{cl} u_2}{2\dot{m}}$	Aungier [5]



Numerical Setup

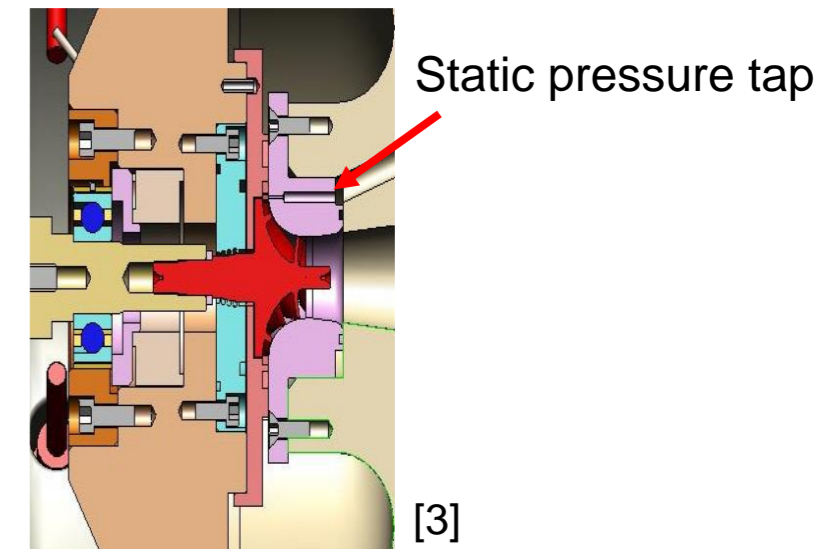
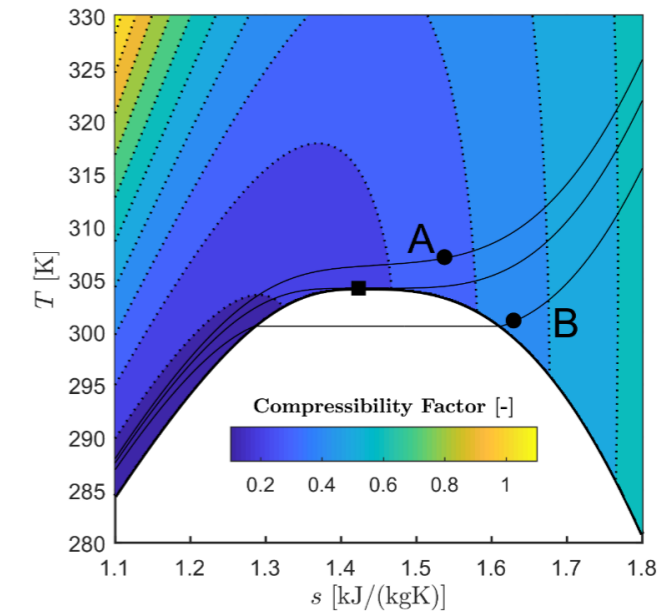
- Steady state RANS simulations
 - Second order AUSM+scheme [12]
 - Implicit LUSGS scheme
- Spalart-Allmaras turbulence model [13]
- Homogenous equilibrium mixture (HEM)
- Block structured mesh
 - No wall functions: $y^+ < 5$
 - ≈ 1.7 mio. cells for single main + splitter blade
- Single domain, no interface



