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Computing a global optimal solution for energy supply and storage of the future The reason reduced models are unavoidable

Power Web Conference

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- different voltage
- transmission system operator's main concern is stability and security of the system in case of contingencies
- the distribution system operator aims to exploit inherent flexibilities
- make the flexibility from the distribution grid available within the whole network
- don't neglect the dynamics











- Simulation of Energy
- Projects that develop new mathematics
- application in power and gas
- Modeling, Simulation and Optimization
- no software, no lab experiments, no financial markets expert
- however regulatory settings should be considered in the modeling



Acknowledgments and Collaborations

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- 1. Global Point of View
- 2. Power flow equation
- 3. Optimization problem
- 4. Numerical simulations



Optimization and Optimal Control

Global Optimal Solution needs an objective function f(x)

- Monetary cost
- Environmental impact
- Societal impact



What is x and what are the constraints on x?



Optimal Battery Control in the Hierarchical Power Grid









- time discrete system
- battery control (charging and discharging)
- only active power demand is considered
- peak shaving could be one optimization goal
- time horizon is important





Figure: The 33-bus distribution grid used as test instance (left), the identified load node clusters (middle), and the surrogate model (right) obtained with the identified clustering.

Two purposes: faster computation and secure communication

¹Mlinarić, P., Ishizaki, T., Chakrabortty, A., Grundel, S., Benner, P., Imura, J. I. (2018, June). Synchronization and aggregation of nonlinear power systems with consideration of bus



- Batteriesteuerung (laden/entladen)
- "peak shaving" als Optimierungsziel
- MPC Zeithorizont!







	cost	runtime[ms]
no contr	12,2	
ADMM	4,4	2.5
RBFs	4,5	1.2
NNs	5.6	0.05

Table: Comparison of the summed MPC closed-loop performance cost and runtime (per call): ADMM vs. RBFs vs. NNs.

²M Baumann, S Grundel, P Sauerteig, K Worthmann Surrogate models in bidirectional optimization of coupled microgrids at-Automatisierungstechnik 67 (12), 1035-1046, 2019



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Network Structure

Tree as graph $\mathcal{G} = (\mathcal{V}, \mathcal{E})$ with nodes \mathcal{V} and edges $\mathcal{E} \subseteq \mathcal{V} \times \mathcal{V}$

- nodes are referred to as buses, edges represent transmission lines
- low-voltage subnet is rooted at a transformer station (the slack 0)



Figure: Tree-structured graph with slack node 0 (red square) and 92 (following) nodes.



Each bus $i \in \mathcal{V}$,

- incorporates an active power demand P_i in kW,
- a reactive power demand Q_i in kvar,
- and a complex voltage $V_i = |V_i| e^{j\delta_i}$, where $|V_i|$ and δ_i denote the voltage magnitude and angle, respectively.

Typically,

- the voltage $V_0 = |V_0| \operatorname{e}^{\mathrm{j} \delta_0}$ at the slack node is given.
- For i > 0, we assume that the active power demand is known in advance.
- Given the power factor $tan(\varphi_i)$ the reactive power demand is determined by

$$Q_i = P_i \cdot \tan(\varphi_i), \qquad (1)$$

with φ_i from the complex power $S_i = P_i + jQ_i = |S_i| e^{j\varphi_i}$.



$$\begin{bmatrix} P_i - |V_i| \sum_{j=1}^n |V_j| (G_{ij} \cos(\delta_{ij}) + B_{ij} \sin(\delta_{ij})) \\ Q_i - |V_i| \sum_{j=1}^n |V_j| (G_{ij} \sin(\delta_{ij}) - B_{ij} \cos(\delta_{ij})) \end{bmatrix} = 0 \quad \forall i \in \mathcal{V},$$
(2)

Admittance Matrix

(complex) admittance $y_{ij} \in \mathbb{C}$ along the transmission line $(i, j) \in \mathcal{E}$ is encoded via the bus admittance matrix $Y \in \mathbb{R}^{n \times n}$ given by

$$Y_{ij} = \begin{cases} y_i + \sum_{k \in \mathcal{V} \setminus \{i\}} y_{ik}, & \text{if } i = j \\ -y_{ij}, & \text{else.} \end{cases}$$

- the so-called shunt admittance, y_i is omitted.
- Y = G + jB with matrices $G = (G_{ij}), B = (B_{ij}) \in \mathbb{R}^{n \times n}$, which are parameters of the system.
- (2) consists of 2*n* equations with 4*n* variables namely $(|V_i|, \delta_i, P_i, Q_i)^{\top} \in \mathbb{R}^4$
- $\delta_{ij} = \delta_i \delta_j$ denotes the angle difference for $i, j \in \mathcal{V}$.



