

Mathematical Programming for the Market Integration of Power-to-X Hybrid Power Plants The Case of a Plant in Denmark

Jalal Kazempour (DTU)

PowerWeb Annual Conference, TU Delft September 27, 2023

All credits of this lecture go to



Enrica Raheli (PhD Student)



Andrea Gloppen Johnsen (PhD Student)



Yannick Werner (PhD Student)



Alice Patig (PhD student)



Lesia Mitridati (Assistant Professor)



Manuel Tobias Baumhof (former MSc Student)



Marco Saretta (former MSc Student)



Anton Ruby Larsen (former MSc Student)



Mads Esben Hansen (former MSc Student)



2/35

SIEMENS Gamesa EUDPO



Towards H₂-driven business model: Portfolio management of a multi-energy system under uncertainty







Preliminaries

- Why Power-to-X
- \circ An Overview of TSO Services
- Challenges

Physical Modeling of Electrolyzers

Value of Ancillary Services for Electrolyzers

Portfolio Management Problem: Distributionally Robust Optimization



Preliminaries:

Why Power-to-X?



4/35

P2X strategy in Denmark: New electrolyzers to be installed

Nordjylland Sjælland Annonceret Projekt Annonceret elektrolysekapacitet 2030 Projekt elektrolysekapacitet 2030 120 MW Aalborg Havn - European Energy 1 24 Arcadia eFuels 2 Hanstholm Havn - European Energy tbd 1, 3, 8, 9 25 Vordingborg Biofuels 200.000 tCH0H/år 3 Green Hub CCU Aalborg tbd 26 European Energy - Nakskov tbd 4 Handest 50 MW Hovedstaden 5 Heiring 35 MW HFC Marine 0,5 MW 6 27 Bornholm Bunker Hub tbd 4, 5, 6, 7 1,2 MW 7 HyBalance 28 Green Fuels for Denmark 1,3 GW Metanolprojekt v. Nordjyllandsværket 300-400 MW 8 29 H2RES 2 MW 0,3 MW 9 Power2Met Nordsøen 30 BrintØ 10 GW 13 Midtjylland 27 10 Brande - Flø Hydrogen 0,4 MW 10 Green Hydrogen Hub 1GW 11 12 Greenlab Skive - GreenHyScale 400 MW 13 REDDAP 10 MW 30 4-6 GW of electrolyzers by 2030 28, 29 **Syddanmark** 20 MW • 1.25 billion DKK in support 14 50 MW 16 12 MW 18 • CO₂ emission reduction: **2.5-4.0** 4.25 1GW 1GW 1GW million tons Brintbranchen



Why Power-to-X?

- 1. Current hydrogen demand
 - 90 Mt of H2 in 2020
 - Only 0.03% from water electrolysis
- 2. Indirect electrification and decarbonization of
 - Heavy transport (heavy-duty vehicles, aviation and shipping
 - Industry
- 3. Added value to the **power system:**
 - Higher utilization of renewables in the grid (reduce curtailment)
 - Ancillary services provision (high ramping rates)



530 Mt in 2050 in IEA's Net Zero









What are the products of the hybrid power plant?





Portfolio of products:

- **Power** (to be sold in various trading floors)
- Hydrogen (fixed price)
- TSO services such as frequency-based ancillary services (electrolyzers are fast flexible demands!)
- **DSO services** (if the plant is connected to a distribution grid) such as grid congestion services



Preliminaries:

An Overview of TSO Services

DTU

8/35

Recall: Who clears what market (European setup)?