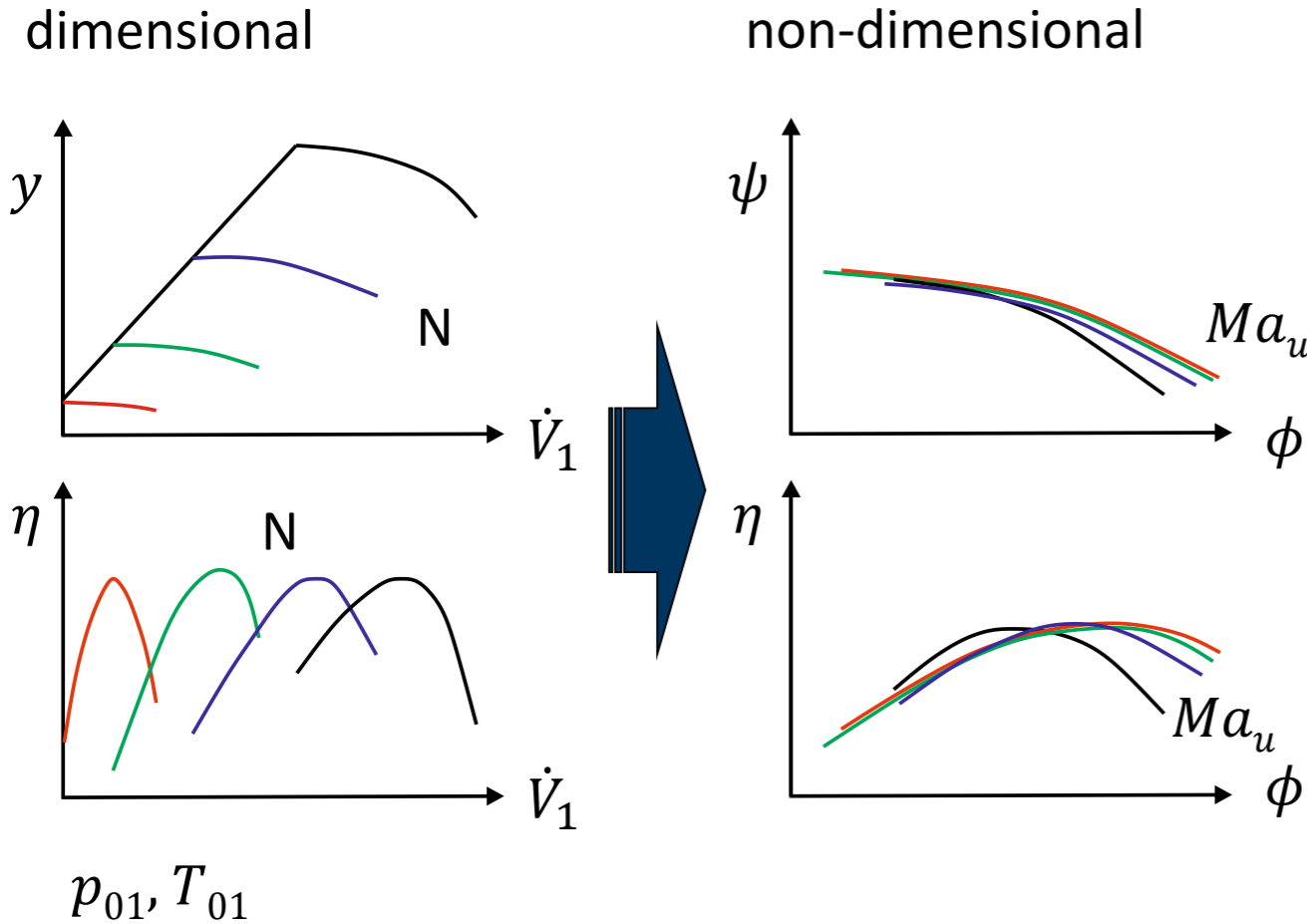
Inlet:
- Total temperature
- Total pressure
- Uniform and normal flow

Investigated Compressor Operating Conditions

- Based on experimental campaigns of Wright et al. [3,14] and Fuller & Eisemann [15]
 - A: Near-Critical Inlet State
77.50 bar, 307 K
 - B: Gaseous Inlet State,
Potentially relevant during cycle startups
67.93 bar, 301 K
- 50 krpm speedline calculation (off-design)
→ most data available
- Experimental performance assessments (total-to-static) are interpreted to be associated with the impeller wheel (static pressure tap at impeller exit)
- Strong variation of experimental inlet states
→ corrected and non-dimensional performance map representation