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Line Loss

The transportation of energy comes along with losses depending on the length and material of the line and the amount of the current flow.

$$P_L(I) = 3 \cdot \sum_{l=1}^{n-1} R_l' \ell_l |I_l|^2.$$
(3)

- R'_l and ℓ_l denote the specific resistance in Ω/km and the length in m
- $|I_l|$ represents the magnitude of the complex current along the line
- The factor 3 reflects the fact that the lines consist of three phases.

$$I = \frac{1}{\sqrt{3}} \max\{\left|Y^{\mathrm{f}} \cdot V\right|, \left|Y^{\mathrm{t}} \cdot V\right|\},\$$

 $|\cdot|$ and max are to be understood component-wise



- active power demand P_i is given.
- $Q_i = P_i \tan(\varphi_i)$ and $\cos(\varphi_i) = \mu_i$

$$\underline{\mu}_i \leq \mu_i \leq \overline{\mu}_i$$

- Note that the power factors can only be set indirectly by manipulating inverters.
- voltages have to stay within some corridors, w

$$\underline{V}_i \leq |V_i| \leq \overline{V}_i$$

• Having the interface to the upper grid level in mind, we assume some bounds on *Q*₀ to be given by the DSO, i.e.

$$\underline{Q}_0 \leq Q_0 \leq \overline{Q}_0$$



$$\min_{\mu_{i} \in [\underline{\mu}_{i}, \overline{\mu}_{i}]} P_{L}(I) = 3 \cdot \sum_{l=1}^{n-1} R_{l}^{\prime} \ell_{l} |I_{l}|^{2}$$

$$subject to \quad \forall i \in \mathcal{V} :$$

$$\left[\begin{array}{c} P_{i} - |V_{i}| \sum_{j=1}^{n} |V_{j}| (G_{ij} \cos(\delta_{ij}) + B_{ij} \sin(\delta_{ij})) \\ P_{i} \cdot \tan(\varphi_{i}) - |V_{i}| \sum_{j=1}^{n} |V_{j}| (G_{ij} \sin(\delta_{ij}) - B_{ij} \cos(\delta_{ij})) \end{array} \right] = 0$$

$$I = \frac{1}{\sqrt{3}} \max\{ \left| Y^{\mathrm{f}} \cdot V \right|, \left| Y^{\mathrm{t}} \cdot V \right| \}$$

$$\left[\begin{array}{c} 4 \mathrm{b} \\ V_{i} \leq |V_{i}| \leq \overline{V}_{i} \quad \forall i > 0 \\ \mu_{i} = \cos \varphi_{i} \quad \forall i \in \mathcal{V} \\ |V_{0}| = 1, \quad \delta_{0} = 0 \end{array} \right]$$

$$\left[\begin{array}{c} 4 \mathrm{b} \\ 4 \mathrm{c} \\ 4 \mathrm{c}$$

Due to constraint (4b) the problem becomes non-convex.



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Details on implementation

*R'*₁, *l*₁ and the grid topology were provided by our industrial partner. *P*_i from Gaussian distribution with E(P) = 2.5 kW, σ(P) = 0.5 kW.

Table: Parameters used in the implementation.

We use the MATLAB package matpower to solve the PFEand MATLABs fmincon to solve the optimization. The fmincon setting is displayed in Table below. For the computation of Y, $Y^{\rm f}$ and $Y^{\rm t}$ we use the open-source software PandaPower.

option	setting	
Algorithm	interior-point	
MaxFunctionEvaluations	1e5	
StepTolerance	1e-16	

Table: fmincon setting.



We distinguish three scenarios with respect to controllability of the power factors:

- 1. $\cos(\varphi_i) = 0.9$ for all i > 0 (no optimization)
- 2. $\cos(\varphi_i) = \mu^*$ for all i > 0 (1-dimensional optimization)
- 3. $\cos(\varphi_i) = \mu_i^*$ for all i > 0 (*n*-dimensional optimization).

The corresponding objective function value is denoted by P_L^{ref} , P_L^{1D} , and $P_L^{n\text{D}}$, respectively.



Figure: Impact of the choice of μ on P_L (left) and Q_0 (middle) for the 1-dimensional unconstraint optimization problem and comparison of reactive power Q_i^{ref} of the reference scenario and Q_i^{\star} of the solution of the *n*-dimensional problem.

Change in active Power at a single node



Figure: Impact of changing the active power at one node *i* to $P_i = 5$ kW.



setting	P_L^{ref}	$P_L^{1\mathrm{D}}$	$P_L^{n\mathrm{D}}$
no manipulation	1.72	1.65	1.62
$P_{6} = 5$	1.75	1.67	1.64
$P_{12} = 5$	1.76	1.68	1.65
$P_{60} = 5$	1.72	1.64	1.61
$P_{61} = 5$	1.74	1.66	1.63
$P_{63} = 5$	1.73	1.66	1.63
$P_{63} = 10$	1.76	1.68	1.64
$P_{63} = 20$	1.87	1.75	1.71
$P_{63} = 50$	2.16	1.96	1.93
$\mathrm{std} = 1$	1.74	1.67	1.64
$\mathrm{std}=2$	1.79	1.71	1.68
$\mathrm{std}=4$	1.82	1.73	1.69
$\mathrm{std}=8$	1.88	1.78	1.73

Table: Impact of manipulating the active power at a single bus or increasing the variance of the active power within the whole grid on the objective function value. All values are given in kW.

Strong disturbance at bus 63



Figure: Impact of changing the active power P_i at one node *i* (major disturbance).





(a) Reference scenario without disturbance.



(b) Reference scenario with $P_{63} = 50$.





Figure: Difference between line losses before and after (*n*-dimensional) optimization with $P_{63} = 50$ kW.

Changes with increased variance



Figure: Impact of increasing the variation of the P_i .



- Modeling is a crucial part of solving the problem
- Different optimization problems everywhere
- $\bullet\,$ Models are complex and need to be communicated $\Rightarrow\,$ Surrogate Models aka reduced models
- There are hidden controls that can be used.

Thank you for your attention!

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- M Baumann, S Grundel, P Sauerteig, K Worthmann Surrogate models in bidirectional optimization of coupled microgrids at-Automatisierungstechnik 67 (12), 1035-1046, 2019