By the market operator (e.g., Nord Pool)



Synchronous Grid Areas in Europe



Synchronous Grid Areas in Europe



Frequency-based Ancillary Services in DK1 and DK2



Source: Energinet (Gennemgang af Nuværende Systemydelse Markeder)

Ancillary services in DK1 (as part of the continental area)

- FCR (frequency containment reserve)
- aFRR (automatic frequency restoration reserve)
- mFRR (manual frequency restoration reserve)

Ancillary services in DK2 (as part of the Nordic area)

- FFR (fast frequency reserve)
- FCR-D (D stands for disturbance)
- FCR-N (N stands for normal)
- o aFRR
- o mFRR



Specifics of Ancillary Services in DK1 and DK2



Source: Energinet (Gennemgang af Nuværende Systemydelse Markeder)



Source: Energinet (Gennemgang af Nuværende Systemydelse Markeder)



Source: Energinet (Gennemgang af Nuværende Systemydelse Markeder)

Ancillary Service Markets in DK1 and DK2



Timeline for reservation auctions for all ancillary services in Denmark Service mFRR has monthly and daily auctions. Both FCR-N and FCR-D have two auctions, running two days and one day before delivery. The auction scheme is shown together with the origin of payment (third row) and the speed of full response (fourth row). For aFRR, the speed of full response is 15 min in DK1 and 5 minutes in DK2, and will be 5 min in DK1 from 2024. *Abbreviations:* PaB: pay-as-bid. UP: uniform pricing. R: reservation payment. A: activation payment. M: month. D: day. m: minutes. s: seconds.

Source: Peter A. V. Gade, Trygve Skjøtskift, Henrik W. Bindner, and JK, "Ecosystem for demand-side flexibility revisited: The Danish solution", *The Electricity Journal*, vol. 35, no. 9, Article no. 107206, November 2022 [link | arXiv]

13/35



14/35

Historical data: Activated FCR-D and FCR-N in DK2 (2021-2022)



Credit: Marco Saretta



Historical data: Activated FCR-D and FCR-N in DK2 (2021-2022)



FCR-D was very rarely activated! Service providers received payments due to capacity reservation but were activated very rarely!

Credit: Marco Saretta



Historical data: FCR-D and FCR-N prices in DK2 (2015-2022)



FCR-D Down (a service when frequency is between 50.1 and 50.5 Hz) started in January 2022

Credit: Marco Saretta

15/35



Challenges



Portfolio Management Problem of the Hybrid Power Plant



Electricity

- Day-ahead price forecast
- Balancing price forecast
- $\circ~$ Wind power forecast

Ancillary services

- FCR/aFRR/mFRR reservation price forecast
- Forecast of activation for each service

Hydrogen

- Hydrogen price
- Minimum hydrogen demand (e.g., over a day)
- Tube trailer availability (e.g., over the next day)

Other technical data

Maximize (expected) profit Subject to physical and bidding constraints



Scheduling (bidding) decisions



Ο

Portfolio Management Problem of the Hybrid Power Plant



Hydrogen

- Hydrogen price (fixed price) Ο
- Minimum hydrogen demand (e.g., over a day) (certain) Ο
- Tube trailer availability (e.g., over the next day) (uncertain) Ο

Other technical data (certain)





Scheduling (bidding) decisions



Portfolio Management Problem of the Hybrid Power Plant



Hydrogen

- Hydrogen price (fixed price)
- Minimum hydrogen demand (e.g., over a day) (certain)
- Tube trailer availability (e.g., over the next day) (uncertain)

Other technical data (certain)

Maximize (expected) profit Subject to physical and bidding constraints



Any challenge?

Scheduling (bidding) decisions





Hydrogen

- Hydrogen price (fixed price) Ο
- Minimum hydrogen demand (e.g., over a day) (certain) Ο
- etc Tube trailer availability (e.g., over the next day) (uncertain) Ο

Other technical data (certain)

High dimensionality

• Many (potentially correlated) sources of uncertainty Maximize

Subject t Non-stationarity

WIND FARM

Grid trade

POWER GRID

• The analysis of historical data suggests our stochastic environment is not necessarily stationary!

Renewable energy sou Lack of enough historical data

- Example 1: FCR-D down market has been recently established
- Example 2: Denmark has recently switched to a 1-price balancing scheme (before it was 2-price)

Conditionality

• The distribution of forecast error depends on the point forecast.