Performance Assessment



$$\phi = \frac{4\dot{V}_1}{\pi d_2^2 u_2} \quad \text{Flow Coefficient}$$

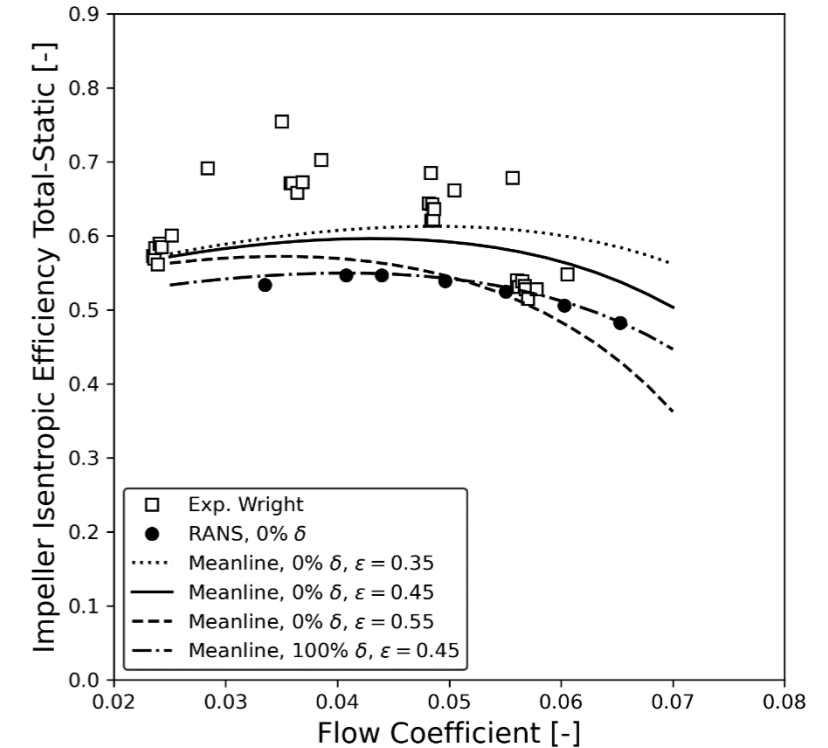
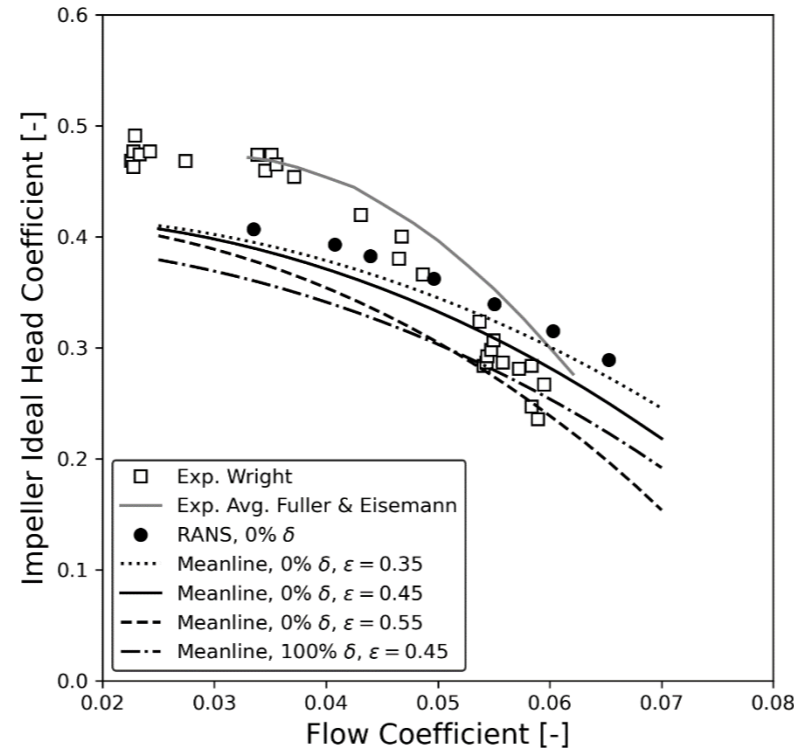
$$\psi = \frac{h_{2s} - h_{01}}{u_2^2} \quad \text{Head Coefficient}$$

$$\eta_s = \frac{h_{2s} - h_{01}}{h_{02} - h_{01}} \quad \text{Isentropic Efficiency}$$

Compressor Performance

State A: Near Critical Operation

- RANS
 - Flatter head characteristic
 - Reduced efficiencies
 - Surge comparable
- Meanline
 - Slope of head curve shows better agreement with RANS
 - Sensitive towards inputs of the parameter ε for high flow coefficients
 - Consideration of tip clearance: 7-14 % decreased head generation, 4-6 percentage points decreased efficiency

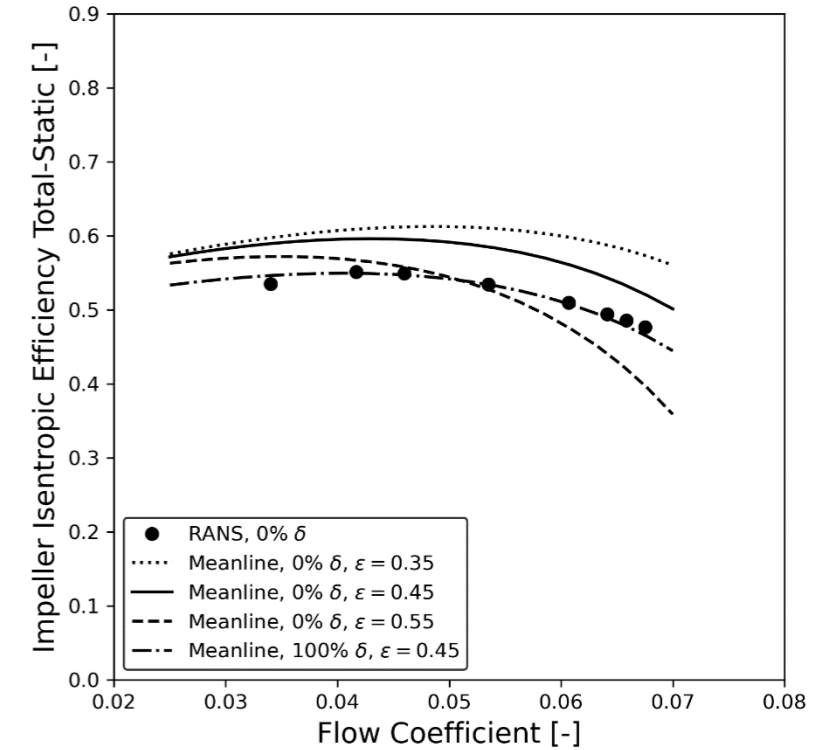
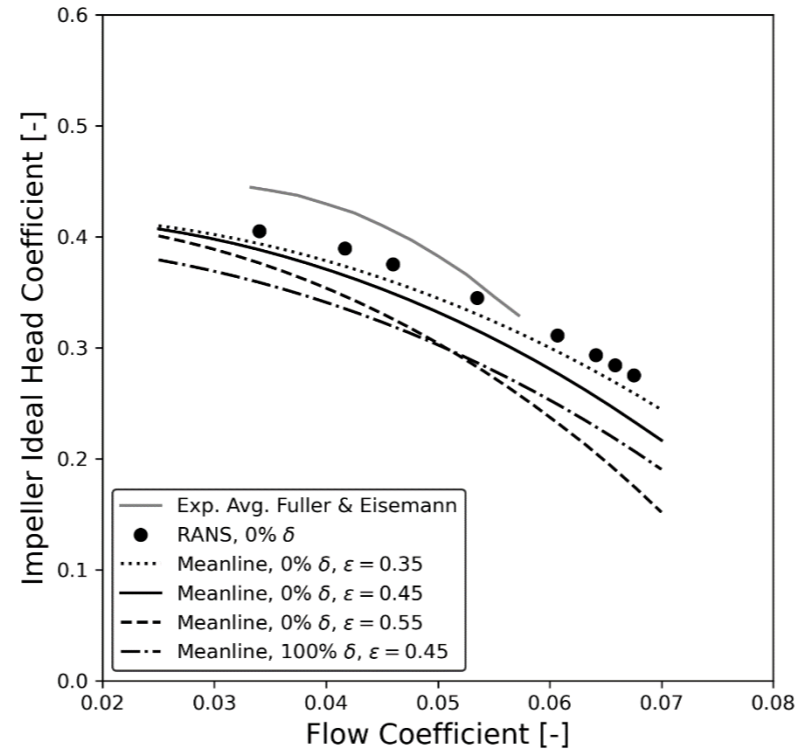


ε : fraction of blade to blade space occupied by the wake
(Mixing loss model of Johnston & Dean)

Compressor Performance

State B: Gaseous Operation

- Almost no difference compared to state A
→ High degree of machine similitude



ε : fraction of blade to blade space occupied by the wake
(Mixing loss model of Johnston & Dean)