Portfolio Management Problem of the Hybrid Power Plant



- Hydrogen price (fixed price)
- Minimum hydrogen demand (e.g., over a day)
- Tube trailer availability (e.g., over the next day

Other technical data (certain)

Maximize (expected) profit Subject to physical and bidding constraints



Any other challenge related to modeling the physics of the plant?

Scheduling (bidding) decisions



- Hydrogen price (fixed price)
- Minimum hydrogen demand (e.g., over a day) (certain)
- Tube trailer availability (e.g., over the next day) (uncertain)

Other technical data (certain)

Approximation

.....

Experimental



Several stakeholders in DK are interested in different aspects of such a portfolio management problem





Site in Flø, Brande, belonging to Siemens Gamesa



Physical Modeling of Electrolyzers:

Piece-wise Linear Approximation

Question: To what extent does it matter to model the physics of electrolyzers in a detailed manner?

M. T. Baumhof, E. Raheli, A. Gloppen Johnsen, and JK, "Optimization of hybrid power plants: When is a detailed electrolyzer model necessary?," IEEE Belgrade PowerTech 2023. <u>https://arxiv.org/abs/2301.05310</u>

Codes: <u>https://github.com/mtba-dtu/detailed-electrolyzer-model</u>



Hydrogen Production and Efficiency Curves

Consider a 52.25-MW alkaline electrolyzer, working at 90 °C and 30 bar.



A simple idea:

18/35

- Hydrogen production curve is linearized by a couple of red segments (each segment: Ax+B) \rightarrow resulting model: MILP
- The approximate efficiency curve (red) is still nonlinear due to the intercept *B*, but this curve will not be used in our optimization model.

Operating States of Electrolyzers



Online

- Power conumption active
- Hydrogen production

Offline

- No power consumption
- No hydrogen production
- When transitions from *Offline* to *Online*, pay the cold startup cost

Standby

- No hydrogen production
- Power consumption reduced, to keep the electrolyzer hot and pressurized
- No cold start cost when transitions from *Standby* to *Online*

19/35





- Only electricity and hydrogen (no ancillary services)
- One year simulation (8760 hours)
- Deterministic (known wind power and price profiles)





- Only electricity and hydrogen (no ancillary services)
- One year simulation (8760 hours)
- Deterministic (known wind power and price profiles)

Wind farm	Capacity	104.5	MW
Electrolyzer	Capacity	52.25	MW
	Standby load	0.523	MW
	Minimum load	7.838	MW
	Pressure	30	bar
	Temperature	90	°C
	Maximum current density	5,000	A/m^2
	Startup cost	50	€/MW
	TSO tariff	15.06	€/MWh
Storage	Capacity	22,000	kg
	Input/Output	912.13	kg/h
Compressor	Inlet temperature	40	°C
	Inlet pressure	30	bar
	Outlet pressure	200	bar
	Mechanical efficiency	75%	
Hydrogen	Price	2.10	€/kg
	Minimum demand	2,750	kg/d

Results: Impact of the number of segments 1/2

(Number of states fixed)

DTU

=

21/35

Power consumption schedule of the electrolyzer in an example high-wind day



- By adding more segments, the electrolyzer consumes power more dynamically (following the day-ahead price signal)
- This happens within a specific price range


Results: Impact of the number of segments 2/2

Histogram of the day-ahead hourly prices in 2019



$$\lambda^{\mathrm{DA,ub}} = \frac{\lambda^{\mathrm{h}} \eta^{\mathrm{max}} P^{\eta,\mathrm{max}}}{P^{\eta,\mathrm{max}} - P^{\mathrm{sb}}}$$

$$\lambda^{\mathrm{DA,lb}} = \lambda^{\mathrm{h}}(\eta^{\mathrm{fl}} + C^{\mathrm{e}}\eta'(x)|_{x=C^{\mathrm{e}}})$$