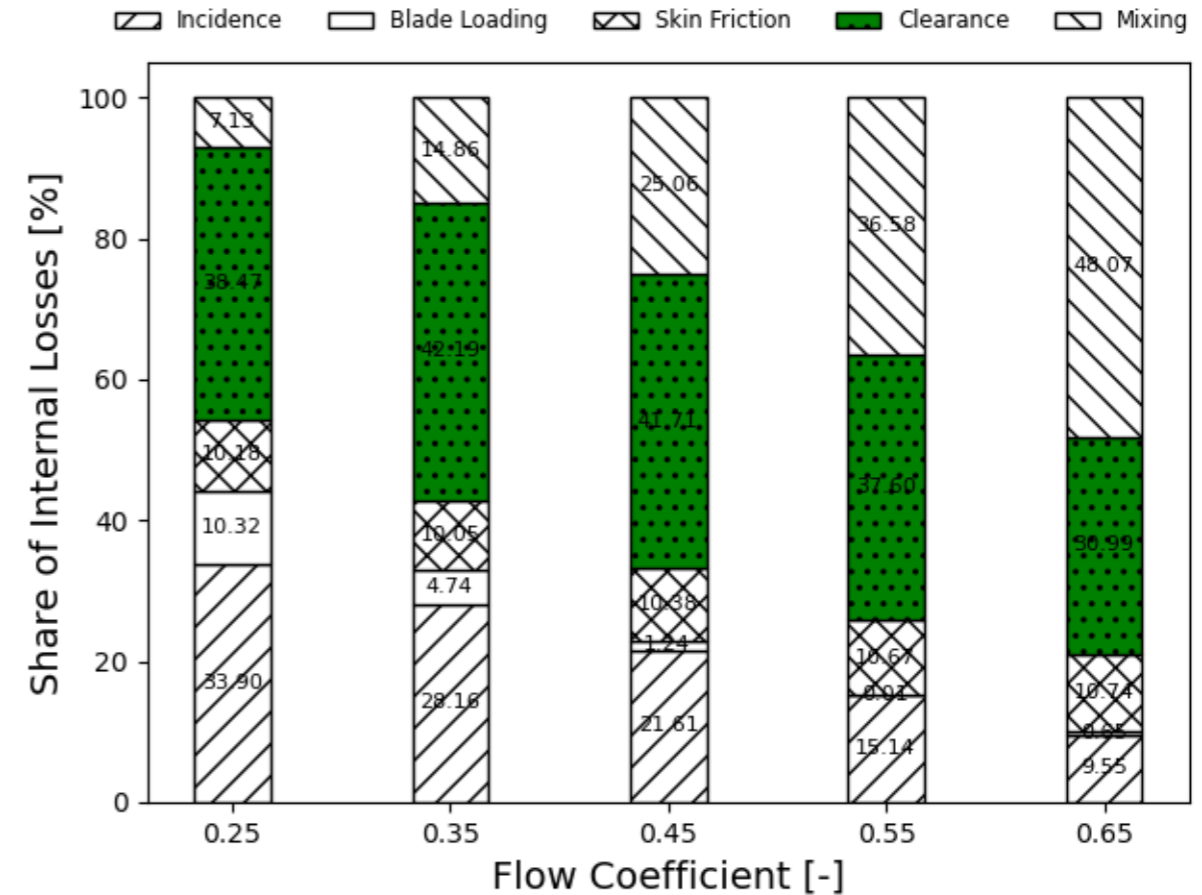
Meanline Loss Distribution

- Clearance loss with significant share over the entire flow range ($\approx 40\%$)

$$\text{SNL: } \frac{\delta}{d_2} \approx 0.007$$

$$\text{Eckardt Impeller: } \frac{\delta}{d_2} \approx 0.001$$

State A



Meanline Loss Distribution

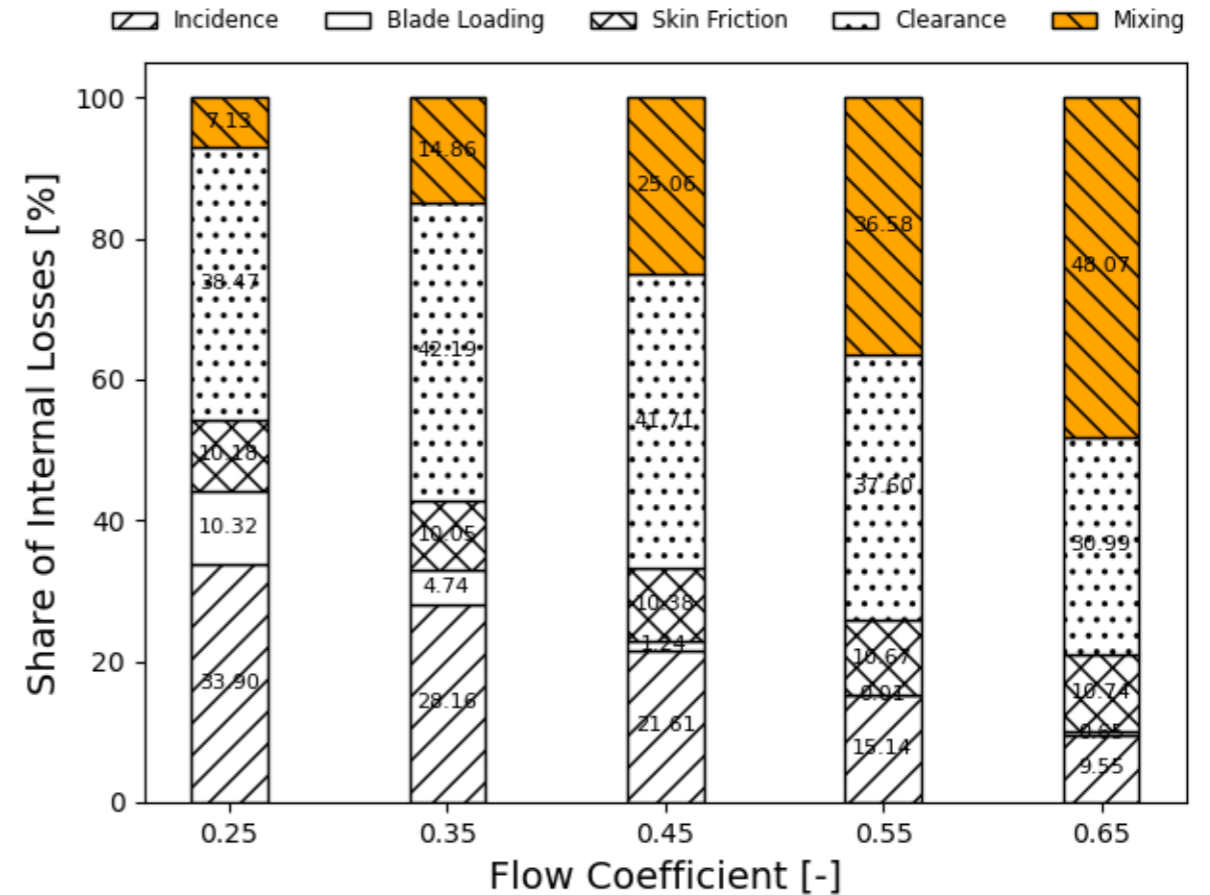
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- Wake mixing losses dominant at high flow coefficients
 - Explains high sensitivity of ε in performance curve derivation

State A



Meanline Loss Distribution

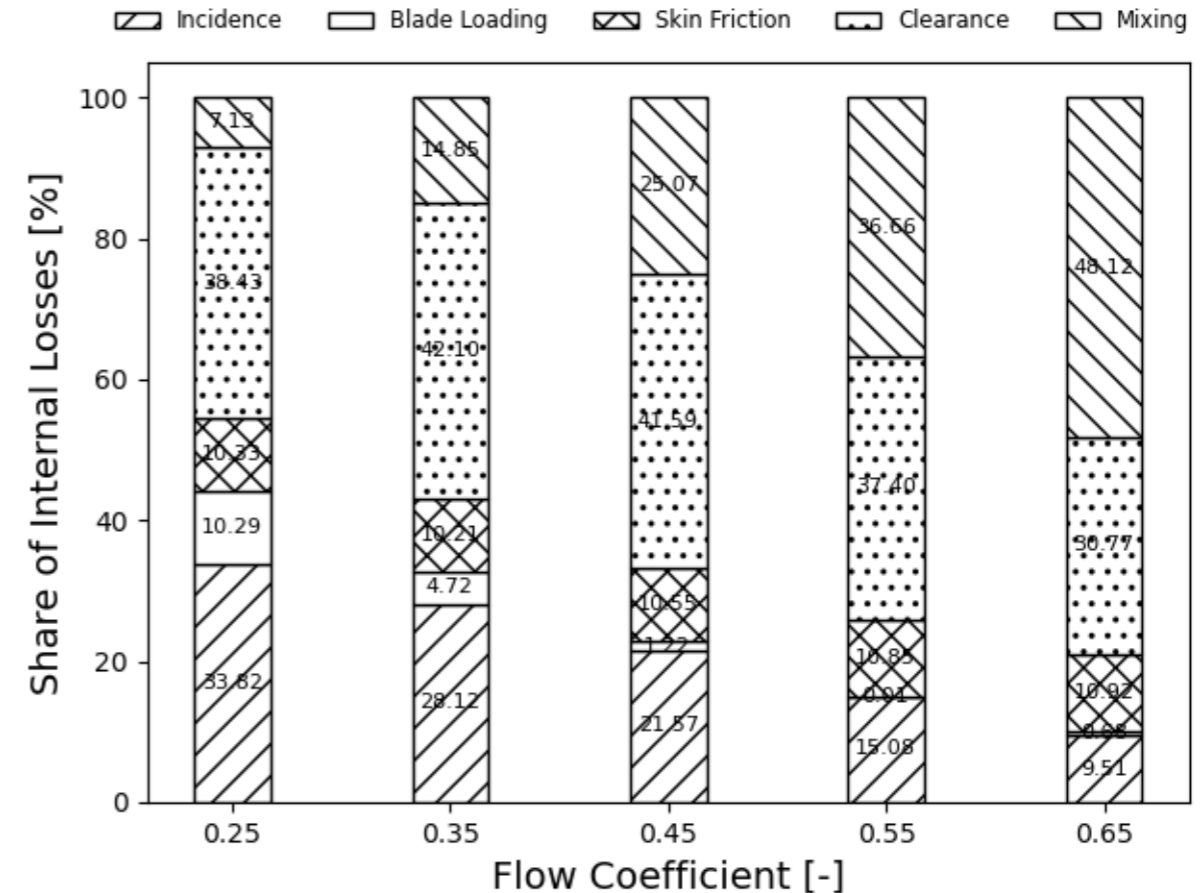
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- Wake mixing losses dominant at high flow coefficients
 - Explains high sensitivity of ε in performance curve derivation
- Shares at state B almost identical due to similitude of velocity triangles