 $\lambda^{DA,ub}$ and $\lambda^{DA,lb}$ depends only on:

- electrolyzer efficiency curve
- standby power consumption
- hydrogen price



Based on the **range of day-ahead prices**, we know "*a priori*" whether adding more segments matter



Physical Modeling of Electrolyzers:

Conic Relaxation

E. Raheli, Y. Werner, and JK, "A conic model for electrolyzer scheduling," <u>https://arxiv.org/abs/2306.10951</u>

Codes: <u>https://github.com/ELMA-Github/conic_electrolyzer_paper</u>



DTU Wind and Energy Systems



23/35

Potential Solutions for Convexification of the Curve





Potential Solutions for Convexification of the Curve



Model HYP-MIL

- Piece-wise linear approximation of the hydrogen production curve
- One binary per segment

23/35



23/35

Potential Solutions for Convexification of the Curve



Model HYP-L

- Outer approximation (relaxation)
- This is a common approach to convexify the gas flow Weymouth equations.
- \circ No binary

Relaxation



Potential Solutions for Convexification of the Curve

Model HYP-SOC

- Fitting a conic equation, with the same efficiency peak
- o Conic relaxation
- \circ No binary





Potential Solutions for Convexification of the Curve

Model HYP-MISOC

- Fitting two conic equations Ο
- **Conic relaxation** Ο
- One binary only to choose the active conic constraint Ο



Experimental Relaxation ••••• Approximation



24/35

Case Study: Tightness of the Relaxation

HYP-SOC model (identical observations for other models)

Day	Minimum daily hydrogen demand constraint	Electricity prices	Wind	Tightness
а	Not binding	Most of hours: negative prices	Low wind	Exact
b	Binding	All hours: positive prices	High wind	Exact
С	Binding	Most of hours: negative prices	High wind	Inexact
d	Binding	Most of hours: positive prices	High wind	Exact 🗾

DTU Wind and Energy Systems

Case Study: Tightness of the Relaxation



Some observations

- Day (a): if the demand constraint is not binding, the relaxation is always exact.
- Day (b): if the demand constraint is binding but prices are positive, the relaxation is always exact.
- Day (c): if the demand constraint is binding and there are many negative prices → relaxation is inexact.
- Day (d): if the demand constraint is binding and there are a few negative prices \rightarrow the relaxation is **exact.**

> Mathematical proofs of the exactness of the conic relaxation under (prevalent) operational circumstances are available in the paper.



Value of Ancillary Services for Electrolyzers

M. Saretta, E. Raheli, and JK, "Electrolyzer scheduling for Nordic FCR services," IEEE SmartGridComm 2023, Glasgow, Scotland, November 2023. <u>https://arxiv.org/abs/2306.10962</u>

Codes: <u>https://github.com/marco-srtt/electrolyzer_nordic_FCR</u>

A. Gloppen Johnsen, L. Mitridati, D. Zarrilli, and JK, "Value of ancillary services for electrolyzers," soon to be shared Codes: TBD



Hybrid Power Plant in Ancillary Service Markets

Let's consider a subset of existing services in DK1, including mFRR (up and down) and FCR. There are minimum bid size and bid time length constraints.



Let's consider a subset of existing services in DK1, including mFRR (up and down) and FCR. There are minimum bid size and bid time length constraints.

mFRR up:

- The hybrid power plant is paid for the reservation sold based on mFRR up market price.
- If activated (partial or full), the plant is paid at the balancing price for the energy not consumed. Meanwhile, the plant will
 produce less hydrogen due to less electric energy consumption.





Let's consider a subset of existing services in DK1, including mFRR (up and down) and FCR. There are minimum bid size and bid time length constraints.

mFRR up:

- The hybrid power plant is paid for the reservation sold based on mFRR up market price.
- If activated (partial or full), the plant is paid at the balancing price for the energy not consumed. Meanwhile, the plant will
 produce less hydrogen due to less electric energy consumption.

mFRR down:

- The hybrid power plant is paid for the reservation sold based on mFRR down market price.
- If activated (partial or full), the plant pays at the balancing price for the additional energy consumed. Meanwhile, the plant will produce more hydrogen due to extra electric energy consumption.