State B



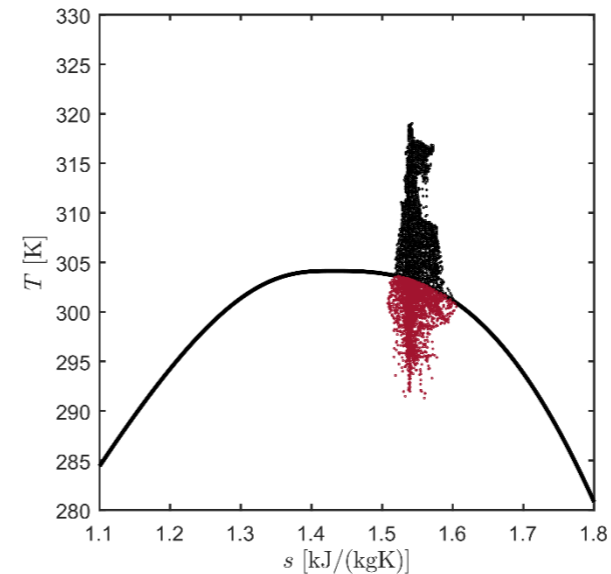
Vapour-Liquid Region

- Points within the vapour-liquid region detected for all simulations
- Located near the impeller leading edges
- Caused by flow acceleration at the suction side
- Small volume fraction of entire domain
 - State A simulations: < 0.02 %
 - State B simulations: < 1.1 % (closer location to the VL-region)

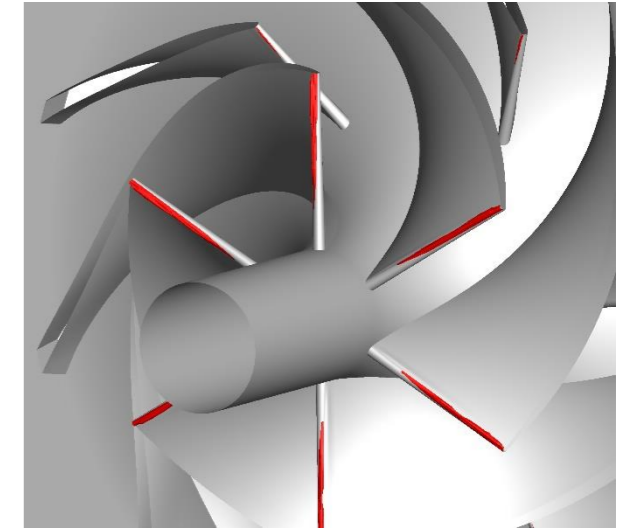
Current limitations:

- Simulations do not account for metastable states
- Non-equilibrium condensation is not modeled