Let's consider a subset of existing services in DK1, including mFRR (up and down) and FCR. There are minimum bid size and bid time length constraints.

mFRR up:

- The hybrid power plant is paid for the reservation sold based on mFRR up market price.
- If activated (partial or full), the plant is paid at the balancing price for the energy not consumed. Meanwhile, the plant will
 produce less hydrogen due to less electric energy consumption.

mFRR down:

- The hybrid power plant is paid for the reservation sold based on mFRR down market price.
- If activated (partial or full), the plant pays at the balancing price for the additional energy consumed. Meanwhile, the plant will produce more hydrogen due to extra electric energy consumption.

FCR:

- The hybrid power plant is paid for the reservation sold based on FCR market price.
- No payment/cost in the balancing stage for the activation. Not an energy-intense service. The activation is automatic based on frequency deviations between 49.9 and 50.1 Hz, which is quite symmetric over a time period, so one can imagine FCR up and down activations cancel out each other.

- We use realized prices in DK1 in 2021 and 2022 (ideal benchmark to obtain the highest potential value of services).
- o Deterministic model



27/35









28/35





28/35



Quantities Frequency (\log) 10_3 10_1 DK1 2021 DK1 2022 60 60 50500 Price (EUR) 4040Reserves [GW] 30 30 202010100 0 $\alpha = 0$ Oracle No AS $\alpha = 0$ Oracle No AS $\alpha = 1$ $\alpha = 1$ Model version Model version FCR mFRR up

Prices

 10^{3}

 10^{1}

0

DK1 2022

2000

Price (EUR)

1

1

DK1 2021

1000

29/35



Portfolio Management Problem: Distributionally Robust Optimization















Timeline of clearing ancillary service markets in Denmark

Reference: P. V. Gade et al., "Ecosystem for demand-side flexibility revisited: The Danish solution," *The Electricity Journal*, 2022





- Model uncertainty sources accurately
- Model and mitigate risk of decisions





31/35





Historical forecasting error = Forecast - Observation



Concept





Concept





Scenario-Based Stochastic Optimization



- Aim: Max. expected profit for given distribution



Scenario-Based Stochastic Optimization



- Aim: Max. expected profit for given distribution
- Challenge: Data-intensive to estimate probability distribution ℙ

Distributionally Robust Optimization



- Aim: Max. expected profit for worst-case distribution in ambiguity set
- Benefit: Data-driven approach





- Model uncertainty sources accurately
- Model and mitigate risk of decisions



Consider **expectation** from **worstcase** <u>forecasting error distribution</u>



- Model uncertainty sources accurately
- Model and mitigate risk of decisions





- Model uncertainty sources accurately
- Model and mitigate risk of decisions



850DRO Control 825SAA DET Average Daily Return [EUR] Active realization Passive realization 800 775**Passive Active** Gap 750725700675

8

9

Percentage improvement [%]

 $10 \ 11 \ 12 \ 13 \ 14 \ 15 \ 16 \ 17 \ 18$

0

2

3

4

5

6



Out-of-Sample Results





Out-of-Sample Results





Out-of-Sample Results



34/35


Out-of-Sample Results



34/35



□ **Operational details** of P2X assets are important for the scheduling of the system.

□ This is a **multi-market** decision-making problem:

- Day-ahead and balancing electricity markets
- Ancillary service (FCR, aFRR, mFRR) markets
- \circ Hydrogen

Modeling uncertainty is key, while there might be lack of sufficient historical data to accurately characterize underlying probability distributions!





Jalal Kazempour Associate Professor, Head of Section jalal@dtu.dk www.jalalkazempour.com

Open-access publications available at:

https://orbit.dtu.dk/en/organisations/energy-analytics-and-markets