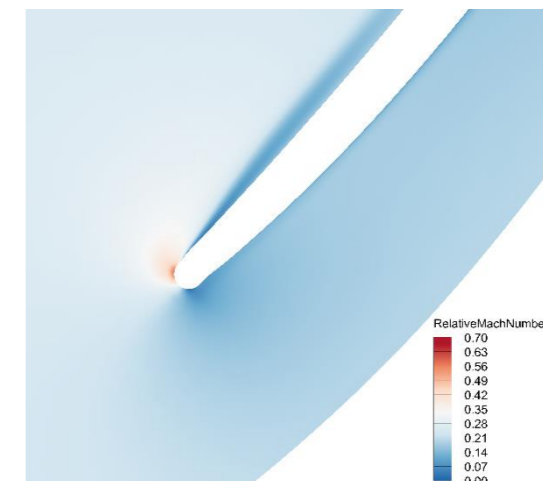
scatter plot of solution domain



isocontours of points within the VL-region

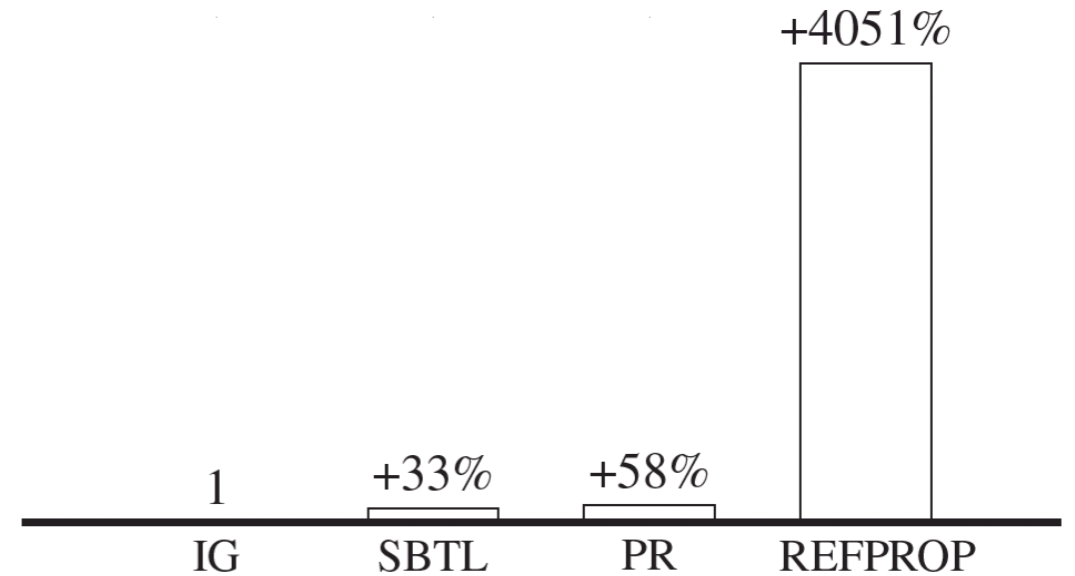


contours of relative Mach number at 75 % span



Benchmark

- IG and PR simulations performed without tabulation
- Direct calls to REFPROP library
- Further reduction of overhead might be expected in future versions of the SBTL library (2 % overhead demonstrated for the highly optimised steam version)



[16]

Conclusion

- Reasonable performance metrics are derived for two operating states despite approximations of the candidate compressor geometry
- High degree of machine similitude observed for both operating states
 - Finding suggests that non-dimensional sCO₂ performance testing could be numerically and practically conducted at inlet states with less pronounced gradients in thermophysical properties
- Compressor operation close to the VL-region might potentially lead to condensation of a small volumetric region
- Meanline loss distributions indicate tip clearance as a dominant loss contributing factor over the entire operating range
- CFD Framework comprising the SBTL library allows for accurate calculations within the range of uncertainties of the EOS at comparatively low computational overhead (33 % compared to IG)

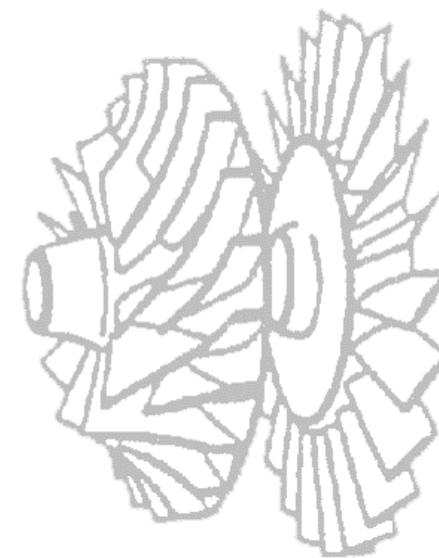
Future Work

- Integration of metastables states and assessment of non-equilibrium condensation
- Extension of the geometry to account for the channel diffuser

THANK YOU

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- [1] M. Kunick. "Fast Calculation of Thermophysical Properties in Extensive Process Simulations with the Spline-Based Table Look-Up Method (SBTL)". Fortschrittberichte VDI, Nr. 618, Reihe 6, Energietechnik, 2018.
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- [3] S. A. Wright et al. "Operation and Analysis of a Supercritical CO₂ Brayton Cycle". SANDIA REPORT SAND2010-0171, Sandia National Laboratories, 2010.
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- [12] P. Post and F. di Mare. "Highly Efficient Euler-Euler Approach for Condensing Steam Flows in Turbomachines". GPPS Montreal 18. Montreal, Canada, 2018.
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- [15] R. L. Fuller and K. Eisemann. "Centrifugal Compressor Off-Design Performance for Super-Critical CO₂". Supercritical CO₂ Power Cycles Symposium. Boulder, Colorado, USA, 2011.
- [16] R. E. Karaefe et al. "Numerical Investigation of a Centrifugal Compressor for Supercritical CO₂ Cycles". Proceedings of ASME Turbo Expo 2020. ASME Paper No. GT2020-15194, 2020.